

New Applications of Resummation in Non-abelian Gauge Theories: QED \otimes QCD Exponentiation for LHC Physics and Resummed Quantum Gravity

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Outline:

- **Introduction**
- **Review of YFS Theory and Its Extension to QCD**
- **Extension to QED \otimes QCD and Quantum Gravity**
- **QED \otimes QCD Threshold Corrections, Shower/ME Matching and IR-Improved DGLAP Theory at the LHC**
- **Final State of Hawking Radiation**
- **Conclusions**

Papers by B.F.L.W., S. Jadach and B.F.L. Ward, S. Jadach, *et al.*, B.F.L.W. and S. Yost, *M. Phys. Lett. A* **14** (1999) 491, hep-ph/0205062; *ibid.* **12** (1997) 2425; *ibid.* **19** (2004) 2113; hep-ph/0503189,0508140,0509003

Motivation

- FNAL/RHIC $t\bar{t}$ PRODUCTION; POLARIZED pp PROCESSES; $b\bar{b}$ PRODUCTION; J/Ψ PRODUCTION: SOFT $n(G)$ EFFECTS ALREADY NEEDED
 $\Delta m_t = 5.1$ GeV with SOFT $n(G)$ UNCERTAINTY $\sim 2-3$ GeV, ..., ETC.
- FOR THE LHC/TESLA/LC, THE REQUIREMENTS WILL BE EVEN MORE DEMANDING AND OUR QCD SOFT $n(G)$ MC EXPONENTIATION RESULTS WILL BE AN IMPORTANT PART OF THE NECESSARY THEORY – YFS EXPONENTIATED $\mathcal{O}(\alpha_s^2)L$, IN THE PRESENCE OF SHOWERS, ON AN EVENT-BY-EVENT BASIS, WITHOUT DOUBLE COUNTING AND WITH EXACT PHASE SPACE.
- HOW RELEVANT ARE QED HIGHER ORDER CORRECTIONS WHEN QCD IS CONTROLLED AT $\sim 1\%$ PRECISION?
- CROSS CHECK OF QCD LITERATURE:
 1. PHASE SPACE – CATANI, CATANI-SEYMOUR, ALL INITIAL PARTONS MASSLESS
 2. RESUMMATION – STERMAN, CATANI ET AL., BERGER ET AL.,
 3. NO-GO THEOREMS
 4. IR QCD EFFECTS IN DGLAP THEORY

- CROSS CHECK OF QED LITERATURE:
 1. ESTIMATES BY SPIESBERGER, STIRLING, ROTH and WEINZIERL – FEW PER MILLE EFFECTS FROM QED CORRECTIONS TO STR. FN. EVOLUTION.
 2. WELL-KNOWN POSSIBLE ENHANCEMENT OF QED CORRECTIONS AT THRESHOLD, ESPECIALLY IN RESONANCE PRODUCTION
⇒ HOW BIG ARE THESE EFFECTS AT THE LHC?
- TREAT QED AND QCD SIMULTANEOUSLY IN THE YFS EXPONENTIATION TO ESTIMATE THE ROLE OF THE QED AND TO ILLUSTRATE AN APPROACH TO SHOWER/ME MATCHING.
- QUANTUM GENERAL RELATIVITY: STILL NO PHENOMENOLOGICALLY TESTED THEORY
- OUTSTANDING ISSUES: FINAL STATE OF HAWKING RADIATION, ... – FERTILE GROUND FOR RESUMMATION; SEE ALSO WORK BY REUTER ET AL., LITIM, DONOGHUE ET AL., CAVAGLIA, SOLA ET AL., ETC.

PRELIMINARIES

- WE USE THE GPS CONVENTIONS OF JWW FOR SPINORS; PHOTON-GLUON POLARIZATION VECTORS FOLLOW THEREFROM:

$$(\epsilon_{\sigma}^{\mu}(\beta))^* = \frac{\bar{u}_{\sigma}(k)\gamma^{\mu}u_{\sigma}(\beta)}{\sqrt{2}\bar{u}_{-\sigma}(k)u_{\sigma}(\beta)}, \quad (\epsilon_{\sigma}^{\mu}(\zeta))^* = \frac{\bar{u}_{\sigma}(k)\gamma^{\mu}u_{\sigma}(\zeta)}{\sqrt{2}\bar{u}_{-\sigma}(k)u_{\sigma}(\zeta)}, \quad (1)$$

- REPRESENTATIVE PROCESSES

$$pp \rightarrow V + n(\gamma) + m(g) + X \rightarrow \bar{\ell}\ell' + n'(\gamma) + m(g) + X,$$

where $V = W^{\pm}, Z$, and $\ell = e, \mu, \ell' = \nu_e, \nu_{\mu}(e, \mu)$

respectively for $V = W^{+}(Z)$, and $\ell = \nu_e, \nu_{\mu}, \ell' = e, \mu$

respectively for $V = W^{-}$.

Quantum Gravity Loop Corrections to Elementary Particle
Proppagators

Review of YFS Theory and Its Extension to QCD

QED CASE – S. Jadach et al., YFS2, YFS3, BHLUMI, BHWIDE, KORALZ, KKMC, YFSWW3, YFSZZ, KoralW

For $e^+(p_1)e^-(q_1) \rightarrow \bar{f}(p_2)f(q_2) + n(\gamma)(k_1, \dots, k_n)$, renormalization group improved YFS theory (PRD36(1987)939) gives

$$d\sigma_{exp} = e^{2\alpha \operatorname{Re} B + 2\alpha \tilde{B}} \sum_{n=0}^{\infty} \frac{1}{n!} \int \prod_{j=1}^n \frac{d^3 k_j}{k_j^0} \int \frac{d^4 y}{(2\pi)^4} e^{iy(p_1 + q_1 - p_2 - q_2 - \sum_j k_j) + D} \bar{\beta}_n(k_1, \dots, k_n) \frac{d^3 p_2 d^3 q_2}{p_2^0 q_2^0}$$

where the YFS real infrared function \tilde{B} and the virtual infrared function B are known and where we note the usual connections

$$2\alpha \tilde{B} = \int^{k \leq K_{max}} \frac{d^3 k}{k_0} \tilde{S}(k)$$

$$D = \int d^3 k \frac{\tilde{S}(k)}{k^0} (e^{-iy \cdot k} - \theta(K_{max} - k)) \quad (2)$$

for the standard YFS infrared emission factor

$$\tilde{S}(k) = \frac{\alpha}{4\pi^2} \left[Q_f Q_{(\bar{f})'} \left(\frac{p_1}{p_1 \cdot k} - \frac{q_1}{q_1 \cdot k} \right)^2 + (\dots) \right] \quad (3)$$

if Q_f is the electric charge of f in units of the positron charge. For example, the YFS hard photon residuals $\bar{\beta}_i$ in (1), $i = 0, 1, 2$, are given in **S. Jadach *et al.*, CPC102(1997)229** for BHLUMI 4.04 \Rightarrow YFS exponentiated exact $\mathcal{O}(\alpha)$ and LL $\mathcal{O}(\alpha^2)$ cross section for Bhabha scattering via a corresponding Monte Carlo realization of (1).

In hep-ph/0210357(ICHEP02), Acta Phys.Polon.B33,1543-1558,2002, we have extended the YFS theory to QCD:

$$\begin{aligned}
 d\hat{\sigma}_{\text{exp}} &= \sum_n d\hat{\sigma}^n \\
 &= e^{\text{SUM}_{\text{IR}}(\text{QCD})} \sum_{n=0}^{\infty} \int \prod_{j=1}^n \frac{d^3 k_j}{k_j} \int \frac{d^4 y}{(2\pi)^4} e^{iy \cdot (P_1 + P_2 - Q_1 - Q_2 - \sum k_j) + D_{\text{QCD}}} \\
 &\quad * \tilde{\beta}_n(k_1, \dots, k_n) \frac{d^3 P_2}{P_2^0} \frac{d^3 Q_2}{Q_2^0}
 \end{aligned} \tag{4}$$

where now the hard gluon residuals $\tilde{\beta}_n(k_1, \dots, k_n)$ defined by

$$\tilde{\beta}_n(k_1, \dots, k_n) = \sum_{\ell=0}^{\infty} \tilde{\beta}_n^{(\ell)}(k_1, \dots, k_n)$$

are free of all infrared divergences to all orders in $\alpha_s(Q)$.

- We stress that the arguments in the earlier papers (DeLaney *et al.* PRD52(1995)108, PLB342(1995)239) are not really sufficient to derive the respective analog of eq.(4); for, they did not really expose the compensation between the left over genuine non-Abelian IR virtual and real singularities between $\int dPh_{\bar{\beta}_n}$ and $\int dPh_{\bar{\beta}_{n+1}}$ respectively that really allows us to isolate $\bar{\beta}_j$ and distinguishes QCD from QED, where no such compensation occurs.
- Our exponential factor corresponds to the $N = 1$ term in the exponent in Gatheral's formula (Phys. Lett.B133(1983)90) for the general exponentiation of the eikonal cross sections for non-Abelian gauge theory; his result is an approximate one in which everything that does not eikonalize and exponentiate is dropped whereas our result (4) is exact.

Extension to QED \otimes QCD and Quantum Gravity

Simultaneous exponentiation of QED and QCD higher order effects,
 hep-ph/0404087,
 gives

$$\begin{aligned}
 B_{QCD}^{nls} &\rightarrow B_{QCD}^{nls} + B_{QED}^{nls} \equiv B_{QCED}^{nls}, \\
 \tilde{B}_{QCD}^{nls} &\rightarrow \tilde{B}_{QCD}^{nls} + \tilde{B}_{QED}^{nls} \equiv \tilde{B}_{QCED}^{nls}, \\
 \tilde{S}_{QCD}^{nls} &\rightarrow \tilde{S}_{QCD}^{nls} + \tilde{S}_{QED}^{nls} \equiv \tilde{S}_{QCED}^{nls}
 \end{aligned}
 \tag{5}$$

which leads to

$$\begin{aligned}
 d\hat{\sigma}_{\text{exp}} &= e^{\text{SUM}_{\text{IR}}(\text{QCED})} \sum_{n,m=0}^{\infty} \int \prod_{j_1=1}^n \frac{d^3 k_{j_1}}{k_{j_1}} \\
 &\prod_{j_2=1}^m \frac{d^3 k'_{j_2}}{k'_{j_2}} \int \frac{d^4 y}{(2\pi)^4} e^{iy \cdot (p_1 + q_1 - p_2 - q_2 - \sum k_{j_1} - \sum k'_{j_2}) + D_{\text{QCED}}} \\
 &\tilde{\beta}_{n,m}(k_1, \dots, k_n; k'_1, \dots, k'_m) \frac{d^3 p_2}{p_2^0} \frac{d^3 q_2}{q_2^0},
 \end{aligned}
 \tag{6}$$

where the new YFS residuals

$\tilde{\beta}_{n,m}(k_1, \dots, k_n; k'_1, \dots, k'_m)$, with n hard gluons and m hard photons,

represent the successive application of the YFS expansion first for QCD and subsequently for QED.

The infrared functions are now

$$\begin{aligned} \text{SUM}_{\text{IR}}(\text{QCED}) &= 2\alpha_s \Re B_{\text{QCED}}^{nls} + 2\alpha_s \tilde{B}_{\text{QCED}}^{nls} \\ D_{\text{QCED}} &= \int \frac{dk}{k^0} \left(e^{-iky} - \theta(K_{max} - k^0) \right) \tilde{S}_{\text{QCED}}^{nls} \end{aligned} \quad (7)$$

where K_{max} is a dummy parameter – here the same for QCD and QED.

Infrared Algebra(QCED):

$$x_{avg}(\text{QED}) \cong \gamma(\text{QED}) / (1 + \gamma(\text{QED}))$$

$$x_{avg}(\text{QCD}) \cong \gamma(\text{QCD}) / (1 + \gamma(\text{QCD}))$$

$$\gamma(A) = \frac{2\alpha_A C_A}{\pi} (L_s - 1), \quad A = \text{QED}, \text{QCD}$$

$$C_A = Q_f^2, C_F, \text{ respectively, for } A = \text{QED}, \text{QCD}$$

⇒ QCD dominant corrections happen an order of magnitude earlier than those for QED.

⇒ Leading $\tilde{\beta}_{0,0}^{(0,0)}$ -level gives a good estimate of the size of the effects we study.

RESUMMED QUANTUM GRAVITY

APPLY (6) TO QUANTUM GENERAL RELATIVITY:

⇒

$$i\Delta'_F(k)|_{\text{resummed}} = \frac{ie^{B''_g(k)}}{(k^2 - m^2 - \Sigma'_s + i\epsilon)} \quad (8)$$

FOR

$$B''_g(k) = -2i\kappa^2 k^4 \frac{\int d^4\ell}{16\pi^4} \frac{1}{\ell^2 - \lambda^2 + i\epsilon} \frac{1}{(\ell^2 + 2\ell k + \Delta + i\epsilon)^2} \quad (9)$$

THIS IS THE BASIC RESULT.

NOTE THE FOLLOWING:

- Σ'_s STARTS IN $\mathcal{O}(\kappa^2)$, SO WE MAY DROP IT IN CALCULATING ONE-LOOP EFFECTS.

- EXPLICIT EVALUATION GIVES, FOR THE DEEP UV REGIME,

$$B_g''(k) = \frac{\kappa^2 |k^2|}{8\pi^2} \ln \left(\frac{m^2}{m^2 + |k^2|} \right), \quad (10)$$

⇒ THE RESUMMED PROPAGATOR FALLS FASTER THAN ANY POWER OF $|k^2|$!

- IF m VANISHES, USING THE USUAL $-\mu^2$ NORMALIZATION POINT WE GET $B_g''(k) = \frac{\kappa^2 |k^2|}{8\pi^2} \ln \left(\frac{\mu^2}{|k^2|} \right)$ WHICH AGAIN VANISHES FASTER THAN ANY POWER OF $|k^2|$!

THIS MEANS THAT ONE-LOOP CORRECTIONS ARE FINITE!

INDEED, ALL QUANTUM GRAVITY LOOPS ARE UV

FINITE(MPLA17(2002)2371)!

QED \otimes QCD Threshold Corrections, Shower/ME Matching

and IR-Improved DGLAP Theory at LHC

We shall apply the new simultaneous QED \otimes QCD exponentiation calculus to the single Z production with leptonic decay at the LHC (and at FNAL) to focus on the ISR alone, for definiteness. See also the work of Baur *et al.*, Dittmaier and Kramer, Zykunov for exact $\mathcal{O}(\alpha)$ results and Hamberg *et al.*, van Neerven and Matsuura and Anastasiou *et al.* for exact $\mathcal{O}(\alpha_s^2)$ results.

For the basic formula

$$d\sigma_{exp}(pp \rightarrow V + X \rightarrow \bar{\ell}\ell' + X') = \sum_{i,j} \int dx_i dx_j F_i(x_i) F_j(x_j) d\hat{\sigma}_{exp}(x_i x_j s), \quad (11)$$

we use the result in (6) here with semi-analytical methods and structure functions from Martin *et al.*.

A MC realization will appear elsewhere.

SHOWER/ME MATCHING

- Note the following: In (11) WE DO NOT ATTEMPT AT THIS TIME TO REPLACE HERWIG and/or PYTHIA – WE INTEND TO COMBINE OUR EXACT YFS CALCULUS, $d\hat{\sigma}_{exp}(x_i x_j s)$, WITH HERWIG and/or PYTHIA BY USING THEM/IT “IN LIEU” OF $\{F_i\}$.
 - A. USE HERWIG/PYTHIA SHOWER FOR $p_T \leq \mu$, YFS nG for $p_T > \mu$.
 - B. EXPAND HERWIG/PYTHIA SHOWER FORMULA $\otimes d\sigma_{exp}$ AND ADJUST $\tilde{\beta}_{n,m}$ TO EXACTNESS FOR DESIRED ORDER WITH NEW $\tilde{\beta}'_{n,m}$ FIRST USE $\{F_i\}$ TO PICK (x_1, x_2) ; MAKE EVT WITH $d\sigma_{exp}$; THEN SHOWER EVT USING HERWIG/PYTHIA VIA LES HOUCHEs RECIPE.
- THIS COMBINATION OF THEORETICAL CONSTRUCTS CAN BE SYSTEMATICALLY IMPROVED WITH EXACT RESULTS ORDER-BY-ORDER IN α_s, α , WITH EXACT PHASE SPACE.
- THE RECENT ALTERNATIVE PARTON SHOWER ALGORITHM BY JADACH and SKRZYPEK, Acta. Phys. Pol. B35, 745 (2004), CAN ALSO BE USED.
- LACK OF COLOR COHERENCE \Rightarrow ISAJET NOT CONSIDERED HERE.

With this said, we compute , with and without QED, the ratio

$$r_{exp} = \sigma_{exp} / \sigma_{Born}$$

to get the results (**We stress that we do not use the narrow resonance approximation here.**)

$$r_{exp} = \begin{cases} 1.1901 & , \text{QCED} \equiv \text{QCD+QED, LHC} \\ 1.1872 & , \text{QCD, LHC} \\ 1.1911 & , \text{QCED} \equiv \text{QCD+QED, Tevatron} \\ 1.1879 & , \text{QCD, Tevatron} \end{cases} \quad (12)$$

⇒

* **QED IS AT .3% AT BOTH LHC and FNAL.**

* **THIS IS STABLE UNDER SCALE VARIATIONS.**

* **WE AGREE WITH BAUR ET AL., HAMBERG ET AL., van NEERVEN and ZIJLSTRA.**

* **QED EFFECT SIMILAR IN SIZE TO STR. FN. RESULTS.**

* **DGLAP SYNTHESIZATION HAS NOT COMPROMISED THE NORMALIZATION.**

IR-Improved DGLAP Theory

APPLY QCD EXPN THEORY TO DGLAP KERNELS:

$$P_{qq}(z) = C_F F_{YFS}(\gamma_q) e^{\frac{1}{2}\delta_q} \left[\frac{1+z^2}{1-z} (1-z)^{\gamma_q} - f_q(\gamma_q) \delta(1-z) \right] \quad (13)$$

where

$$f_q(\gamma_q) = \frac{2}{\gamma_q} - \frac{2}{\gamma_q + 1} + \frac{1}{\gamma_q + 2} \quad (14)$$

and

$$\gamma_q = C_F \frac{\alpha_s}{\pi} t = \frac{4C_F}{\beta_0} \quad (15)$$

$$\delta_q = \frac{\gamma_q}{2} + \frac{\alpha_s C_F}{\pi} \left(\frac{\pi^2}{3} - \frac{1}{2} \right) \quad (16)$$

and

$$F_{YFS}(\gamma_q) = \frac{e^{-C_E \gamma_q}}{\Gamma(1 + \gamma_q)}. \quad (17)$$

SIMILAR RESULTS HOLD FOR P_{Gq} , P_{GG} , P_{qG} , GIVING:

$$P_{qq}(z) = C_F F_{YFS}(\gamma_q) e^{\frac{1}{2}\delta_q} \left[\frac{1+z^2}{1-z} (1-z)^{\gamma_q} - f_q(\gamma_q) \delta(1-z) \right], \quad (18)$$

$$P_{Gq}(z) = C_F F_{YFS}(\gamma_q) e^{\frac{1}{2}\delta_q} \frac{1+(1-z)^2}{z} z^{\gamma_q}, \quad (19)$$

$$P_{GG}(z) = 2C_G F_{YFS}(\gamma_G) e^{\frac{1}{2}\delta_G} \left\{ \frac{1-z}{z} z^{\gamma_G} + \frac{z}{1-z} (1-z)^{\gamma_G} \right. \\ \left. + \frac{1}{2} (z^{1+\gamma_G} (1-z) + z(1-z)^{1+\gamma_G}) - f_G(\gamma_G) \delta(1-z) \right\}, \quad (20)$$

$$P_{qG}(z) = F_{YFS}(\gamma_G) e^{\frac{1}{2}\delta_G} \frac{1}{2} \{ z^2 (1-z)^{\gamma_G} + (1-z)^2 z^{\gamma_G} \}, \quad (21)$$

where

$$\gamma_G = C_G \frac{\alpha_s}{\pi} t = \frac{4C_G}{\beta_0} \quad (22)$$

$$\delta_G = \frac{\gamma_G}{2} + \frac{\alpha_s C_G}{\pi} \left(\frac{\pi^2}{3} - \frac{1}{2} \right), \quad (23)$$

$$f_G(\gamma_G) = \frac{n_f}{C_G} \frac{1}{(1 + \gamma_G)(2 + \gamma_G)(3 + \gamma_G)} + \frac{2}{\gamma_G(1 + \gamma_G)(2 + \gamma_G)} \quad (24)$$

$$+ \frac{1}{(1 + \gamma_G)(2 + \gamma_G)} + \frac{1}{2(3 + \gamma_G)(4 + \gamma_G)} \quad (25)$$

$$+ \frac{1}{(2 + \gamma_G)(3 + \gamma_G)(4 + \gamma_G)}. \quad (26)$$

Parton Distributions

Moments of kernels \Leftrightarrow Logarithmic exponents for evolution

$$\frac{dM_n^{NS}(t)}{dt} = \frac{\alpha_s(t)}{2\pi} A_n^{NS} M_n^{NS}(t) \quad (27)$$

where

$$M_n^{NS}(t) = \int_0^1 dz z^{n-1} q^{NS}(z, t) \quad (28)$$

and the quantity A_n^{NS} is given by

$$\begin{aligned} A_n^{NS} &= \int_0^1 dz z^{n-1} P_{qq}(z), \\ &= C_F F_{YFS}(\gamma_q) e^{\frac{1}{2}\delta_q} [B(n, \gamma_q) + B(n+2, \gamma_q) - f_q(\gamma_q)] \end{aligned} \quad (29)$$

where $B(x, y)$ is the beta function given by

$$B(x, y) = \Gamma(x)\Gamma(y)/\Gamma(x + y)$$

.

Compare the usual result

$$A_n^{NS^o} \equiv C_F \left[-\frac{1}{2} + \frac{1}{n(n+1)} - 2 \sum_{j=2}^n \frac{1}{j} \right]. \quad (30)$$

- **ASYMPTOTIC BEHAVIOR: IR-improved goes to a multiple of $-f_q$, consistent with $\lim_{n \rightarrow \infty} z^{n-1} = 0$ for $0 \leq z < 1$;
usual result diverges as $-2C_F \ln n$.**
- **Different for finite n as well: for $n = 2$ we get, for example, for $\alpha_s \cong .118$,**

$$A_2^{NS} = \begin{cases} C_F(-1.33) & , \text{ un-IR-improved} \\ C_F(-0.966) & , \text{ IR-improved} \end{cases} \quad (31)$$

- For completeness we note

$$\begin{aligned}
 M_n^{NS}(t) &= M_n^{NS}(t_0) e^{\int_{t_0}^t dt' \frac{\alpha_s(t')}{2\pi}} A_n^{NS}(t') \\
 &= M_n^{NS}(t_0) e^{\bar{a}_n [Ei(\frac{1}{2} \delta_1 \alpha_s(t_0)) - Ei(\frac{1}{2} \delta_1 \alpha_s(t))]} \\
 &\xrightarrow[t, t_0 \text{ large with } t \gg t_0]{} M_n^{NS}(t_0) \left(\frac{\alpha_s(t_0)}{\alpha_s(t)} \right)^{\bar{a}'_n}
 \end{aligned} \tag{32}$$

where $Ei(x) = \int_{-\infty}^x dr e^r / r$ is the exponential integral function,

$$\begin{aligned}
 \bar{a}_n &= \frac{2C_F}{\beta_0} F_{YFS}(\gamma_q) e^{\frac{\gamma_q}{4}} [B(n, \gamma_q) + B(n+2, \gamma_q) - f_q(\gamma_q)] \\
 \bar{a}'_n &= \bar{a}_n \left(1 + \frac{\delta_1}{2} \frac{(\alpha_s(t_0) - \alpha_s(t))}{\ln(\alpha_s(t_0)/\alpha_s(t))} \right)
 \end{aligned} \tag{33}$$

with

$$\delta_1 = \frac{C_F}{\pi} \left(\frac{\pi^2}{3} - \frac{1}{2} \right).$$

Compare with un-IR-improved result where last line in eq.(32) holds exactly with $\bar{a}'_n = 2A_n^{NS^o} / \beta_0$.

- Comparison with Moch et al., Vogt et al., etc., in progress.

FINAL STATE OF HAWKING RADIATION

CONSIDER THE GRAVITON PROPAGATOR IN THE THEORY OF GRAVITY COUPLED TO A MASSIVE SCALAR(HIGGS) FIELD(Feynman). WE HAVE THE GRAPHS

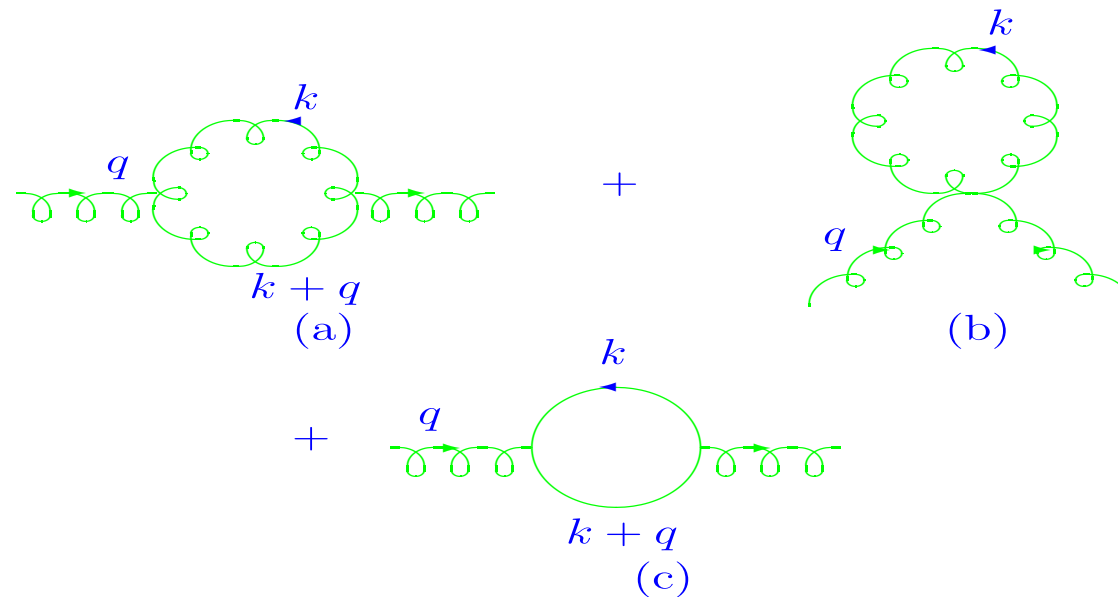


Figure 1: The graviton((a),(b)) and its ghost((c)) one-loop contributions to the graviton propagator. q is the 4-momentum of the graviton.

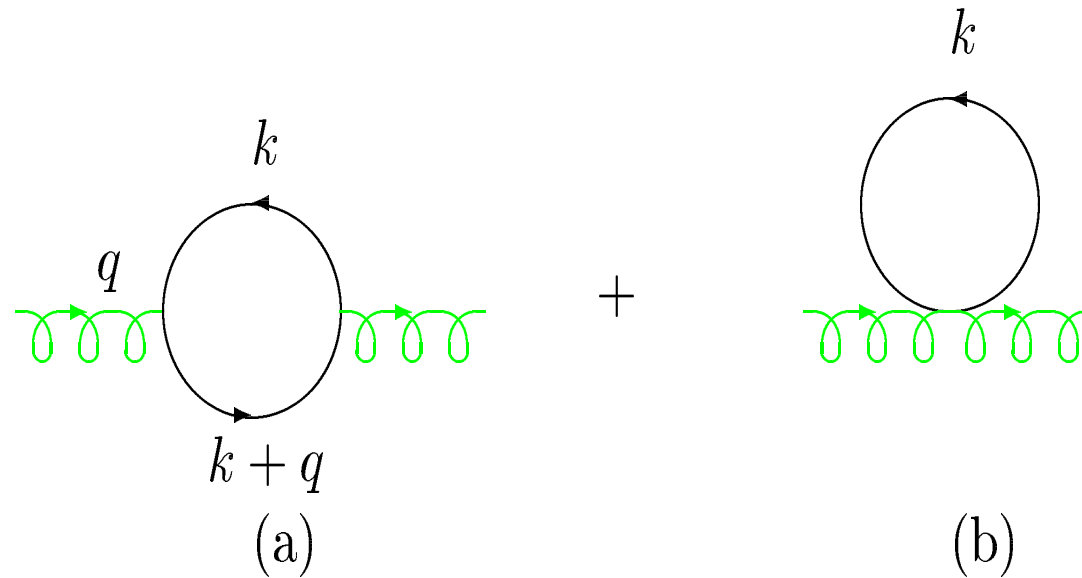


Figure 2: The scalar one-loop contribution to the graviton propagator. q is the 4-momentum of the graviton.

USING THE RESUMMED THEORY, WE GET THAT THE NEWTON POTENTIAL BECOMES

$$\Phi_N(r) = -\frac{G_N M}{r} (1 - e^{-ar}), \quad (34)$$

FOR

$$a \cong 0.210 M_{Pl}. \quad (35)$$

CONTACT WITH ASYMPTOTIC SAFETY APPROACH

- OUR RESULTS IMPLY

$$G(k) = G_N / \left(1 + \frac{k^2}{a^2}\right)$$

⇒ FIXED POINT BEHAVIOR FOR

$$k^2 \rightarrow \infty,$$

IN AGREEMENT WITH THE PHENOMENOLOGICAL ASYMPTOTIC SAFETY APPROACH OF BONNANNO & REUTER IN PRD62(2000) 043008.

- OUR RESULTS IMPLY THAT AN ELEMENTARY PARTICLE HAS
NO HORIZON WHICH ALSO AGREES WITH BONNANNO'S & REUTER'S
RESULT THAT A BLACK HOLE WITH A MASS LESS THAN

$$M_{cr} \sim M_{Pl}$$

HAS NO HORIZON.

BASIC PHYSICS:

$G(k)$ VANISHES FOR $k^2 \rightarrow \infty$.

- A FURTHER “AGREEMENT”: FINAL STATE OF HAWKING RADIATION OF AN ORIGINALLY VERY MASSIVE BLACKHOLE

BECAUSE OUR VALUE OF THE COEFFICIENT,

$$\frac{1}{a^2},$$

OF k^2 IN THE DENOMINATOR OF $G(k)$

AGREES WITH THAT FOUND BY BONNANNO & REUTER(B-R),

IF WE USE THEIR PRESCRIPTION FOR THE

RELATIONSHIP BETWEEN k AND r

IN THE REGIME WHERE THE LAPSE FUNCTION VANISHES,

WE GET THE SAME HAWKING RADIATION PHENOMENOLOGY AS THEY DO:

THE BLACK HOLE EVAPORATES IN THE B-R ANALYSIS UNTIL IT REACHES A MASS

$$M_{cr} \sim M_{Pl}$$

AT WHICH THE BEKENSTEIN-HAWKING TEMPERATURE VANISHES,

LEAVING A PLANCK SCALE REMNANT.

- FATE OF REMNANT? IN hep-ph/0503189 \Rightarrow OUR QUANTUM LOOP EFFECTS COMBINED WITH THE $G(r)$ OF B-R IMPLY HORIZON OF THE PLANCK SCALE REMNANT IS OBIATED – CONSISTENT WITH RECENT RESULTS OF HAWKING.

TO WIT, IN THE METRIC CLASS

$$ds^2 = f(r)dt^2 - f(r)^{-1}dr^2 - r^2d\Omega^2 \quad (36)$$

THE LAPSE FUNCTION IS, FROM B-R,

$$\begin{aligned} f(r) &= 1 - \frac{2G(r)M}{r} \\ &= \frac{B(x)}{B(x) + 2x^2} \Big|_{x=\frac{r}{G_N M}}, \end{aligned} \quad (37)$$

WHERE

$$B(x) = x^3 - 2x^2 + \Omega x + \gamma\Omega \quad (38)$$

FOR

$$\Omega = \frac{\tilde{\omega}}{G_N M^2} = \frac{\tilde{\omega} M_{Pl}^2}{M^2}. \quad (39)$$

AFTER H-RADIATING TO REGIME NEAR $M_{cr} \sim M_{Pl}$, QUANTUM LOOPS ALLOW US TO REPLACE $G(r)$ WITH $G_N(1 - e^{-ar})$ IN THE LAPSE FUNCTION FOR $r < r_>$, THE OUTERMOST SOLUTION OF

$$G(r) = G_N(1 - e^{-ar}). \quad (40)$$

IN THIS WAY, WE SEE THAT THE INNER HORIZON MOVES TO NEGATIVE r AND THE OUTER HORIZON MOVES TO $r = 0$ AT THE NEW CRITICAL MASS $\sim 2.38M_{Pl}$.

NOTE: M. BOJOWALD *et al.*, gr-qc/0503041, – LOOP QG CONCURS WITH GENERAL CONCLUSION.

PREDICTION: THERE SHOULD BE ENERGETIC COSMIC RAYS AT $E \sim M_{Pl}$ DUE TO THE DECAY OF SUCH A REMNANT.

Conclusions

YFS THEORY (EEX AND CEEX) EXTENDS TO NON-ABELIAN GAUGE THEORY AND ALLOWS SIMULTANEOUS EXPN OF QED AND QCD WITH PROPER SHOWER/ME MATCHING BUILT-IN.

FOR QED \otimes QCD

- FULL MC EVENT GENERATOR REALIZATION IS POSSIBLE.
- SEMI-ANALYTICAL RESULTS FOR QED (AND QCD) THRESHOLD EFFECTS AGREE WITH LITERATURE ON Z PRODUCTION
- AS QED IS AT THE .3% LEVEL, IT IS NEEDED FOR 1% LHC THEORY PREDICTIONS.
- A FIRM BASIS FOR THE COMPLETE $\mathcal{O}(\alpha_s^2, \alpha\alpha_s, \alpha^2)$ MC RESULTS NEEDED FOR THE FNAL/LHC/RHIC/TESLA/LC PHYSICS HAS BEEN DEMONSTRATED AND ALL THE LATTER IS IN PROGRESS.

THE THEORY ALLOWS A NEW APPROACH
TO QUANTUM GENERAL RELATIVITY:

- RESUMMED QG UV FINITE

- MANY CONSEQUENCES:

BLACK HOLES EVAPORATE TO FINAL MASS $\sim M_{Pl}$

WITH NO HORIZON

$\Rightarrow E \sim M_{Pl}$ COSMIC RAYS, \dots