# **T-odd effects in hadronic collisions**

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Outline

- Motivation from spin physics
- Sivers effect  $(f_{1T}^{\perp})$ 
  - Sivers effect asymmetries in hadronic collisions
  - What is (T-)odd about it
- BM effect  $(h_1^{\perp})$ 
  - Azimuthal asymmetries in unpolarized hadronic collisions
- Relation to GPDs
- Relation to twist-3 effects

# Left-right asymmetries

Large single spin asymmetries in  $p^{\uparrow} p \rightarrow \pi X$  have been observed at high  $\sqrt{s}$ E704 Collab. ('91); STAR ('02); BRAHMS ('05); ...



A left-right asymmetry

Pion distribution is asymmetric depending on transverse spin direction and on pion charge

The perturbatively generated SSA is very small (involves helicity flip)

Clearly a nonperturbative spin-orbit coupling, but how to describe such effects in a factorized, partonic approach in order to make predictions?

Single spin asymmetries in  $p^{\uparrow}p \rightarrow \pi X$ 



#### **Partonic correlators**

Theoretical description of the cross sections is based on factorization:



# **Transverse Momentum of Quarks**

For spin-orbit couplings it is natural to consider transverse momentum (TM) of the quarks inside a hadron

Natural, but more than just an extension of  $f_1^q(x) \rightarrow f_1^q(x, \mathbf{k}_T^2)$ 

 $k_T$ -odd functions may arise, that vanish upon integration over all  $k_T$ And also new spin-dependent terms may arise Ralston & Soper '79; Sivers '90; Mulders & Tangerman '95; D.B. & Mulders '98

Include partonic transverse momentum  $\Phi(x) \rightarrow \Phi(x, \mathbf{k}_T)$ : TMD factorization

TMD = transverse momentum dependent parton distribution function

Can be probed in for instance semi-inclusive DIS or Drell-Yan (DY)

#### **Sivers effect**

Proposal of a  $k_T$  and  $S_T$  dependent distribution function by Sivers ('90)



Captures nonperturbative spin-orbit coupling effects inside a polarized proton

$$\Phi(x, \boldsymbol{k}_T) = \frac{1}{2} f_1(x, \boldsymbol{k}_T^2) \mathcal{P} + \frac{\mathcal{P} \cdot (\boldsymbol{k}_T \times \boldsymbol{S}_T)}{2M} f_{1T}^{\perp}(x, \boldsymbol{k}_T^2) \mathcal{P} + \dots$$

Proposed to explain data on  $p^{\uparrow} + p \rightarrow \pi^0 + X$  at  $\sqrt{s} \approx 7$  GeV (Antille *et al.* '80)

TMD factorization of  $p + p \rightarrow \pi + X$  not established (power suppressed asymmetry), but it works phenomenologically

Anselmino et al., since '95

# Sivers effect in semi-inclusive DIS

Sivers effect leads to an unsuppressed  $\sin(\phi_h - \phi_S)$  asymmetry in  $e p^{\uparrow} \rightarrow e' h X \propto f_{1T}^{\perp} D_1$ D.B. & Mulders '98



Such an asymmetry has been clearly observed by the HERMES Collaboration TMD (or Collins-Soper) factorization established [later more]

#### Sivers effect in Drell-Yan

Sivers effect also leads to a  $\sin(\phi - \phi_S)$  asymmetry in Drell-Yan  $\propto f_{1T}^{\perp} \bar{f}_1$ Some predictions based on fit to SIDIS data:



Anselmino et al. '09

#### Sivers effect in Drell-Yan



Anselmino et al. '09

These  $p^{\uparrow}p$  DY data are kinematically largely complementary to SIDIS data

# Sivers effect in dijet production

Asymmetric jet or hadron correlations in  $p^{\uparrow} p \rightarrow h_1 h_2 X$ 

D.B. & Vogelsang '04 Bacchetta *et al.* '05

Sivers effect  $\Rightarrow \sin \delta \phi$  asymmetry  $\delta \phi = \text{dijet}$  imbalance angle



RHIC data consistent with zero at the few percent level STAR Collaboration, Abelev *et al.* '07

Theoretically this Sivers asymmetry is not as straightforward as in SIDIS or DY Potential problems with factorization

Collins & Qiu '07, Collins '07

#### **T-odd effects**



The Sivers function is a  $P \cdot (k_T \times S_T)$  correlation, which is T-odd since under time reversal transformation:  $P \rightarrow -P$  and  $S \rightarrow -S$ Sivers function is often called "naive" T-odd, as time reversal also interchanges  $i \leftrightarrow f$ 

$$e p \to e' h X \quad \stackrel{T}{\leftrightarrow} \quad e' h X \to e p$$

which cannot be compared in practice, but theoretically also difficult because: multiparticle out-states are nontrivially related to multiparticle in-states

A T-odd correlation as part of a process does not need to imply time reversal violation De Rújula, Kaplan & De Rafael '71; Hagiwara, Hikasa, Kai '83

# **T-odd effects and factorization**

But factorization allows one to go a step further:

 $T\sigma_{\text{SIDIS}} = T(H \otimes \Phi \otimes \Delta) = H \otimes T(\Phi \otimes \Delta)$ 

 ${\cal T}$  stands for the actual time reversal operation

One could select the T-invariant part of  $\Delta$  and conclude  $f_{1T}^{\perp}$  is time reversal violating Collins '93

Based on gauge variant operator definition:

 $P \cdot (\boldsymbol{k}_T \times \boldsymbol{S}_T) f_{1T}^{\perp}(x, \boldsymbol{k}_T^2) \propto \mathsf{F.T.} \langle P, S_T | \overline{\psi}(0) \gamma^+ \psi(\boldsymbol{\xi}) | P, S_T \rangle \Big|_{\boldsymbol{\xi} = (\boldsymbol{\xi}^-, 0^+, \boldsymbol{\xi}_T)}$ 

Thanks to a model calculation by Brodsky, Hwang & Schmidt '02 taking into account final state interactions (FSI), Collins realized this conclusion is invalid

One has to consider the proper gauge invariant definition of  $\Phi(x, \mathbf{k}_T)$ 

#### Link structure of TMDs

 $\Phi(x, \mathbf{k}_T)$  is a matrix element of operators that are nonlocal off the lightcone

$$\Phi(x, \boldsymbol{k}_T) = \mathsf{F}.\mathsf{T}.\left\langle P \mid \overline{\psi}(0) \,\mathcal{L}[0, \boldsymbol{\xi}] \,\psi(\xi) \mid P \right\rangle \Big|_{\boldsymbol{\xi} = (\boldsymbol{\xi}^-, 0^+, \boldsymbol{\xi}_T)}$$

$$\mathcal{L}[0,\boldsymbol{\xi}] = \mathcal{P} \exp\left(-ig \int_{\mathcal{C}[0,\boldsymbol{\xi}]} ds_{\mu} A^{\mu}(s)\right)$$

Proper gauge invariant definition of TMDs in SIDIS contains a future pointing Wilson line (FSI), whereas in Drell-Yan (DY) it is past pointing (ISI)



# **Obtaining the link structure**





#### path-ordered exponentials in off-lightcone non-local operators

D.B. & Mulders '00 Belitsky, Ji & Yuan '03

DY: ISI SIDIS: FSI

### Link structure of TMDs

Time reversal invariance relates  $\Phi^{[+]}(x, p_T)$  of SIDIS to  $\Phi^{[-]}(x, p_T)$  of Drell-Yan Collins '02



Time reversal invariance does not yield a constraint on  $\Phi^{[\pm]}$ , but a relation

 $f_{1T}^{\perp[+]} = -f_{1T}^{\perp[-]}$ 

Ignoring the link dependence yields  $f_{1T}^{\perp} = 0$  because of time reversal invariance  $f_{1T}^{\perp[\pm]}$  could be called naive T-odd (since not exchanging ISI and FSI)  $\Phi(x, \mathbf{k}_T)$  contains parts that depend on H, universality is lost for those parts But predictability is not lost!

# **Process dependence of TMDs**

There is a *calculable* process dependence, which yields the relation (Collins '02):

 $(f_{1T}^{\perp})_{\mathrm{SIDIS}} = -(f_{1T}^{\perp})_{\mathrm{DY}}$  to be tested

The color flow of a process is crucial (usually not the case in high energy scattering!) The more hadrons are observed, the more complicated the end result (ISI and FSI) Bomhof, Mulders & Pijlman '04



### **Collins-Soper factorization**

Collins-Soper factorization in DY:

 $\Phi\otimes\bar\Phi\otimes H\otimes {\color{black}U}$ 

 $\boldsymbol{U}$  is called the soft factor, a correlator of Wilson lines

Collins & Soper '81; Ji, Ma & Yuan '04 & '05

At tree level  $(U(l_T^2) \propto \delta(l_T^2))$  this corresponds to the often used description:



#### Extension to $p p \rightarrow h h' X$ not clear

#### **Transverse quark polarization**

Besides  $f_{1T}^{\perp}$  there is another (naive) T-odd distribution function:

$$\Phi(x, \boldsymbol{k}_T) = \frac{1}{2} f_1(x, \boldsymbol{k}_T^2) \mathcal{P} + \frac{\boldsymbol{P} \cdot (\boldsymbol{k}_T \times \boldsymbol{S}_T)}{2M} f_{1T}^{\perp}(x, \boldsymbol{k}_T^2) \mathcal{P} + i\boldsymbol{h}_1^{\perp}(x, \boldsymbol{k}_T^2) \frac{\mathcal{P} \, \boldsymbol{k}_T}{M} + \dots$$



D.B. & Mulders '98

Transversely polarized quarks inside an *unpolarized* hadron Allowed by the symmetries as long as  $k_T \neq 0$ 

It generates azimuthal asymmetries in unpolarized collisions, e.g. in DY

There is very interesting data from the 1980s on  $\pi^- N \rightarrow \mu^+ \mu^- X$ It shows an anomalously large  $\cos 2\phi$  asymmetry (w.r.t. pQCD predictions)

# Azimuthal asymmetries in Drell-Yan in theory



#### Collinear factorization:

Mirkes & Ohnemus '95

Parton Model $\mathcal{O}(\alpha_s^0)$  $\lambda = 1, \ \mu = \nu = 0$ LO pQCD $\mathcal{O}(\alpha_s^1)$  $1 - \lambda - 2\nu = 0$ Lam-Tung relationNLO $\mathcal{O}(\alpha_s^2)$  $1 - \lambda - 2\nu \neq 0$ small and positive

#### Azimuthal asymmetries in Drell-Yan in experiment



Data:  $1 - \lambda - 2\nu \neq 0$  large and negative! NA10 Collab. ('86/'88) & E615 Collab. ('89)

Data for  $\pi^- N \to \mu^+ \mu^- X$ , with N = D, W $\sqrt{s} \approx 20 \pm 3 \text{ GeV}$ lepton pair invariant mass  $Q \sim 4 - 12 \text{ GeV}$ 

Nonzero  $h_1^{\perp}$  offers an explanation of this anomalous Drell-Yan data D.B. '99

# **Explanation in terms of** $h_1^{\perp}$

 $(1 - \lambda - 2\nu) \propto h_1^{\perp}(\pi) h_1^{\perp}(N)$   $(1 - \lambda - 2\nu) \propto h$ 



Many model calculations of  $h_1^{\perp}$  and its asymmetries have been performed Goldstein & Gamberg '02, '07; D.B., Brodsky & Hwang '03 Lu & Ma '04, '05; Barone, Lu & Ma '07; Zhang, Lu, Ma & Schmidt '08 Courtoy, Scopetta & Vento '09; Lu & Schmidt '09

#### Allows to predict other observables, such as DY for $pp, \bar{p}p, p^{\uparrow}p, p^{\uparrow}\pi$ , etc

# New unpolarized DY data

Asymmetry for p p and p d expected to be smaller, as confirmed by recent Fermilab data FNAL-E866/NuSea Collaboration, L.Y. Zhu *et al.* '07 & '09  $\rightarrow$  [next talk]

Asymmetry for  $\bar{p} p$  expected to be very similar to  $\pi p$  (both have valence antiquarks)

Although this depends on the kinematics too of course:



# $h_1^\perp$ in dijet production

 $h_1^{\perp}$  of quarks and gluons contributes to the dijet imbalance  $\delta \phi$  distribution Lu & Schmidt '08; D.B., Mulders & Pisano '09

 $h_1^{\perp g}$ : linearly polarized gluons inside an unpolarized hadron (T-, chiral- &  $k_T$ -even) In the plane transverse to the collision axis:  $\delta \phi = \phi_{j_1} - \phi_{j_2} - \pi$ In unpolarized scattering its distribution is often used to extract  $\langle k_T^2 \rangle$  of partons Sizeable  $h_1^{\perp}$  contributions can modify the  $\delta \phi$  distribution (especially in  $p \ \bar{p} \rightarrow$  jet jet X)



#### **Possible relation between TMDs and GPDs**

If the Sivers effect describes spin-orbit coupling, one may expect a relation with OAM and hence with GPDs

A relation between  $f_{1T}^{\perp}$  and the GPD E has been put forward Burkardt '04; Burkardt & Hwang '04

$$f_{1T}^{\perp(1)}(x) \equiv \int d^2 \mathbf{k}_T \frac{\mathbf{k}_T^2}{2M^2} f_{1T}^{\perp}(x, \mathbf{k}_T^2) \propto S_T \times b_{\perp} \int db_{\perp}^2 \mathbf{I}(b_{\perp}^2) \frac{\partial}{\partial b_{\perp}^2} E(x, b_{\perp}^2)$$

Note:  $k_T$  and  $b_{\perp}$  are not each other's Fourier conjugates

The factor  $I(b_{\perp}^2)$  is called the lensing function

Allows to link the Sivers function to the anomalous magnetic moment of  $\boldsymbol{u}, \boldsymbol{d}$ 

A similar relation between  $h_1^{\perp}$  and the chiral-odd GPD combination  $\bar{E}_T \equiv E_T + 2\tilde{H}_T$ 

### Lattice results



#### $S_T \times b_\perp$ correlations exist!

QCDSF & UKQCD Collaboration, Göckeler *et al.* '07

 $h_1^{\perp \, u}$  same sign as  $h_1^{\perp \, d}$ Burkardt & Hannafious '07

# The lensing function

The lensing function has recently been calculated in an eikonal approach



Gamberg & Schlegel '09

### Other explanations of the asymmetries

Qiu-Sterman effect proposed as a mechanism for single spin asymmetries in  $p^{\uparrow} p \rightarrow \pi X$ Qiu & Sterman '91

It is a collinear twist-3 function relevant for the high- $p_T$  description

$$T(x, S_T) \stackrel{A^+=0}{\propto} \mathsf{F.T.} \langle P | \ \overline{\psi}(0) \ \int d\eta^- \ F^{+\alpha}(\eta^-) \ \gamma^+ \ \psi(\xi^-) \ | P \rangle$$

Applicable when collinear factorization is justified

The Sivers effect in Drell-Yan deals with a multi-scale process: M,  $Q_T$  and Q

TMD or Collins-Soper factorization applies when  $Q_T^2 \ll Q^2$ Collins & Soper '81; Ji, Ma & Yuan '04 & '05

Collinear factorization applies when  $Q_T^2 \sim Q^2$ 

#### These two descriptions can actually be connected! Ji, Qiu, Vogelsang, Yuan '06

#### Large transverse momentum tails

Consider the large transverse momentum tails of TMDs:

$$f_1(x, \boldsymbol{p}_T^2) \stackrel{\boldsymbol{p}_T^2 \gg M^2}{\sim} \alpha_s \frac{1}{\boldsymbol{p}_T^2} \left( K \otimes f_1 \right) (x)$$
  
$$f_{1T}^{\perp}(x, \boldsymbol{p}_T^2) \stackrel{\boldsymbol{p}_T^2 \gg M^2}{\sim} \alpha_s \frac{M^2}{\boldsymbol{p}_T^4} \left( K' \otimes f_{1T}^{\perp(1)} \right) (x)$$

$$f_{1T}^{\perp(1)}(x) \equiv \int d^2 \mathbf{k}_T \frac{\mathbf{k}_T^2}{2M^2} f_{1T}^{\perp}(x, \mathbf{k}_T^2) \propto T(x, S_T)$$

The first transverse moment of the Sivers function is the Qiu-Sterman function D.B., Mulders & Pijlman '03

The Qiu-Sterman effect determines the large  $p_T$  behavior of the Sivers effect This yields precisely the high  $Q_T$  result! Ji, Qiu, Vogelsang, Yuan '06

Thanks to this one can consider the integral of the Sivers asymmetry over all  $Q_T$ 

### $\cos 2\phi$ asymmetry as function of $Q_T$

The high- $p_T$  tail of  $h_1^{\perp}$  is related to a chiral-odd QS effect (power suppressed)

But the  $\cos(2\phi)$  asymmetry at high  $Q_T$  is dominated by the perturbative contribution



$$\nu = \nu_{h_1^{\perp}} + \nu_{\text{pert}} + \mathcal{O}(\frac{Q_T^2}{Q^2}, \frac{M^2}{Q_T^2})$$

Bacchetta, D.B., Diehl, Mulders '08

This time the integral over all  $Q_T$  picks up both contributions The  $Q_T^2$ -weighted asymmetry is mostly sensitive to the high  $Q_T$  perturbative result The  $Q_T^2$ -weighted asymmetry at tree level and at order  $\alpha_s$  are very different expressions Very different from Sivers effect asymmetries

# $\cos 2\phi$ asymmetry from $h_1^{\perp}$ beyond tree level

Collins-Soper factorization dictates the  $Q^2$  dependence of azimuthal asymmetries Assuming Gaussian  $k_T$  dependence for  $h_1^{\perp}$ , its contribution to  $\nu$  is proportional to



Considerable Sudakov suppression with increasing  $Q: \sim 1/Q$  (effectively twist-3) On the other hand, the perturbative contribution falls off as  $1/Q^2$ 

# Conclusions

- Sivers & BM effects are naive T-odd effects: their correlations are T-odd, but distributions multiplying them are process dependent
- These naive T-odd effects give rise to many different azimuthal asymmetries Several such asymmetries are visible in the available data
- Calculable process dependence, so universality is lost, but predictability is not Tests of this are expected soon
- Lattice results on asymmetric GPDs suggest these TMD effects are nonzero
- $Q_T$  and Q dependence of TMD asymmetries dictated by factorization
- Factorization for DY under control, for dijet and dihadron production not (yet?)
- All in all, a lot of theoretical & experimental progress in recent years!

# Back-up Slides

KEK theory center workshop on High-energy hadron physics with hadron beams, January 6, 2010



# **T-odd effects and factorization**

But factorization allows one to go a step further:

 $T\sigma_{\rm DIS} = T(H \otimes \Phi) = H \otimes T\Phi$ 

Here T stands for the actual time reversal operation

Time reversal invariance leads to the constraint

$$(-i\gamma_5 C)\Phi(x,\bar{P},\bar{S})(-i\gamma_5 C) = \Phi(x,P,S)^*$$

where  $\bar{P}=(P^0,-\boldsymbol{P})$ , etc

T-odd correlations in the parametrization of  $\Phi(x)$  are really time reversal violating

So what about processes involving TMDs?

$$T\sigma_{\text{SIDIS}} = T(H \otimes \Phi \otimes \Delta) = H \otimes T(\Phi \otimes \Delta)$$

Here one could select the T-even part of  $\Delta$  and conclude  $f_{1T}^{\perp}$  is time reversal violating Collins '93

#### **Collins-Soper factorization**

$$W_{\mathsf{DY}}^{\mu\nu} \propto |H(x_1, x_2, Q^2)|^2 \sum_a e_a^2 \int d^2 p_T \, d^2 k_T \, d^2 l_T \, \delta^{(2)}(p_T + k_T - l_T - q_T) \\ \times \operatorname{Tr} \left\{ \Phi^a(x_1, p_T) \gamma^{\mu} \bar{\Phi}^a(x_2, k_T) \gamma^{\nu} \right\} \, U(l_T^2) \, + \, \mathcal{O}(Q_T^2/Q^2)$$

Collins & Soper '81; Ji, Ma & Yuan '05

At tree level  $(U(l_T^2) \propto \delta(l_T^2))$  this corresponds to the often used description:



#### Extension to $p p \rightarrow h h' X$ not clear

 $h_1^\perp$  in  $p \ \bar{p} \to \gamma$  jet X

$$\frac{d\sigma^{h_1 h_2 \to \gamma \text{ jet } X}}{d\eta_\gamma \, d\eta_j \, d^2 \boldsymbol{K}_{\gamma \perp} \, d^2 \boldsymbol{q}_\perp} \quad \propto \quad (1 + \nu_{\mathsf{DY}} \, \boldsymbol{R} \cos 2(\phi_\perp - \phi_\gamma))$$

 $\nu_{\text{DY}}$  probed at the scale  $|\mathbf{K}_{\gamma\perp}| \ (\neq Q)$ Proportionality factor R only function of  $f_1$ 

$$y \equiv -\frac{\hat{t}}{\hat{s}} = \frac{1}{e^{\eta_{\gamma} - \eta_{j}} + 1}$$

For typical Tevatron kinematics in the central region (DØ, arXiv:0804.1107)  $\nu_{\rm DY} R \sim 5 - 15\%$  expected D.B., Mulders & Pisano '08



# Single spin asymmetries in $p^{\uparrow}p \to \pi X$

SSA in  $p p^{\uparrow} \rightarrow \pi X$  [E704, AGS, STAR, BRAHMS]



Description in terms of Sivers (and Collins) effect studied extensively Anselmino, Boglione, D'Alesio, Murgia, and collaborators, since 1995

Twist-3 (factorization not proven) remains to be connected to Qiu-Sterman effect

### The polarized Drell-Yan process

In the case of one transversely polarized hadron beam:

$$\frac{d\sigma}{d\Omega \ d\phi_S} \propto 1 + \cos^2\theta + \sin^2\theta \left[\frac{\nu}{2} \ \cos 2\phi - \rho \ |\boldsymbol{S}_T| \ \sin(\phi + \phi_S)\right] + \dots$$

Assuming *u*-quark dominance and Gaussian  $k_T$ -dependence for  $h_1^{\perp}$ :



First extraction of  $h_1$  from HERMES, COMPASS, BELLE data indicates  $h_1 \approx f_1/3$ Anselmino *et al.* '07

# **DY** at **Compass**

Measurement of  $\nu$  and  $\rho$  with only one polarized beam offers a probe of *transversity* The distribution of transversely polarized quarks inside a transversely polarized hadron

The COMPASS experiment plans to extract them using  $\pi^{\pm} p^{\uparrow}$  Drell-Yan Would provide valuable information on the flavor dependence of  $h_1$  and  $h_1^{\perp}$ 

Especially  $\pi^+ p^{\uparrow}$  is of interest, since no data yet and it provides information on the *d*-quark ratio  $h_1^{\perp d/p}/h_1^{d/p}$ , without suppression by a charge-squared factor

Using the input on  $h_1^{\perp}$  from for example unpolarized  $p \bar{p}$  Drell-Yan would allow for an extraction of  $h_1$  from  $\pi^{\pm} p^{\uparrow}$  Drell-Yan at COMPASS

### **Future DY data**

Usually Drell-Yan data is taken in the safe region, cutting out the resonances  $(J/\psi \text{ and } \Upsilon)$ 

They are however also vector particles Anselmino, Barone, Drago & Nikolaev '04

Note that the NA10 data ('86) on the  $\Upsilon$  is very similar to that above/below it

