

# 高エネルギー宇宙線におけるハドロンカスケード模型

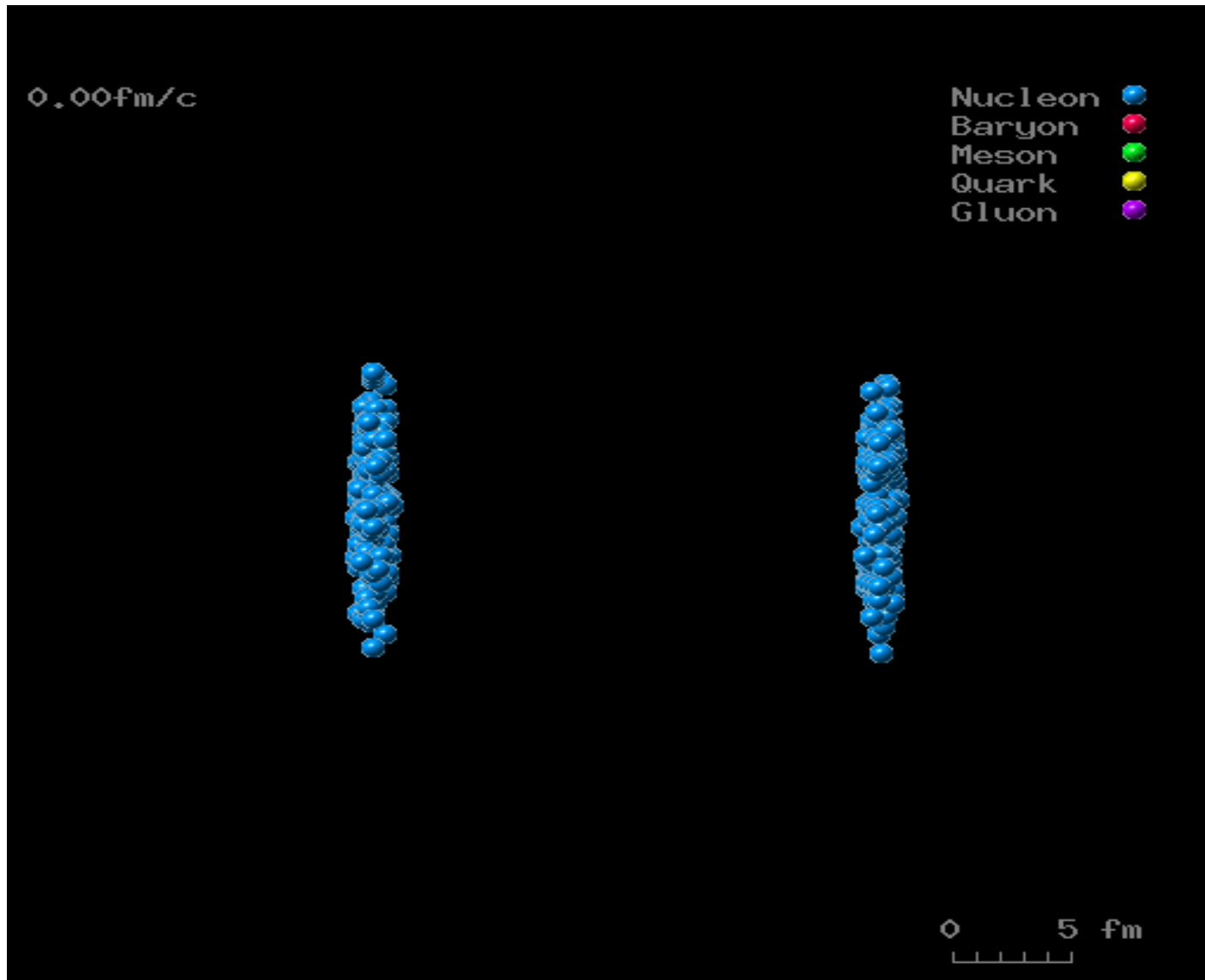
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(国際教養大学)

- 高エネルギー重イオン衝突におけるハドロンカスケード模型
- モデルの説明: インプット (ハドロン散乱レベルでの素過程)
- 応用例
- まとめ

# High energy heavy ion collision

Pb+Pb collision at E=200 AGeV

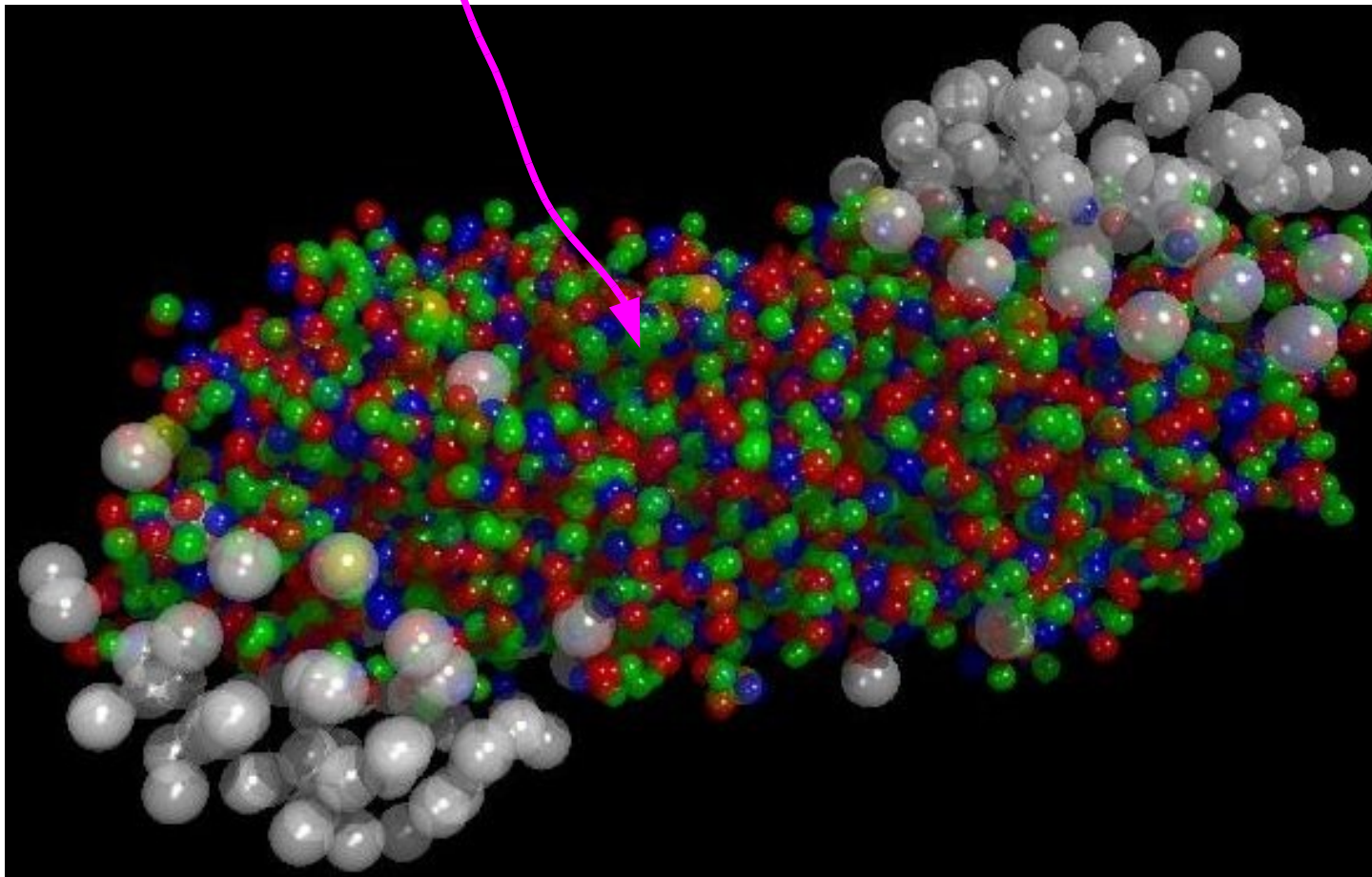
Animation  
from  
Hydrodynamic  
Cascade  
model  
JAM



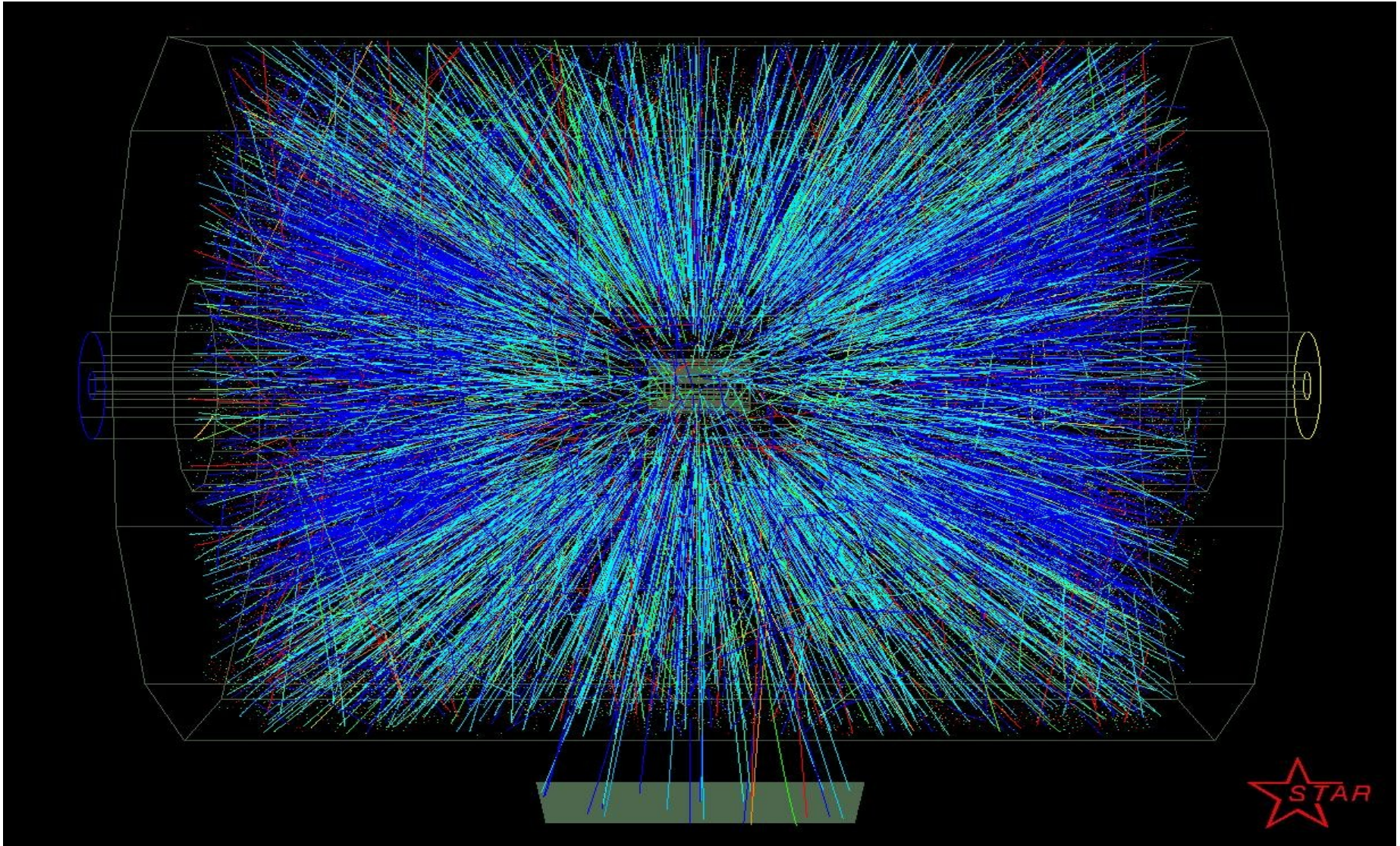
After the collision,  
matter looks like this.

*UrQMD simulation*

**Hot and dense matter created!**

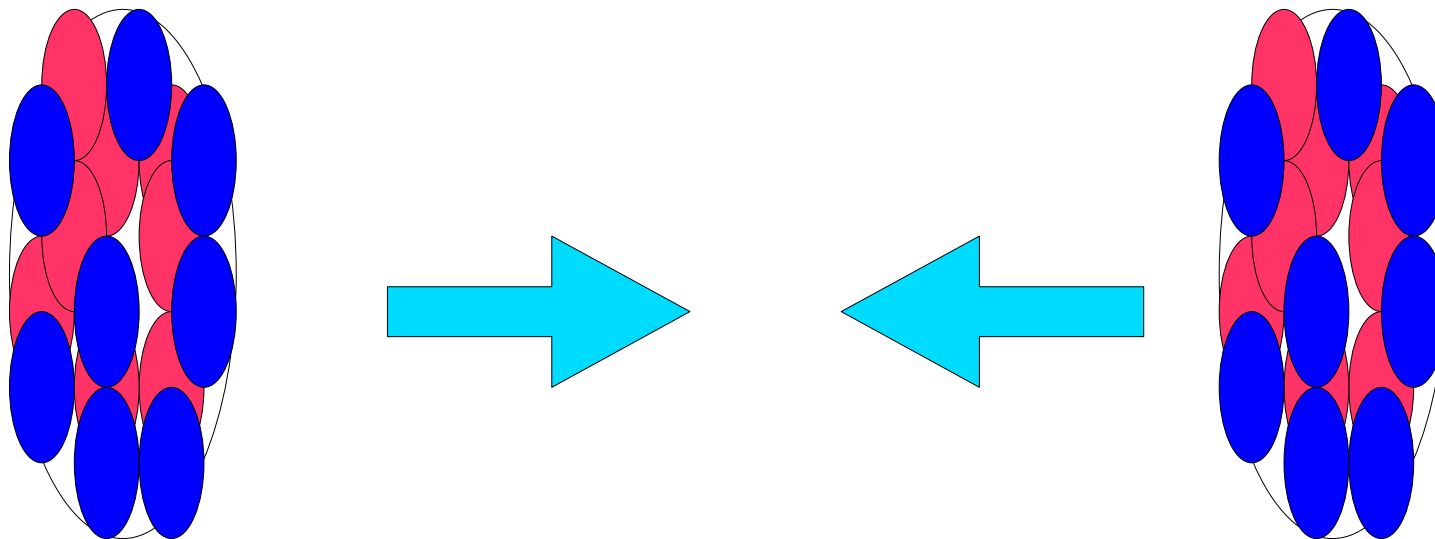


# Gold beam-beam collision event at RHIC experiment



# Hadron cascade の簡単な説明

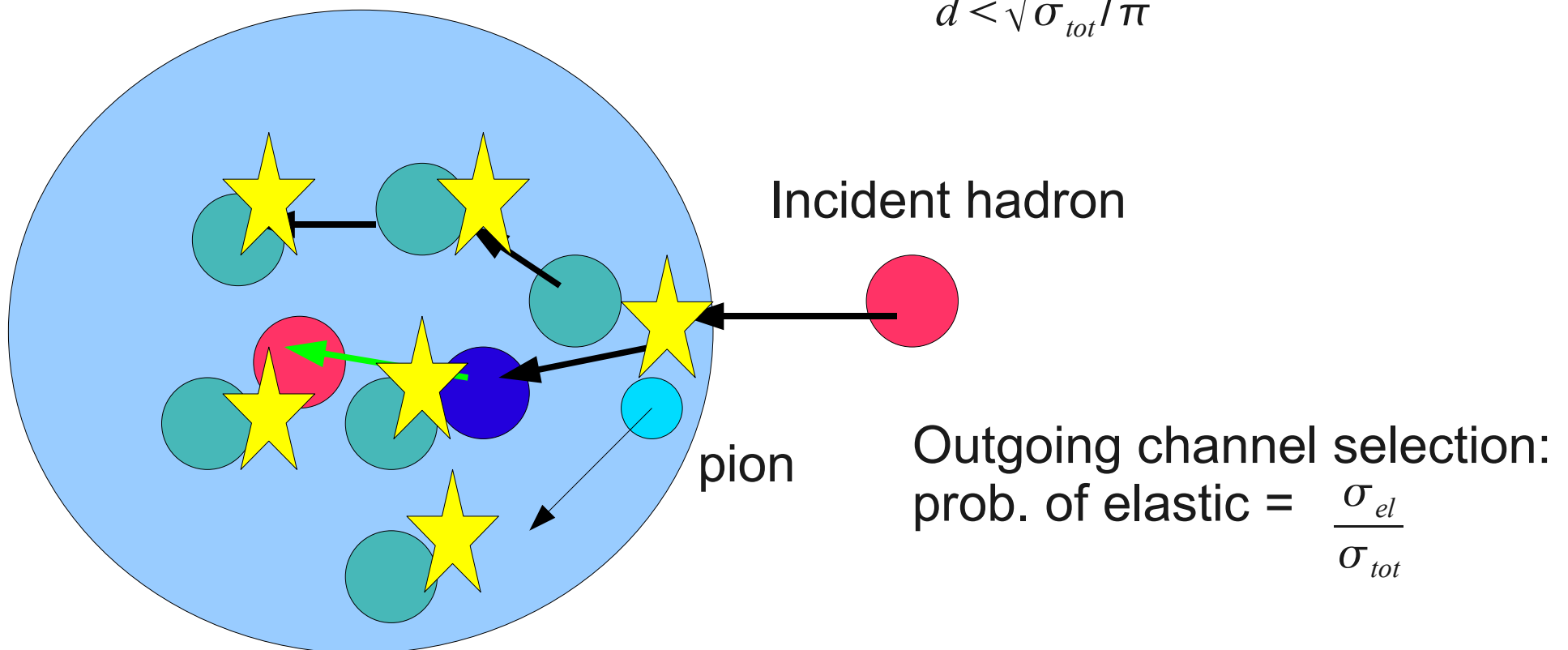
1. Initial state (before collision): Nucleons are sampled according to Woods-Saxon distribution, momentum of each nucleon is sampled by Fermi momentum, boost two nucleus according to the corresponding incident energy.



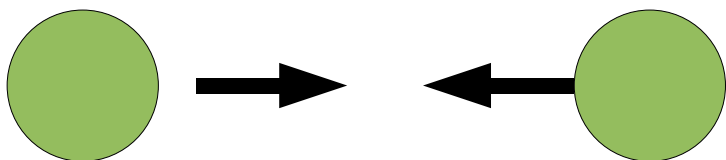
# ハドロン-ハドロン散乱の インコヒーレントな重ね合わせ

2. Straight line trajectories until particles interact
3. Collision at closest approach

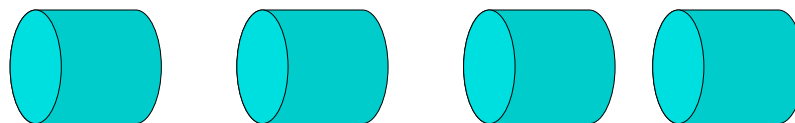
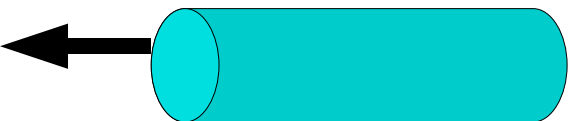
$$d < \sqrt{\sigma_{tot}/\pi}$$



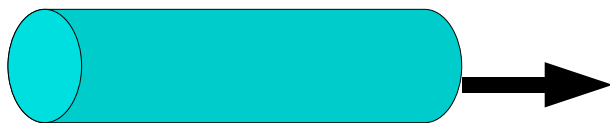
- すべての可能な素過程
- 粒子発生の時空発展



String excitation of hadrons



String decay into hadrons



# Hadronic transport models

## OSCAR (Open Standard Codes and Routines)

<http://nt3.phys.columbia.edu/OSCAR/>

**RQMD**

**UrQMD**

Frankfurt group: <http://th.physik.uni-frankfurt.de/~urqmd/>

**GiBUU**

The Giessen Boltzmann-Uehling-Uhlenbeck project  
<http://gibuu.physik.uni-giessen.de/GiBUU/>

**JAM**

<http://quark.phy.bnl.gov/~ynara/jam/>

Y.Nara, N.Otuka, A.Ohnishi, K.Niita and S.Chiba,

"Study of relativistic nuclear collisions at AGS energies from p + Be to Au + Au with hadronic cascade model,"

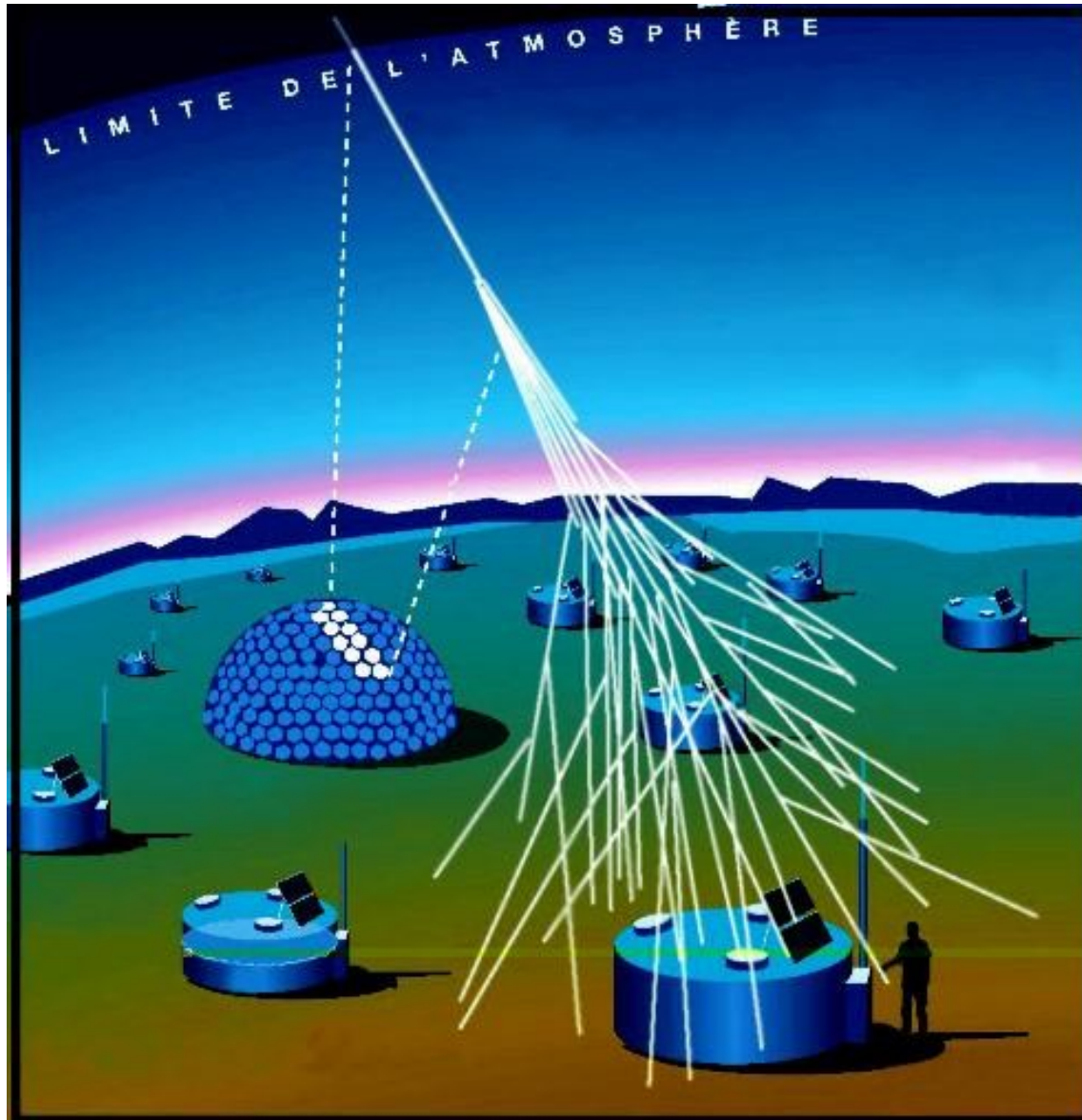
Phys. Rev. C61, 024901 (2000) [arXiv:nucl-th/9904059].

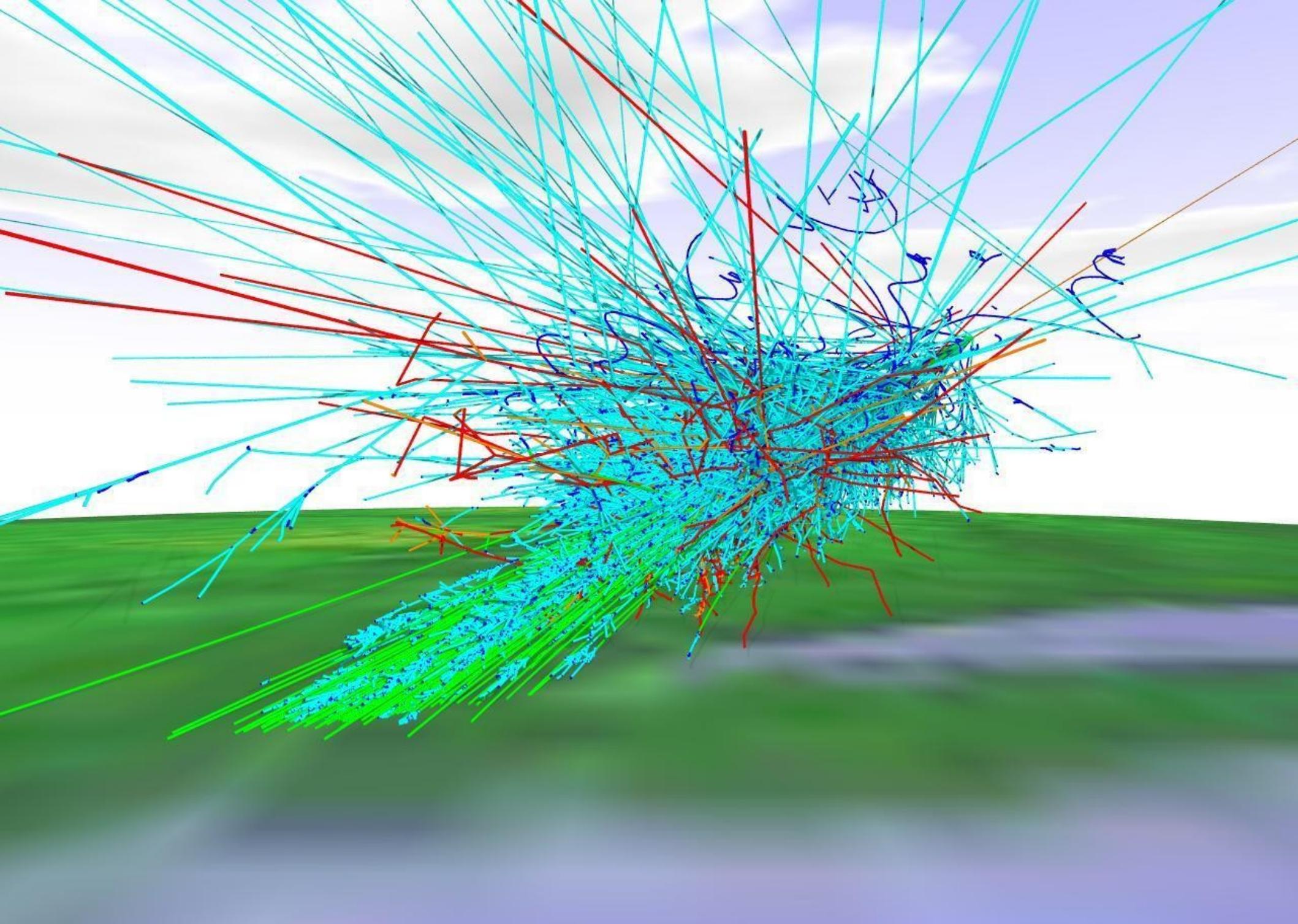


# Applications of hadronic cascade code

- hadron-nucleus collisions (proton, pion, kaon,....)
- Nucleus-nucleus collisions
- Gamma-nucleus collisions
  - Hydrodynamics + hadron cascade
  - Parton cascade + hadron cascade
  - GIANT4
  - Air shower model of cosmic ray

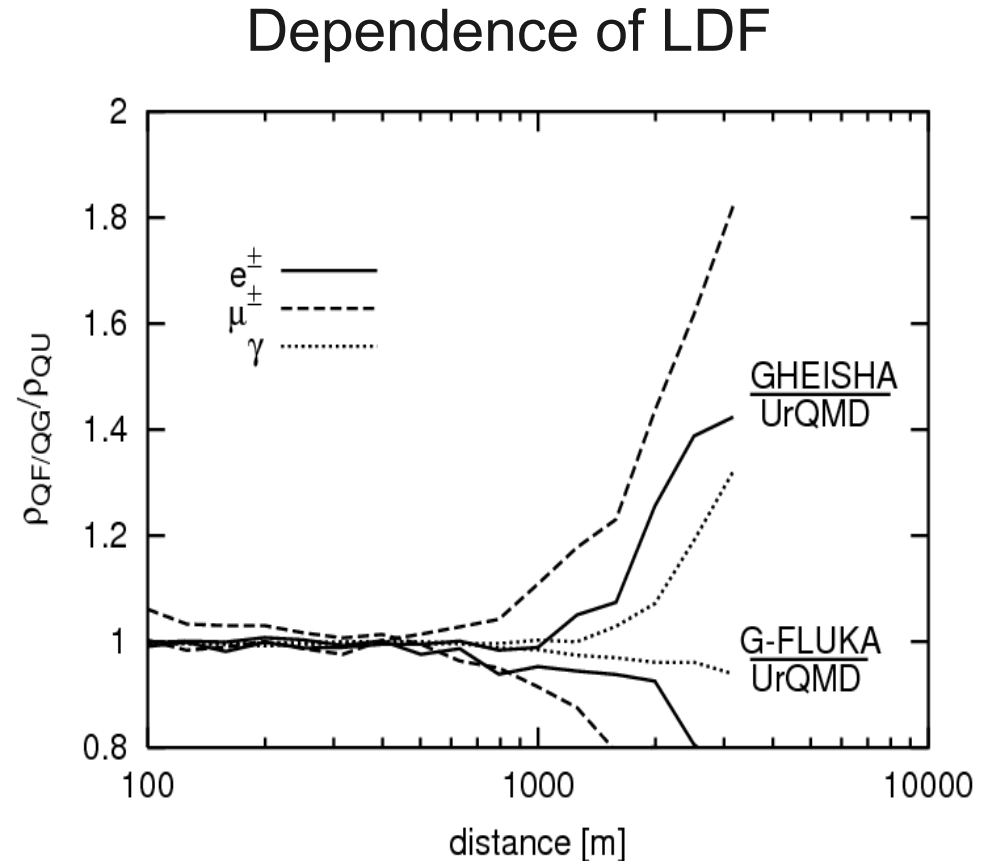
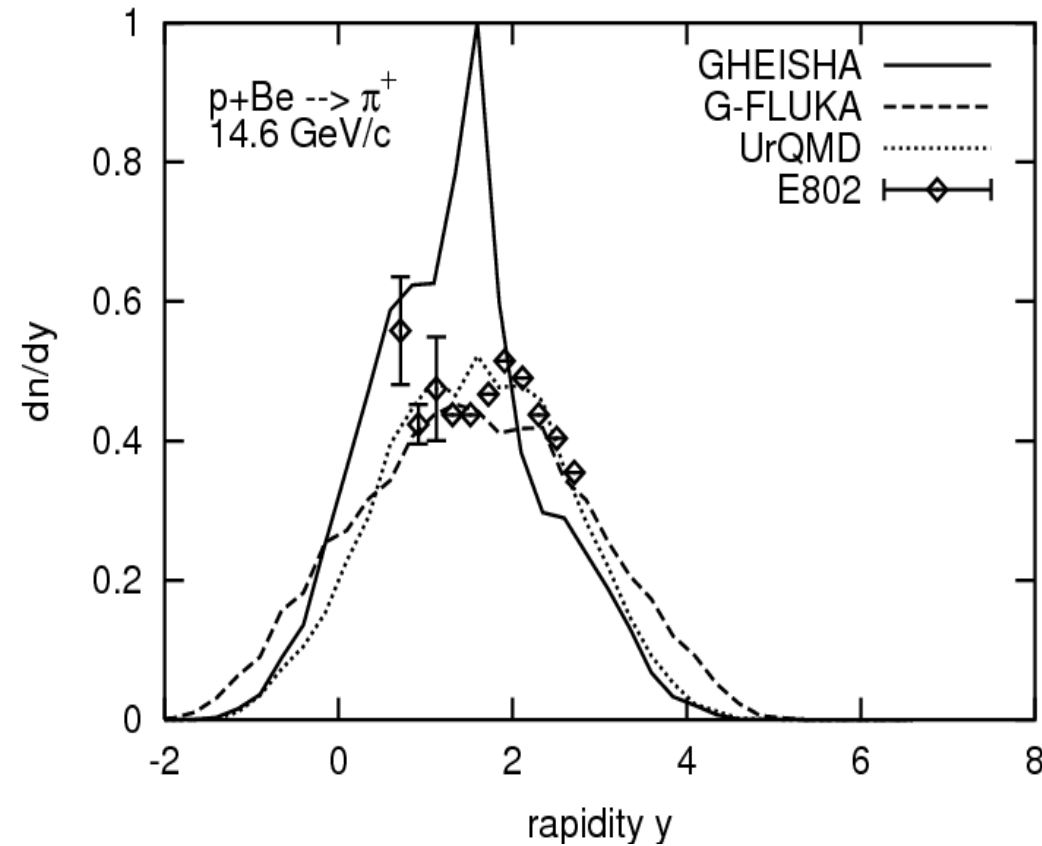
Air shower simulations needed for analysis and interpretation of data





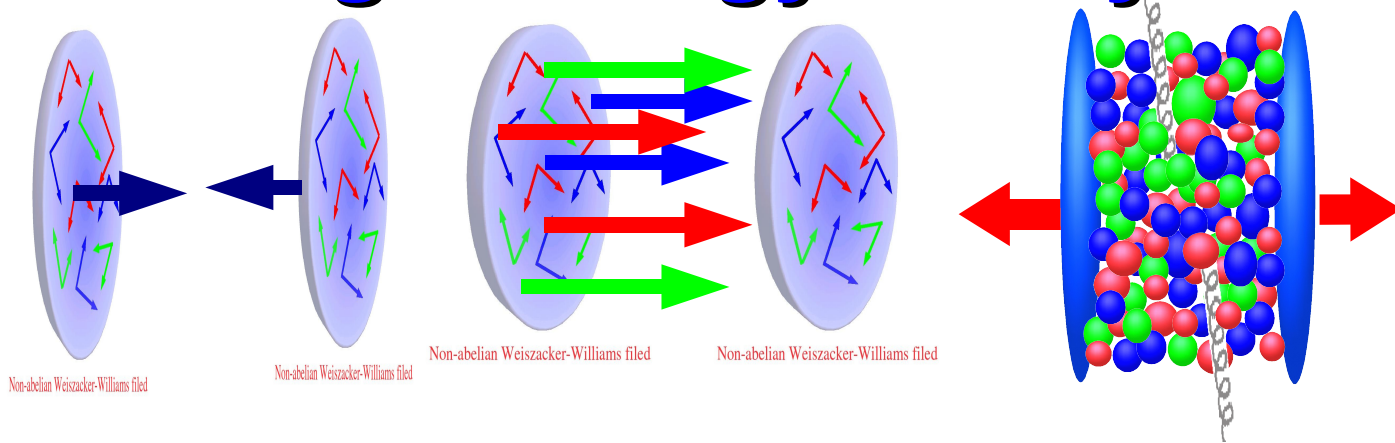
*Hajo Drescher, Frankfurt U.*

# Model dependence of rapidity distribution



H. J. Drescher, M. Bleicher, S. Soff and H. Stoecker, Astropart. Phys. 21, 87 (2004)

# High energy heavy ion collisions



$$\tau = 0$$

$$\tau \approx 1/Q_s$$

$$\tau \approx 1 \sim 2 \text{ fm}/c$$

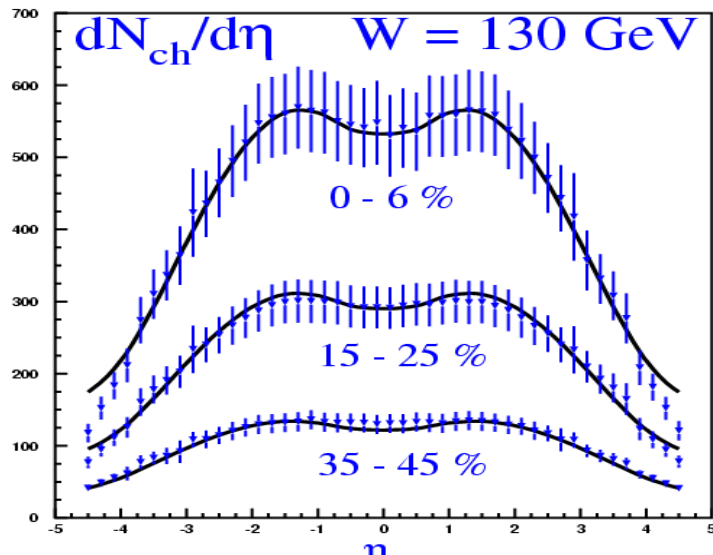
CGC

Non equilibrium

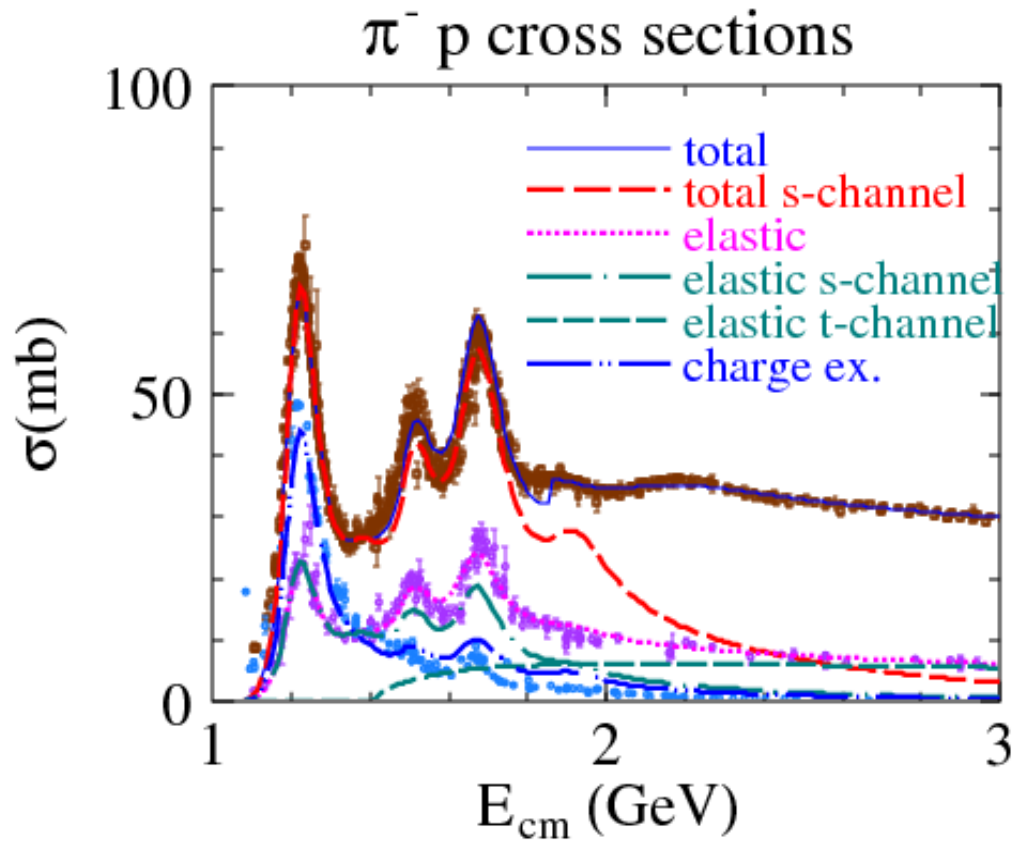
Hydro evolution

Hadron gas

time



# Modeling low energy $\pi$ -p cross sections



- S-channel inelastic:  
 $\pi$ -p  $\rightarrow$  resonance (or string)
- T-channel inelastic:  
 $\pi$ -p  $\rightarrow$  resonance + resonance
- Elastic
- Charge exchange:  $\pi^- p \rightarrow \pi^0 n$

# Hadronic Cross sections in JAM

$$\begin{aligned}\sigma_{tot}(s) &= \sigma_{el}(s) + \sigma_{ch}(s) + \sigma_{ann}(s) \\ &+ \sigma_{t-R}(s) + \sigma_{s-R}(s) \quad : \text{Resonance} \\ &+ \sigma_{t-S}(s) + \sigma_{s-S}(s) \quad : \text{String}\end{aligned}$$

## Resonance production (absorption)

$$\sigma_{t-R}(s) : NN \leftrightarrow N\Delta, \quad NN \leftrightarrow N^*\Delta^*, \dots$$

$$\sigma_{s-R}(s) : \pi N \leftrightarrow \Delta, \quad \bar{K}N \leftrightarrow Y^*, \dots$$

## String formation

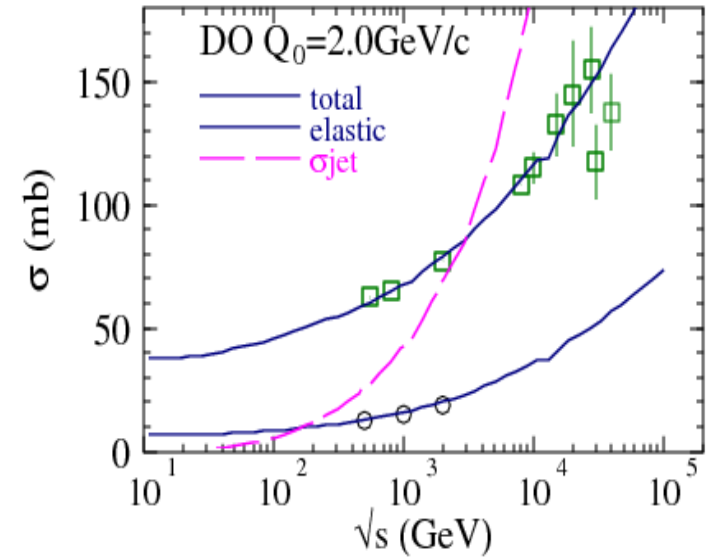
$$\sigma_{t-S}(s) : NN \rightarrow \text{String} + \text{String},$$

$$\sigma_{s-S}(s) : \pi N \rightarrow \text{String}$$

# Eikonal Formulation for pQCD (HIJING)

$$\sigma_{t-S}(s) = 2\pi \int_0^\infty db^2 [1 - \exp(\chi(b, s))],$$

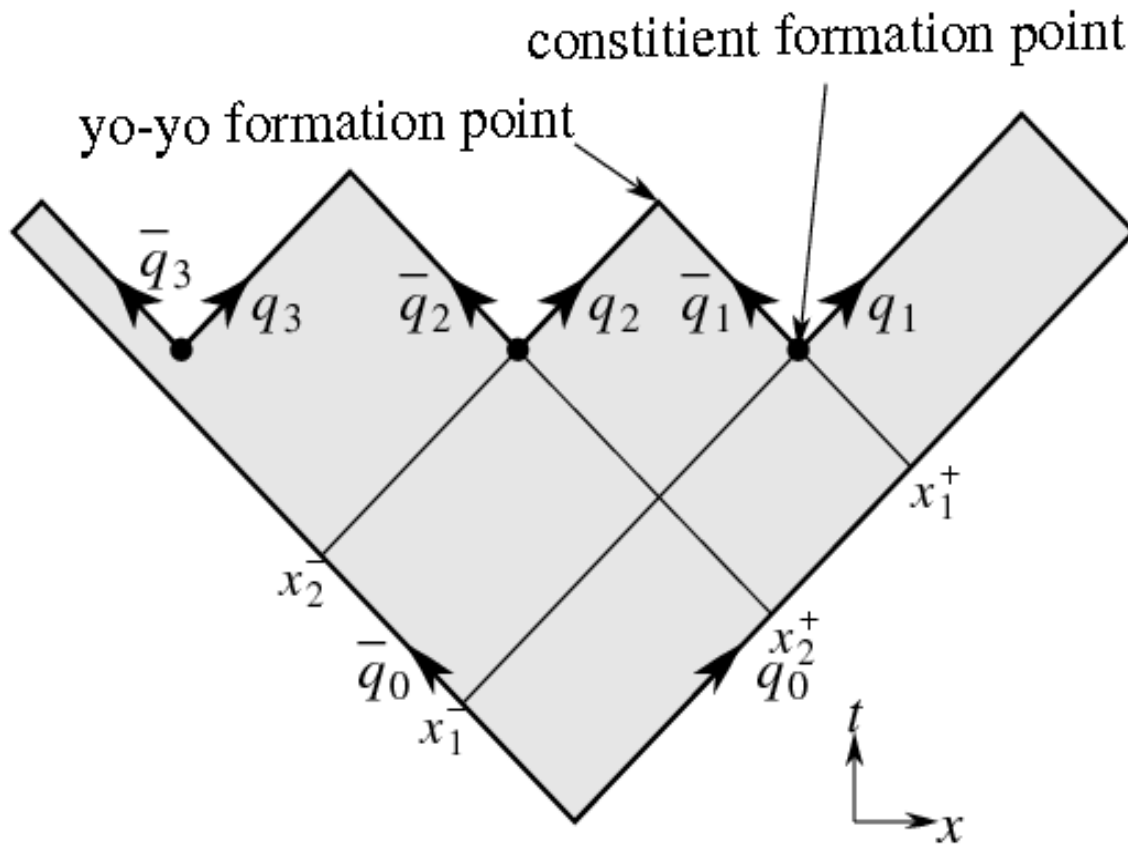
$$\chi(b, s) = \frac{1}{2} (\sigma_{jet}(s) + \sigma_{soft}(s)) A(b, s)$$



$$\sigma_{jet} = \int_{p_0^2}^{s/4} dp_T^2 dy_1 dy_2 \frac{1}{2} K \sum_{a,b} x_1 x_2 f_a(x_1, P_T^2) f_b(x_2, P_T^2) \frac{d\sigma^{ab}(\hat{s}, \hat{t}, \hat{u})}{d\hat{t}}$$

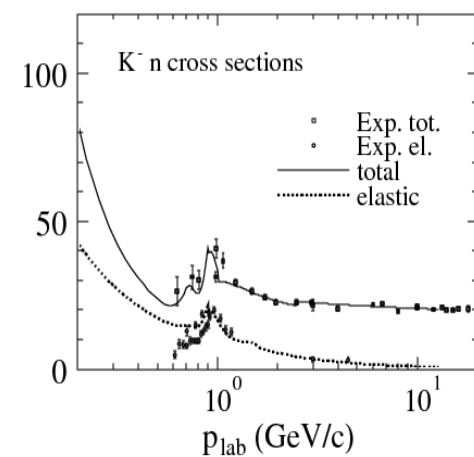
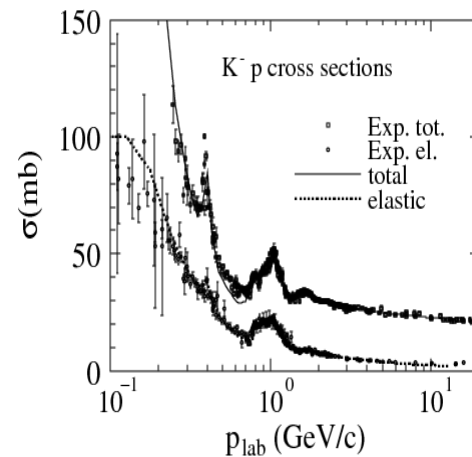
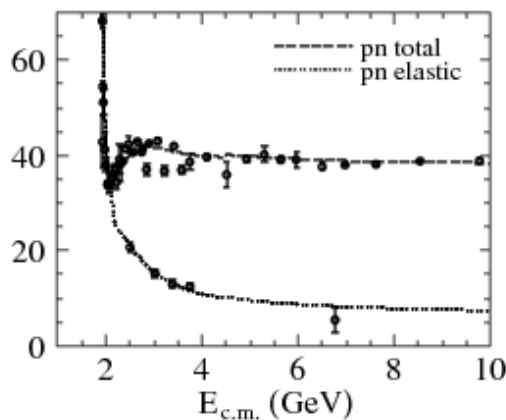
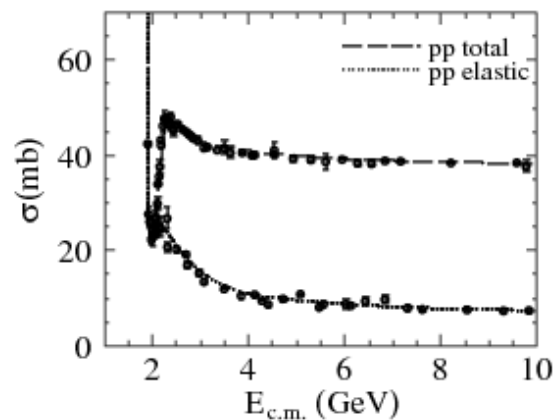
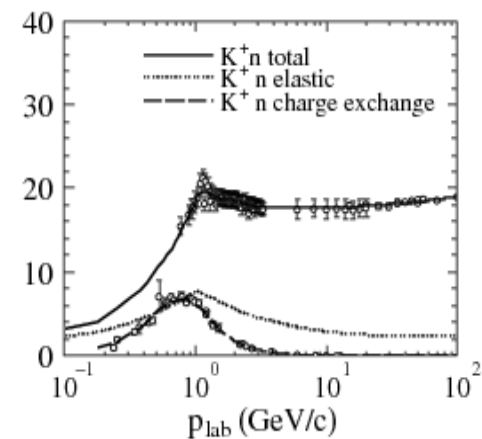
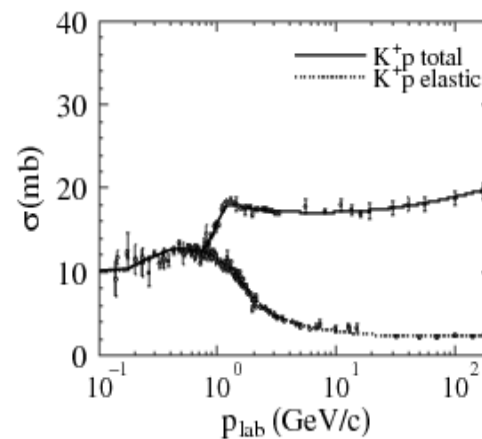
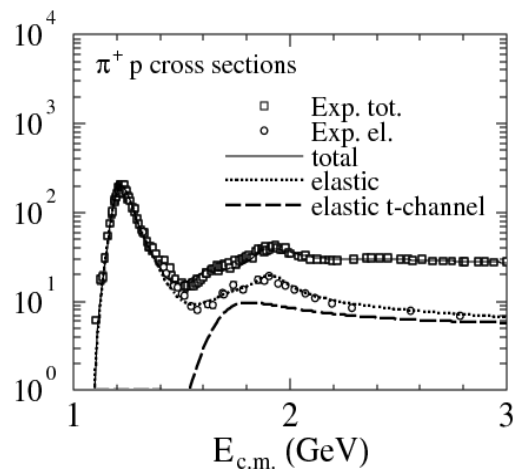
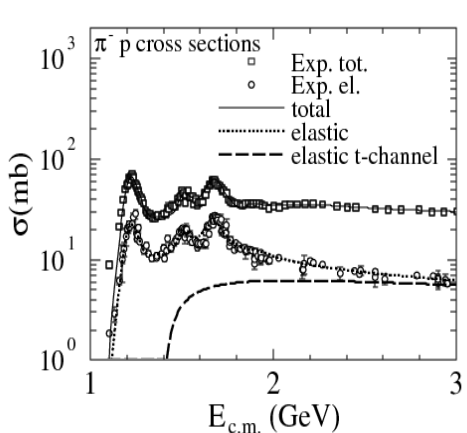


# Hadron formation point from string decay

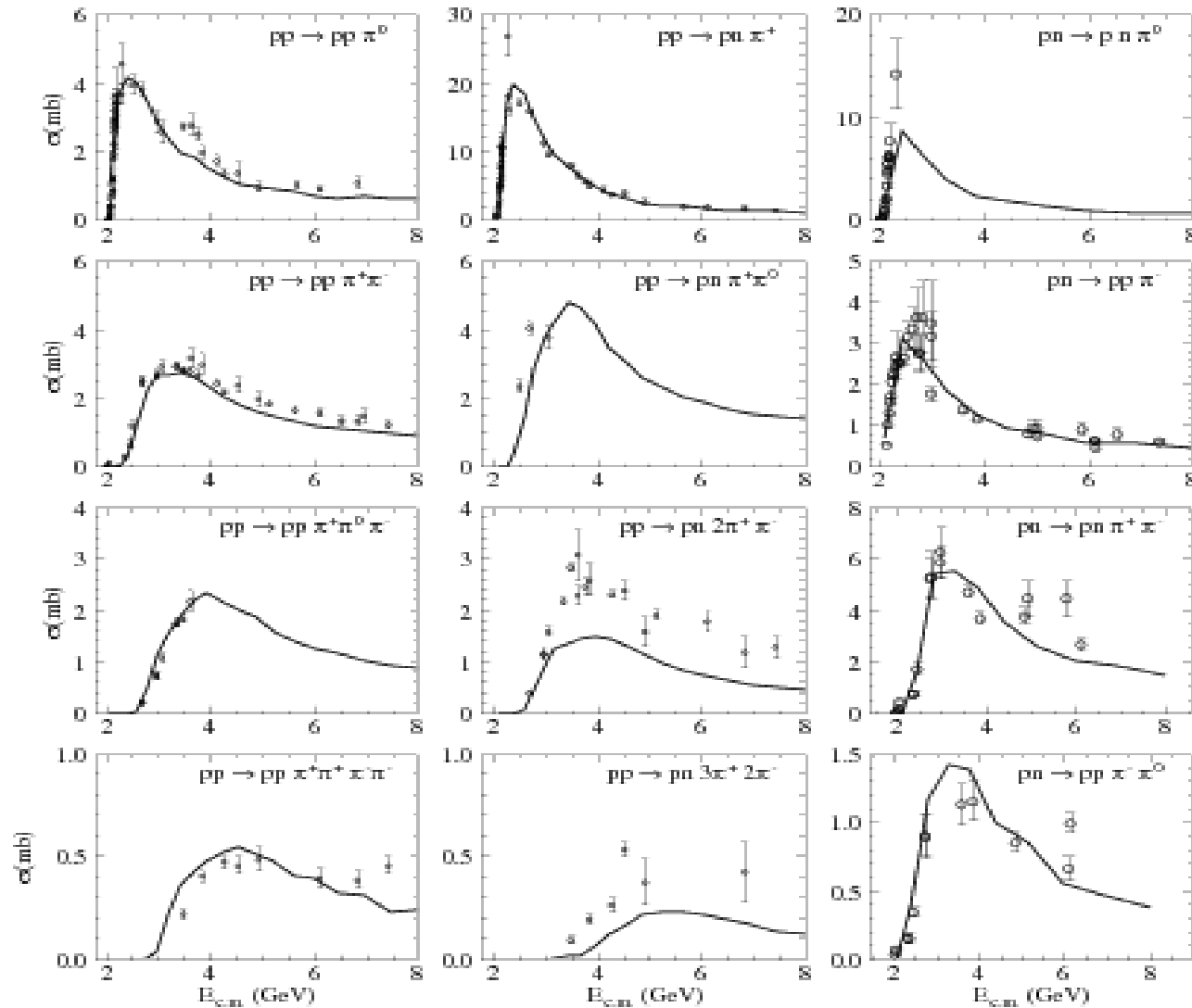


Spacetime picture  
of  $q\bar{q}$  string motion

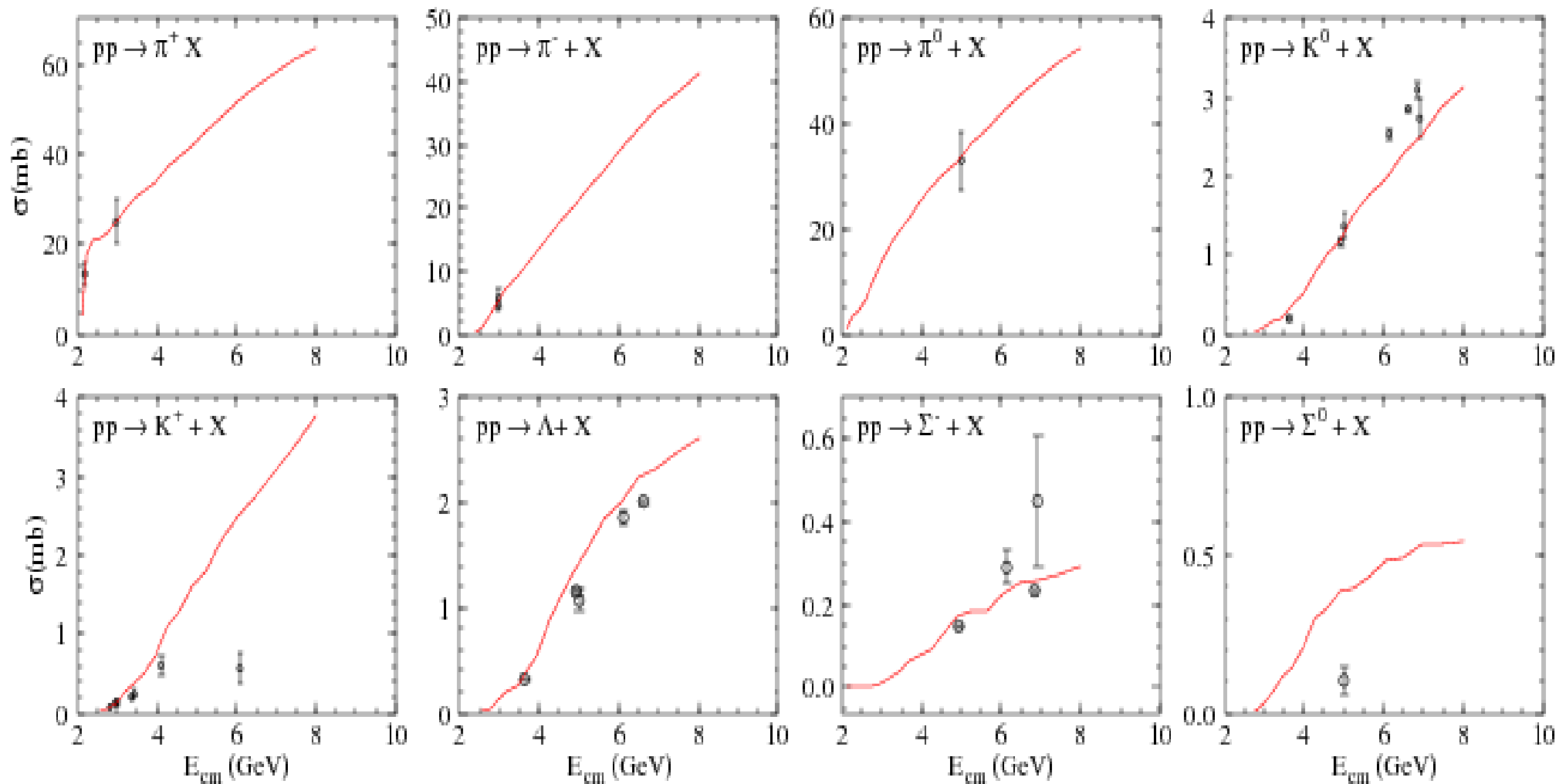
# JAM: total cross sections



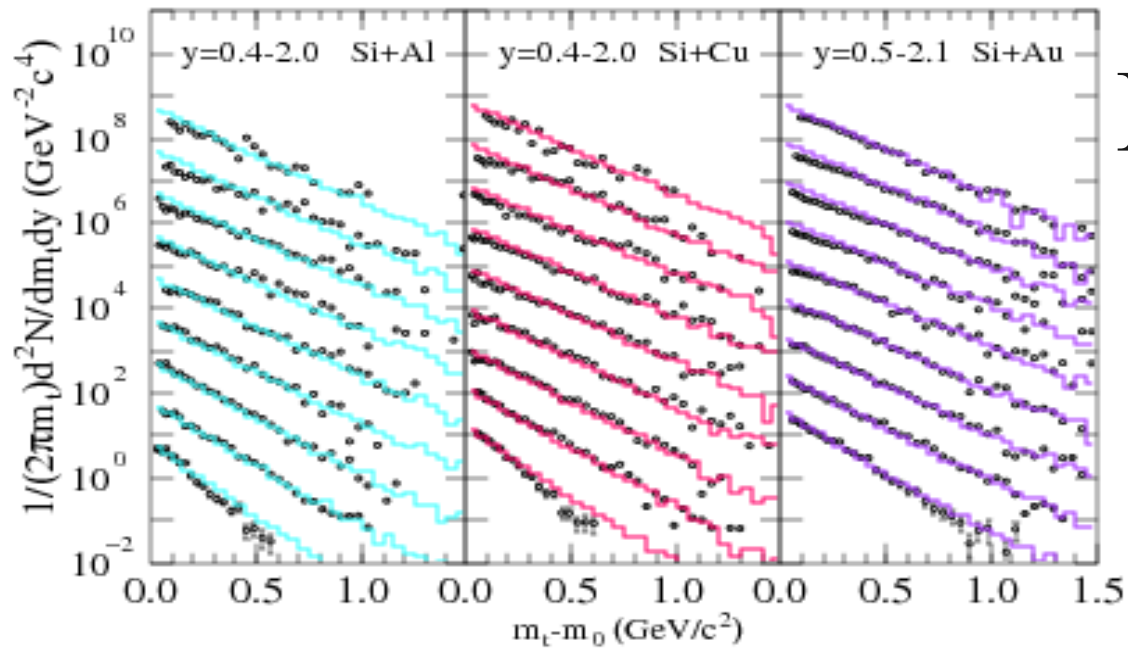
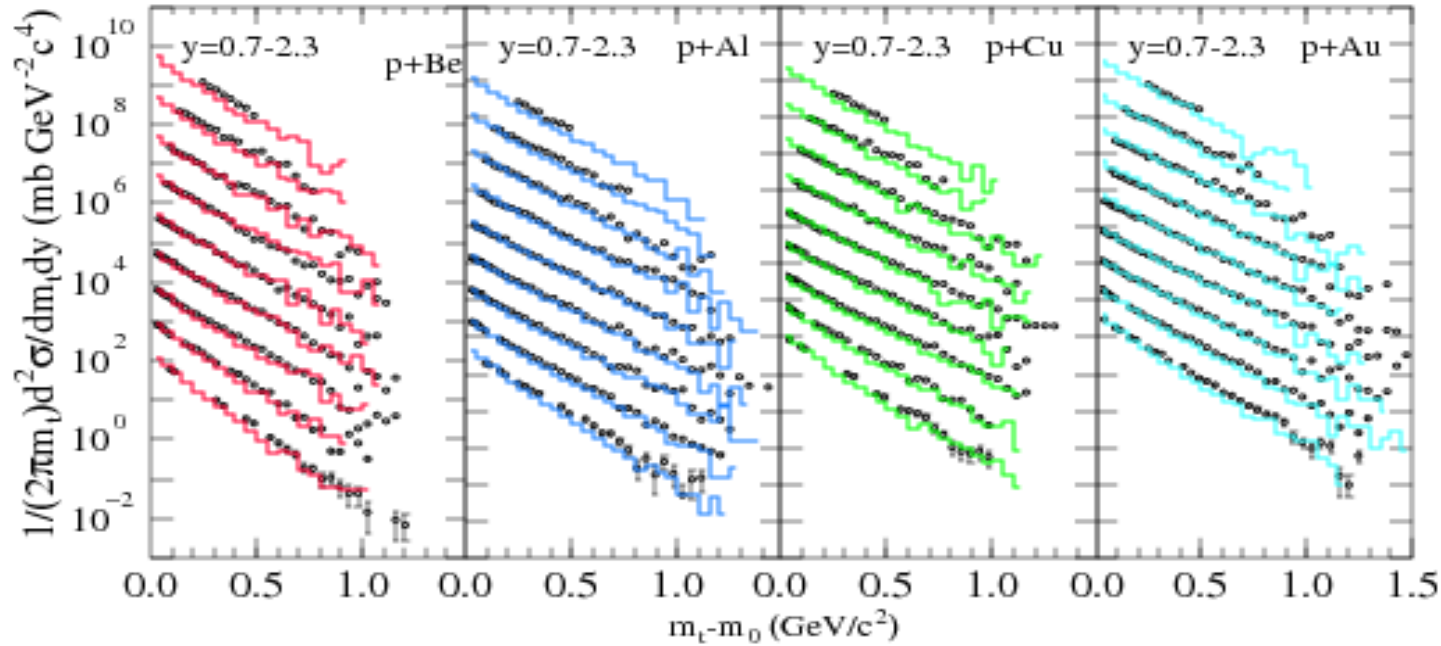
# Pion production cross sections in JAM



# Excitation function of $p+p \rightarrow X$ in JAM

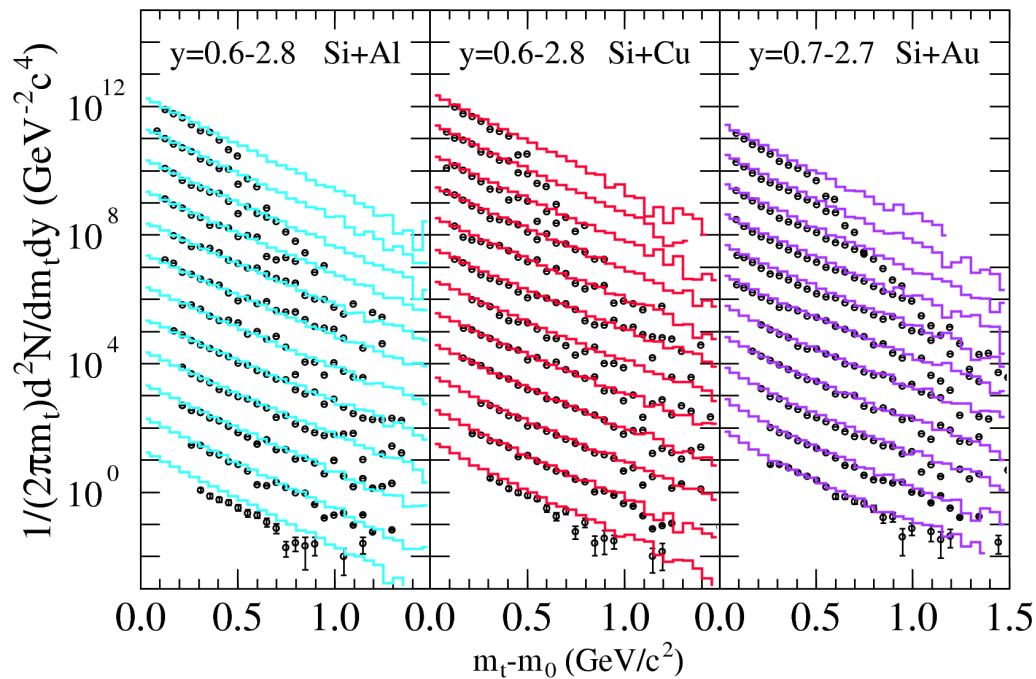
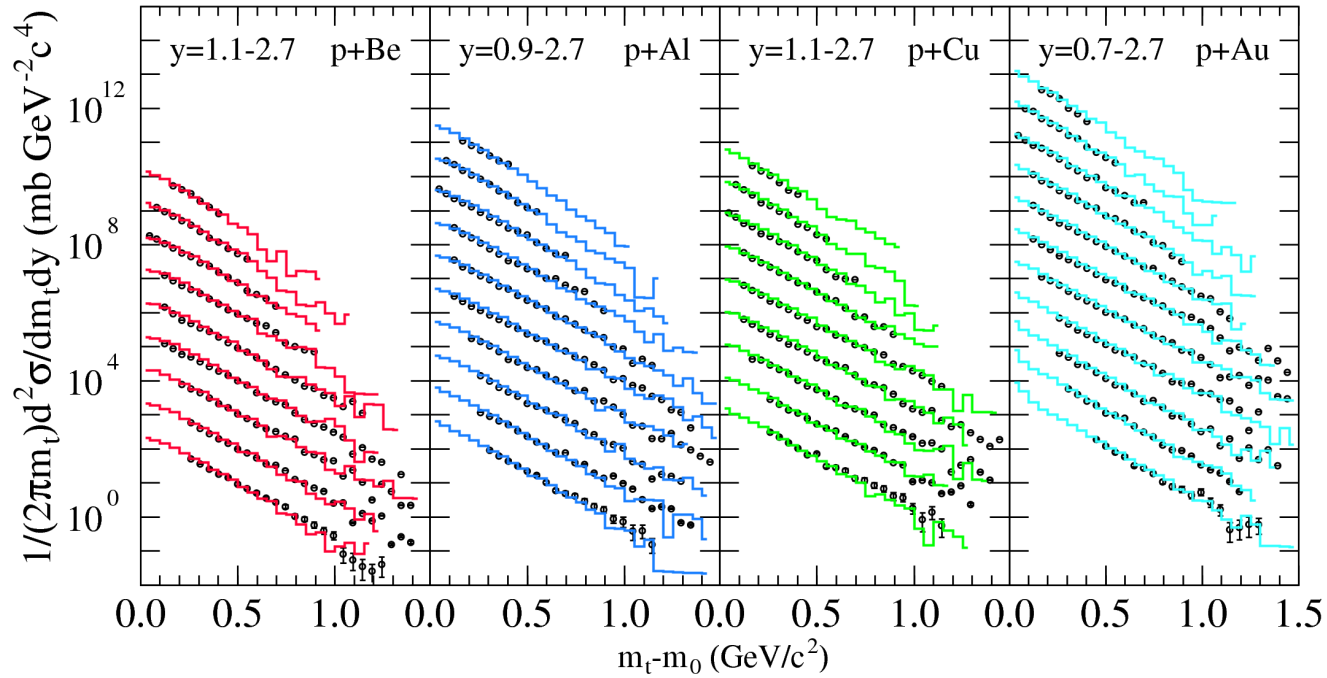


proton distributions



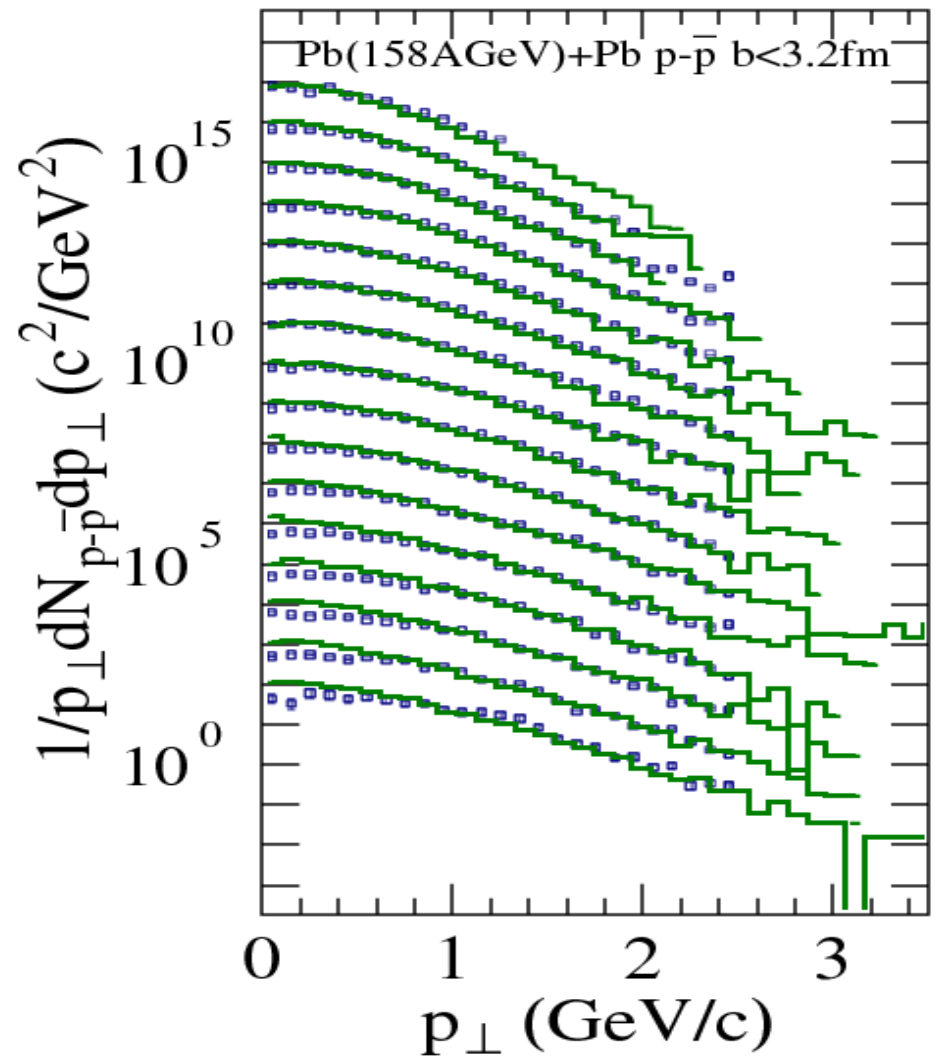
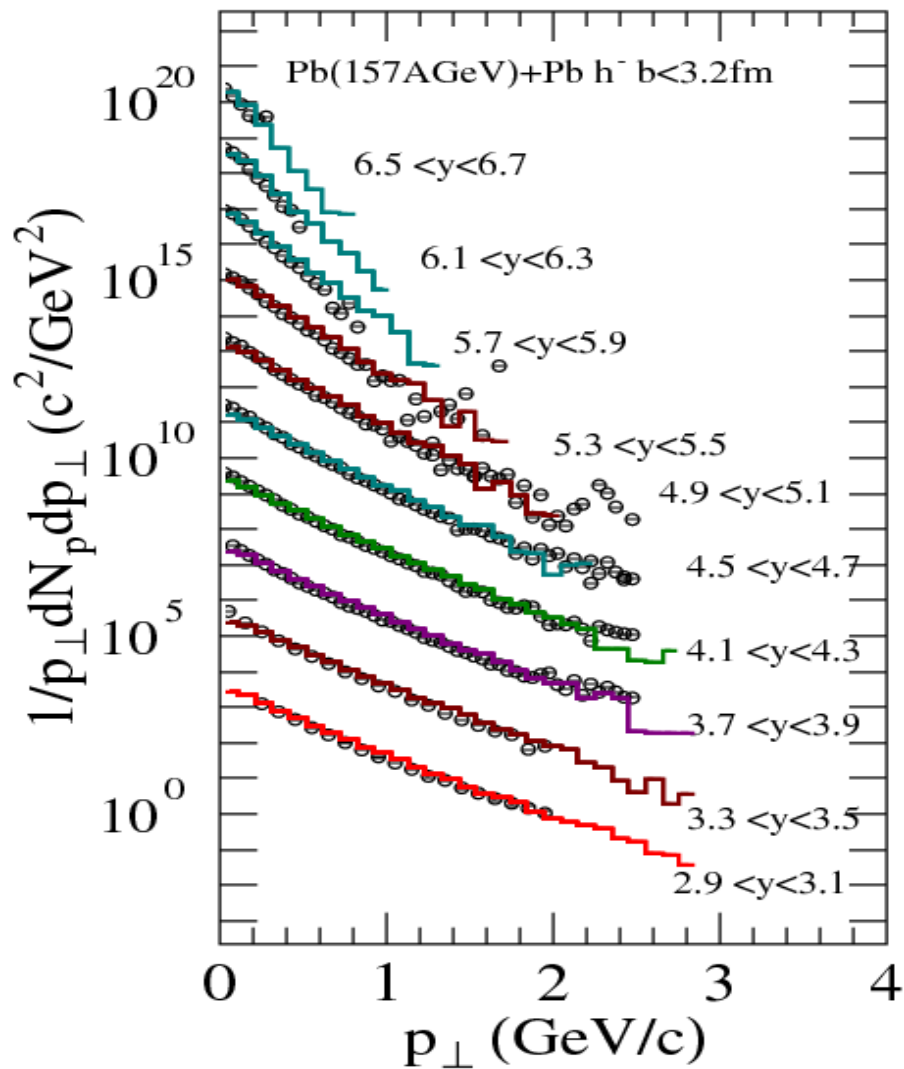
Proton distribution  
at AGS energy

### Negative pion distributions

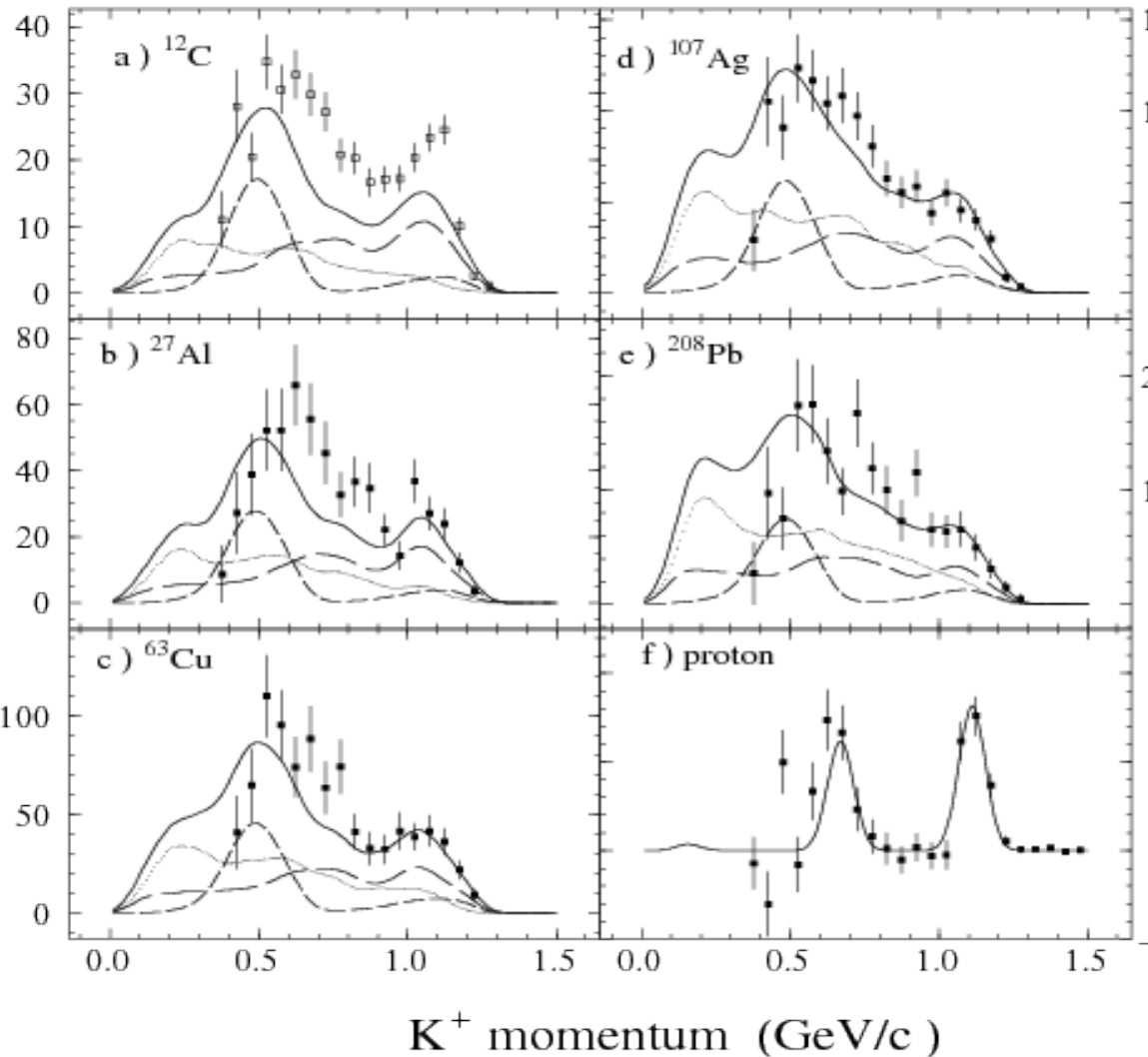


pion distribution  
at AGS energy  
(E=14GeV)

# Transverse momentum distribution at SPS energy (160A GeV)



# (K<sup>-</sup>,K<sup>+</sup>) reactions



$$\bar{K} N \rightarrow K \Xi, K \Xi^* (1530)$$

$$\bar{K} N \rightarrow (\phi, a_0, f_0) \Lambda$$

$$(\phi, a_0, f_0) \rightarrow K^+ K^-$$

$$\bar{K} N \rightarrow (\pi, \rho, \eta, \omega, \eta') (Y, Y^*)$$

$$(\pi, \rho, \eta, \omega, \eta') N \rightarrow$$

$$(K, K^*) (Y, Y^*), \phi N$$



# まとめ

- ハドロニックカスケードモデルは、重イオン衝突や、ハドロン-原子核反応の時空発展をマイクロに記述するものである。
- 現在最高エネルギーで原子核を衝突できるRHIC energy まで、粒子の multiplicity などのバルクな観測量はよく再現できるが、集団効果,例えば楕円形フローなどは再現できない。