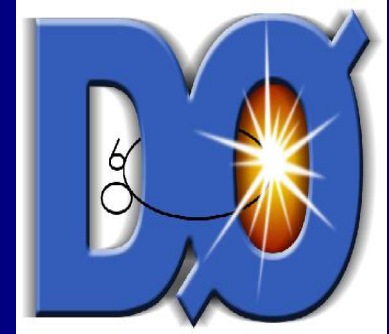




# Top Quark Properties at the Tevatron



- Outline:
- Measurements of the Top Quark Mass
  - Measurements of other Top Quark Properties
    - W Boson Helicity
    - Top Quark Charge
    - Search for  $t\bar{t}$  Resonances

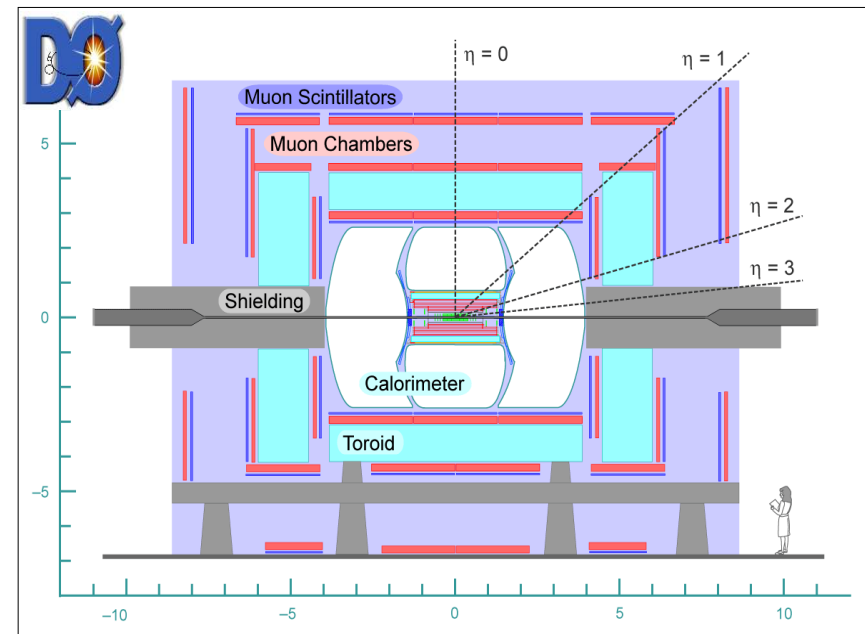
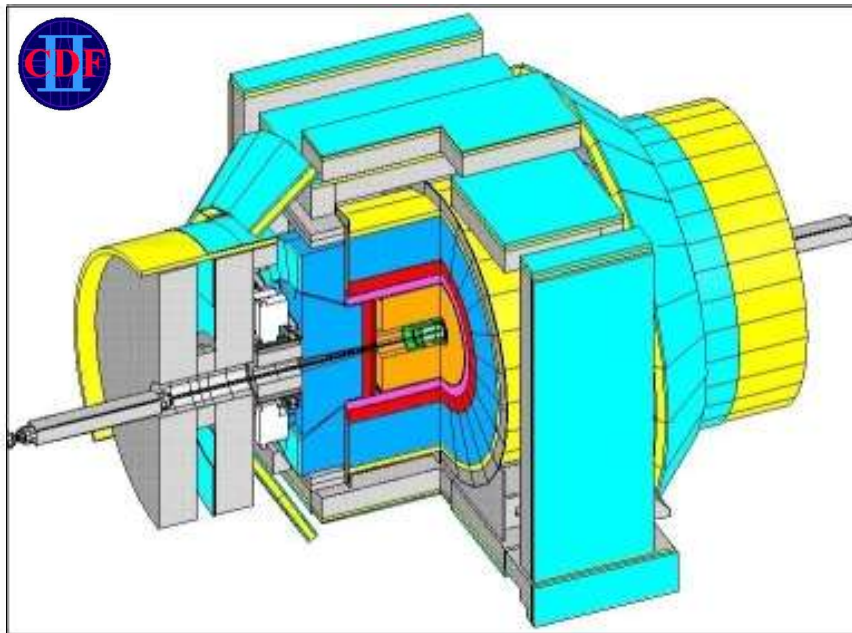
Philipp Schieferdecker, Munich University (LMU)  
on behalf of the CDF and DØ Collaborations



**bmb+f** - Förderschwerpunkt

Elementarteilchenphysik

Großgeräte der physikalischen  
Grundlagenforschung

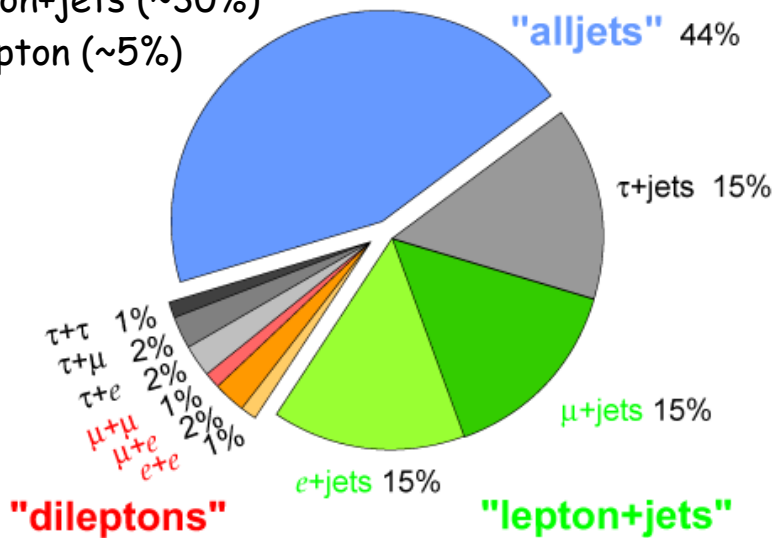


- Both CDF and DØ recording collisions at  $\sqrt{s}=1.96 \text{ TeV}$  from the Tevatron, currently the world's only top quark factory
- Precise tracking and vertexing for b-tagging and improved lepton identification
- Data taking efficiency:  $>85\%$
- More than  $1\text{fb}^{-1}$  of data recorded per experiment; Results presented here make use of up to  $750\text{pb}^{-1}$

- In ppbar collision at  $\sqrt{s}=1.96$  TeV, top quarks are primarily produced in pairs
  - SM cross section:  $\sim 7$  pb
  - $\sim 85\%$  via quark annihilation
  - $\sim 15\%$  via gluon fusion

- $t \rightarrow Wb$  branching ratio  $\sim 1$ , different analysis channels considered according to W boson decay modes:

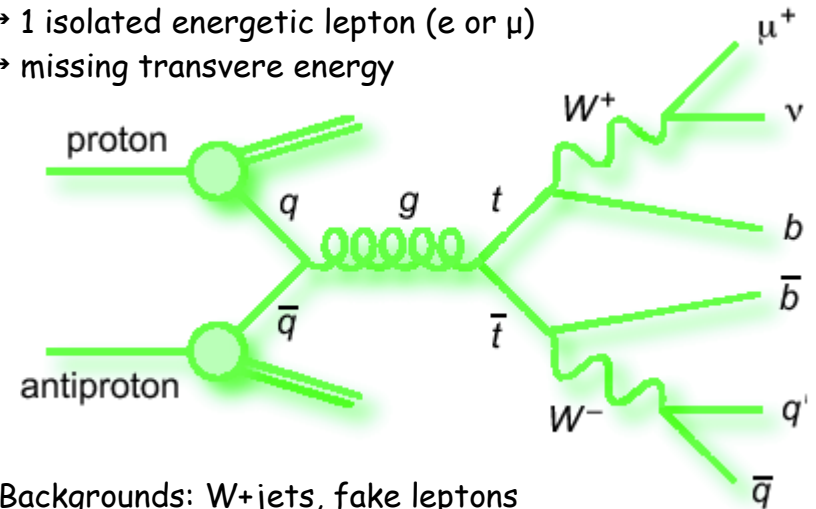
- alljets ( $\sim 44\%$ )
- lepton+jets ( $\sim 30\%$ )
- dilepton ( $\sim 5\%$ )



- Reconstruction of  $\tau$ -leptons is experimentally challenging.  $\tau$ -final states are not considered in the analyses presented here, in the following "lepton" always refers to  $e$  or  $\mu$ !

## Lepton+Jets:

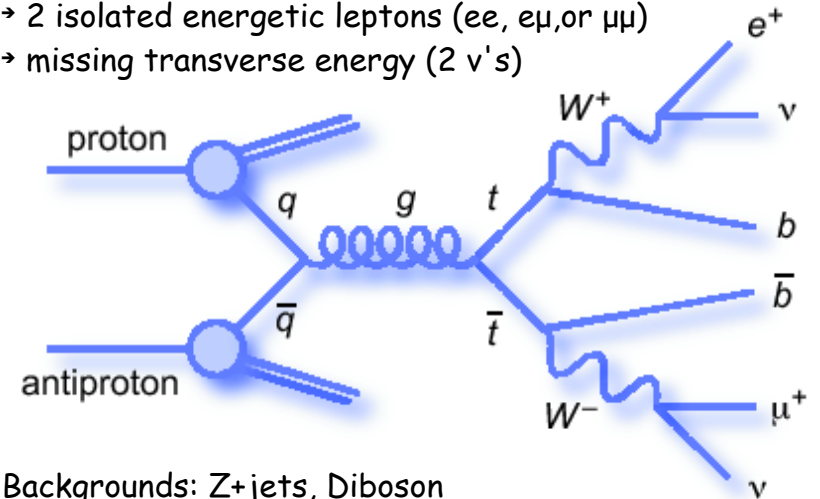
- $\geq 4$  calorimeter jets (2 b-jets)
- 1 isolated energetic lepton ( $e$  or  $\mu$ )
- missing transverse energy



Backgrounds:  $W$ +jets, fake leptons

## Dilepton:

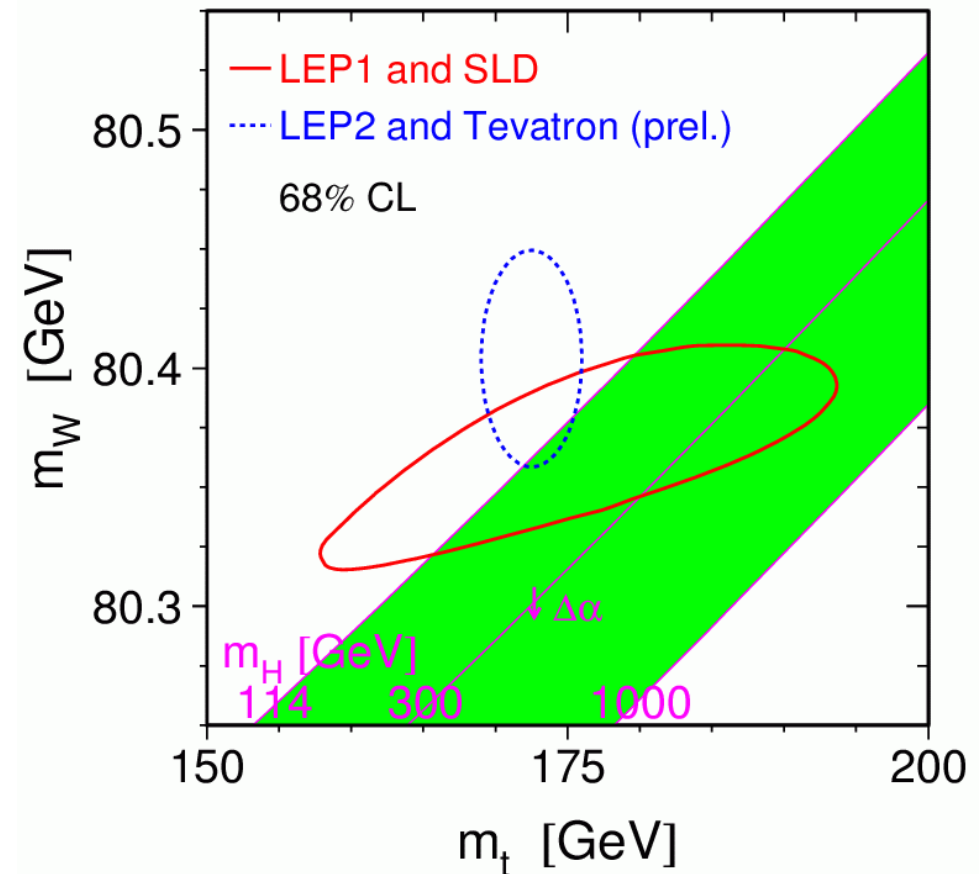
- $\geq 2$  calorimeter jets (2 b-jets)
- 2 isolated energetic leptons ( $ee, e\mu, \text{or } \mu\mu$ )
- missing transverse energy (2  $\nu$ 's)



Backgrounds:  $Z$ +jets, Diboson

- The top quark mass is a free parameter of the Standard Model
- The top quark is by far the heaviest of the six known quarks
- Its suspiciously high mass suggests a special role of the top quark in the Standard Model yet to be revealed
- Precision measurements of the top quark and  $W$  boson masses constrain the mass of the Higgs boson via radiative corrections
- With  $4\text{-}8\text{fb}^{-1}$  of Tevatron data:  $\delta m_t \sim 1.5\text{ GeV}$  (CDF and DØ combined)

Tevatron top quark mass measurements will be relevant for many years, even after LHC turnon



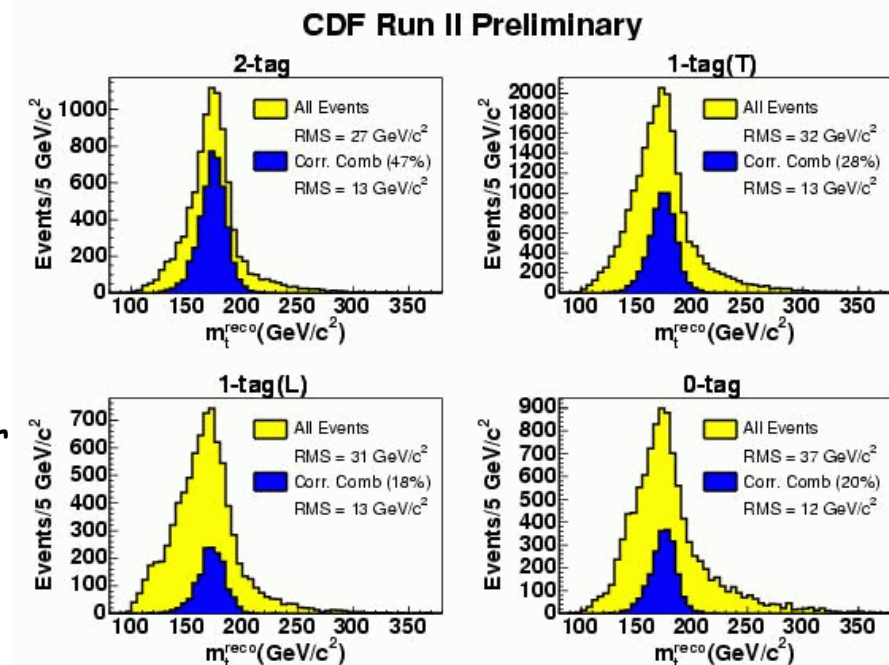
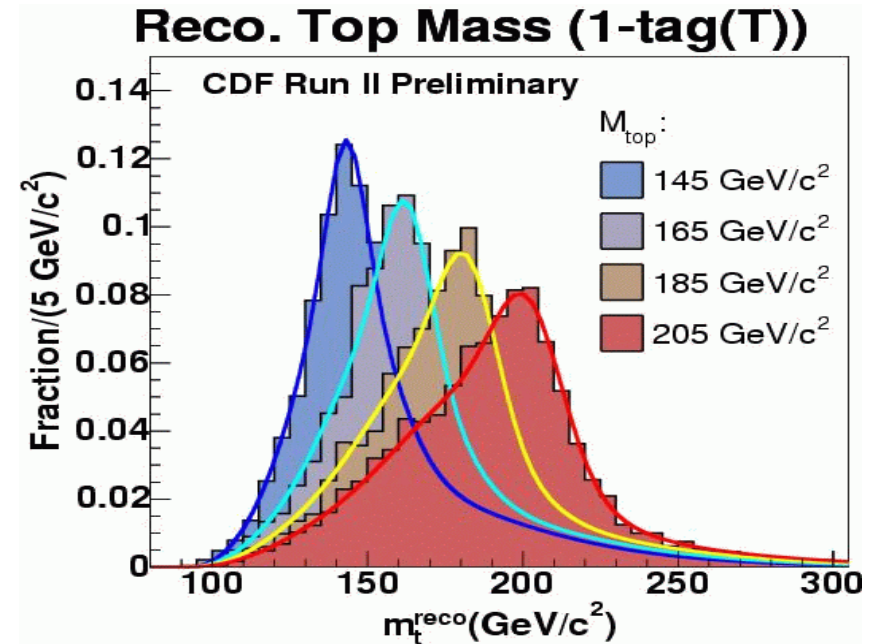
- For each event, reconstruct  $m_{\top}$  using a kinematic fit:

$$\chi^2 = \sum_{i=\ell, 4\text{jets}} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,fit} - p_j^{UE,meas})^2}{\sigma_j^2} + \frac{(M_{\ell\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{b\ell\nu} - m_t^{\text{reco}})^2}{\Gamma_t^2} + \frac{(M_{bjj} - m_t^{\text{reco}})^2}{\Gamma_t^2}$$

- Choose  $m_{\top}$  from jet-parton assignment with lowest  $\chi^2$
- Build template distributions from Monte Carlo samples with different true top quark masses
- Extract result from data sample using an unbinned likelihood fit:

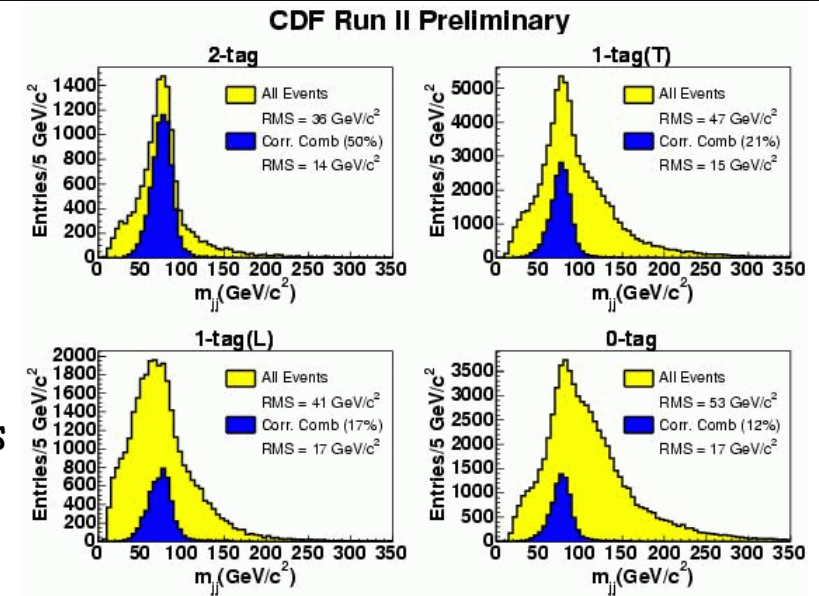
$$\mathcal{L}_{\text{sample}} = \mathcal{L}_{\text{shape}}^{m_t^{\text{reco}}} \times \mathcal{L}_{\text{shape}}^{m_{jj}} \times \mathcal{L}_{\text{nev}} \times \mathcal{L}_{\text{bg}}$$

- Divide events into 4 subsamples according to the number of identified b-jets to improve statistical sensitivity
  - events with more b-tags show better mass resolution and higher S/B
  - 1-tag(L): lower pT threshold for 4<sup>th</sup> jet than 1-tag(T)



In situ jet energy calibration:

- The mass of the hadronically decaying  $W$  boson provides a constraint on the jet energy calibration
- Expressed in units of the uncertainty  $\sigma(p_T, \eta)$  of the external calibration
- Use reconstructed di-jet mass templates, various scales
- Reduce dominant systematic uncertainty due to jet energy scale!

Systematic Uncertainties:

- Dominant systematic uncertainty (JES) absorbed in likelihood fit result ( $\sim 1.8$  GeV)
- Residual JES error: from  $p_T$  and  $\eta$  dependent scale uncertainties
- Remaining uncertainties largely due to uncertainties in modeling

Source	$\Delta M_{top} (GeV/c^2)$
Residual Jet Energy Scale	0.7
ISR/FSR	0.6
B-jet modeling	0.6
Background Shape	0.5
Background JES	0.4
Parton Distributions	0.3
Generator	0.2
Simulation Statistics	0.3
B-tagging	0.1
<b>Total</b>	<b>1.3</b>

Result:

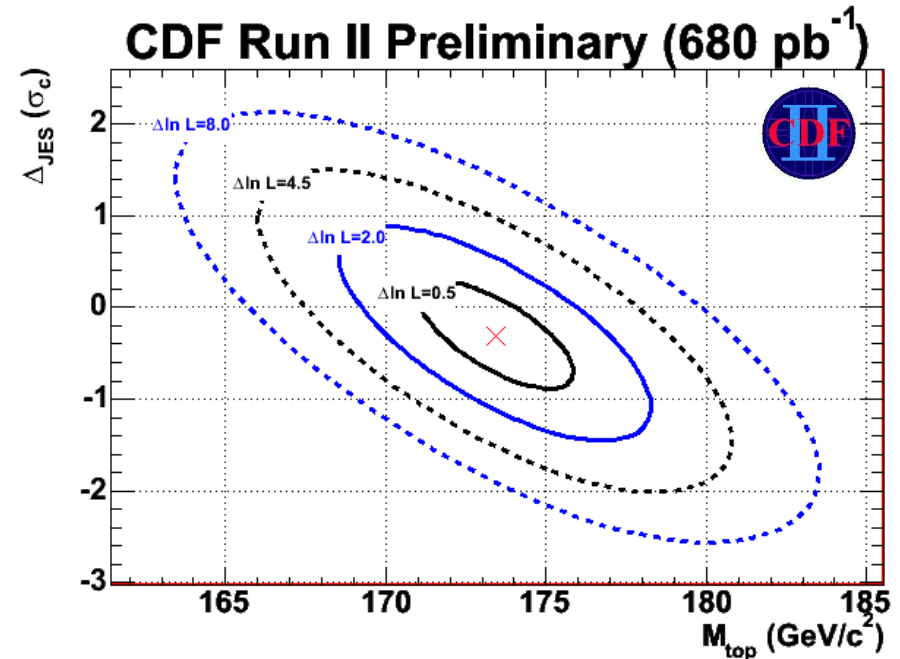
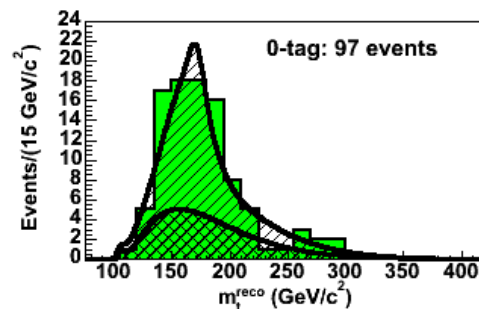
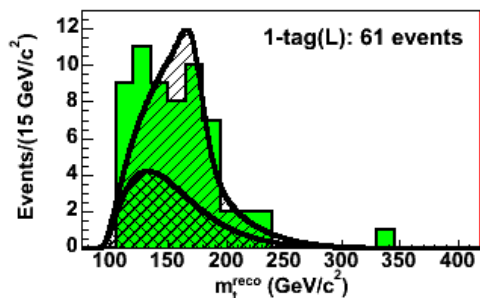
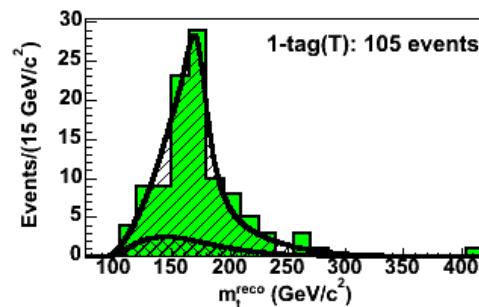
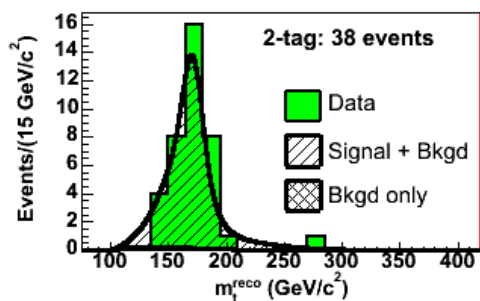
$$m_{\tau} = 173.4 \pm 2.5 \text{ (stat.+JES)} \pm 1.3 \text{ (syst.) GeV}$$

or

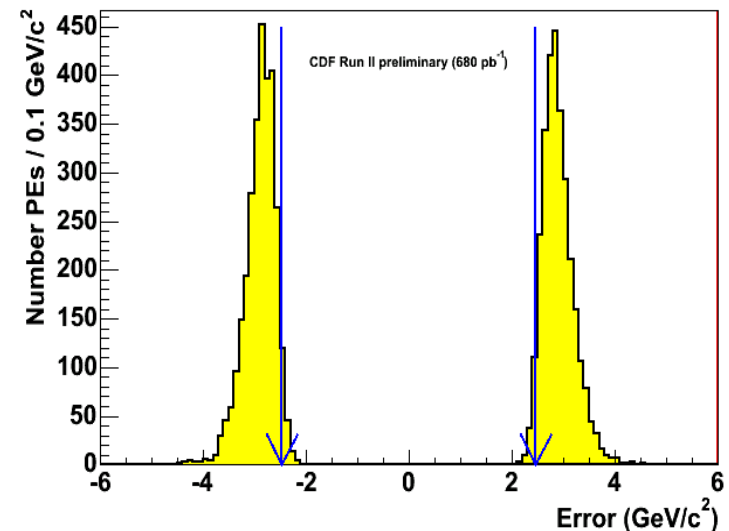
$$m_{\tau} = 173.4 \pm 2.8 \text{ GeV}$$

Single best measurement of  $m_{\tau}$ 

$$\Delta\text{JES} = -0.3 \pm 0.6\sigma$$

CDF Run II Preliminary (680 pb<sup>-1</sup>)

Expected error with observed num events



- Use each event's full kinematic information to calculate probability to originate from  $t\bar{t}$  production, as a function of assumed  $m_t$
- Calculate the probability to be background accordingly and combine to event probability:

$$\rightarrow P_{\text{evt}}(\mathbf{x}; m_t, f_{\text{sgn}}) = f_{\text{sgn}} P_{\text{sgn}}(\mathbf{x}; m_t) + (1 - f_{\text{sgn}}) P_{\text{bkg}}(\mathbf{x})$$

where  $f_{\text{sgn}}$  is the fraction of signal events in the sample

- Combine all events in a likelihood

$$\rightarrow -\ln L(\mathbf{x}_1, \dots, \mathbf{x}_n; m_t, f_{\text{sgn}}) = -\sum_{i=1}^n \ln P_{\text{evt}}(\mathbf{x}_i; m_t, f_{\text{sgn}})$$

and maximize likelihood w.r.t. to  $m_t$  and  $f_{\text{sgn}}$

- Well measured events contribute more than poorly measured events:  
**achieve optimal use of statistical information!**
- I will present applications of this method to both lepton+jets and dilepton events
- Lepton+Jets: Use invariant mass of hadronically decaying W boson to obtain JES
  - $L=L(\mathbf{x}_1, \dots, \mathbf{x}_n; m_t, f_{\text{sgn}}, \text{JES})$
  - JES is global scale factor relative to external jet energy calibration
  - Reduce dominant systematic uncertainty by fitting  $m_t$  and JES simultaneously

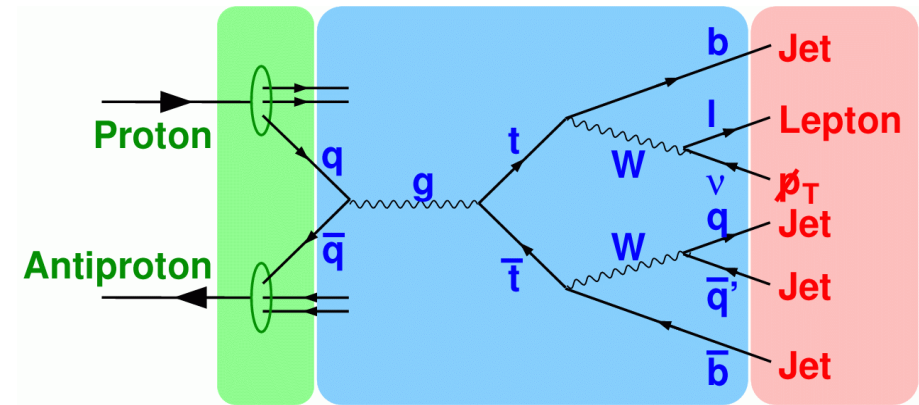


## Calculation of the signal probability:

- Integration over parton phasespace ( $y$ )
- Assume all angles to be well measured
- Assume  $p_T(t\bar{t})=0$
- Parametrize detector resolution of all energies ( $W(x,y)$ )
- Perform remaining (5-6) integrations using MC integration techniques:

$$\mathcal{P}_{t\bar{t}}(\vec{x}, m_t) = \underbrace{\frac{1}{\sigma_{t\bar{t}}(m_t)}}_{\text{Normalisation}} \int \underbrace{dp_q dp_{\bar{q}} f(p_q) f(p_{\bar{q}})}_{\text{PDFs}} \underbrace{d\sigma_{t\bar{t}}(\vec{y}, m_t)}_{\substack{\text{diff. xsec} \\ \text{MATRIX ELEMENT}}} \underbrace{W(\vec{x}, \vec{y})}_{\text{det. resolutions}}$$

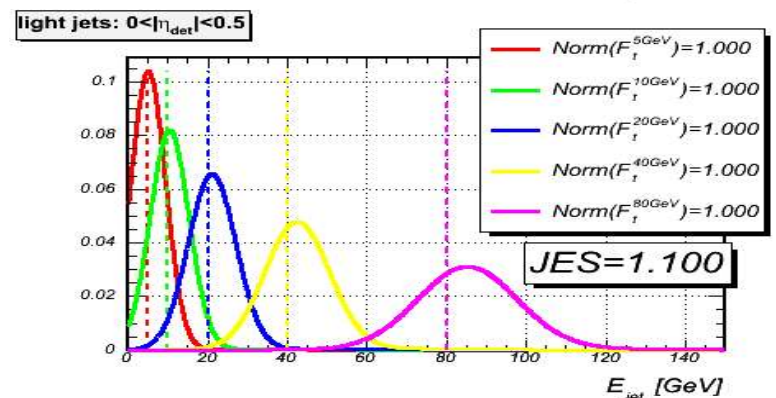
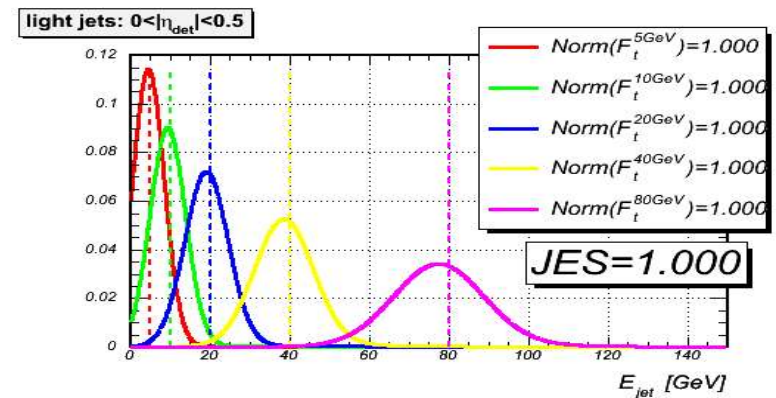
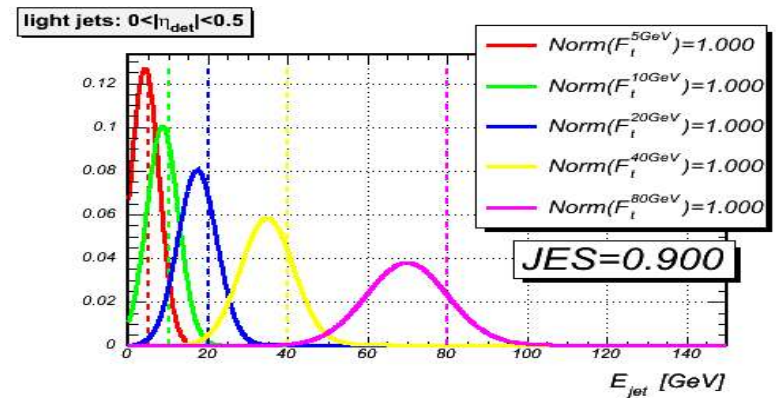
- Consider all possible jet-parton assignments!
- Consider all possible solutions for the z-component of the neutrino momenta



## Parametrization of jet energy resolution: jet transfer function $W(E_j, E_p)$

- $W(E_j, E_p)$  yields for each parton energy  $E_p$  the probability to be measured as  $E_j$  ( $j$ =jet) in the calorimeter
- Parametrized as a double Gaussian in  $\delta E = E_j - E_p$  (5 parameters), where each parameter is a linear function of  $E_p$  itself
  - jet resolution is function of  $E_p$
- Different parameter sets for light jets, b jets, and semileptonic b-jets. Derived from Monte Carlo events.
- Lepton+Jets: The global jet energy scale parameter JES is included in the event probability via the jet transfer function:

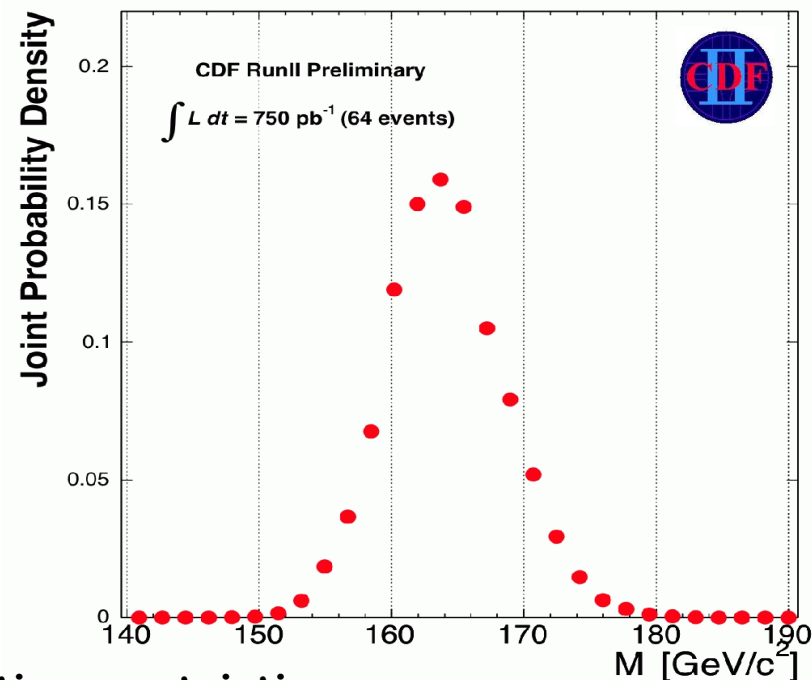
$$W(E_j, E_p; JES) = \frac{W\left(\frac{E_j}{JES} - E_p\right)}{JES}$$



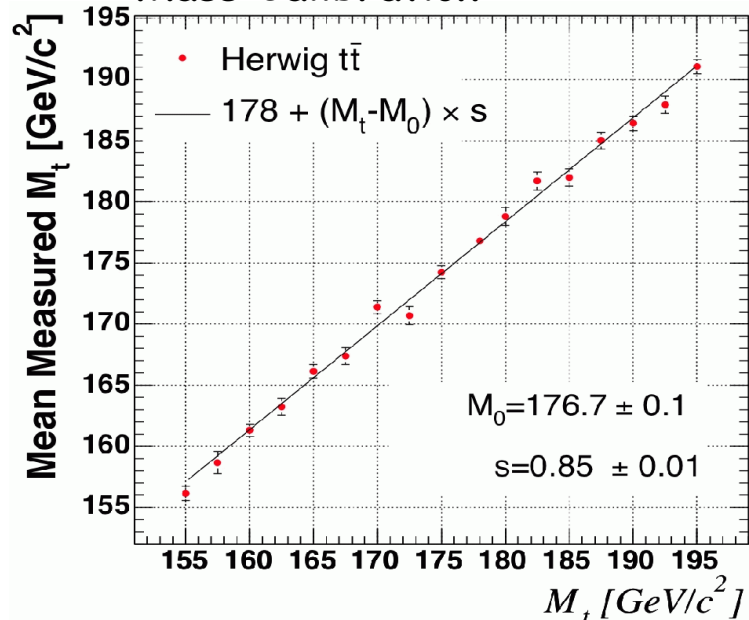
## Dilepton-Result:

$$m_t = 164.5 \pm 4.5 \text{ (stat.)} \pm 3.1 \text{ (syst.) GeV}$$

- Most precise dilepton-measurement to date
- No b-tagging used in result above
- Result with b-tagging:  $162.7 \pm 4.6_{\text{stat}} \pm 3.0_{\text{syst}} \text{ GeV}$ 
  - require at least one b-tagged jet (secondary vertex tag)



## Mass Calibration:



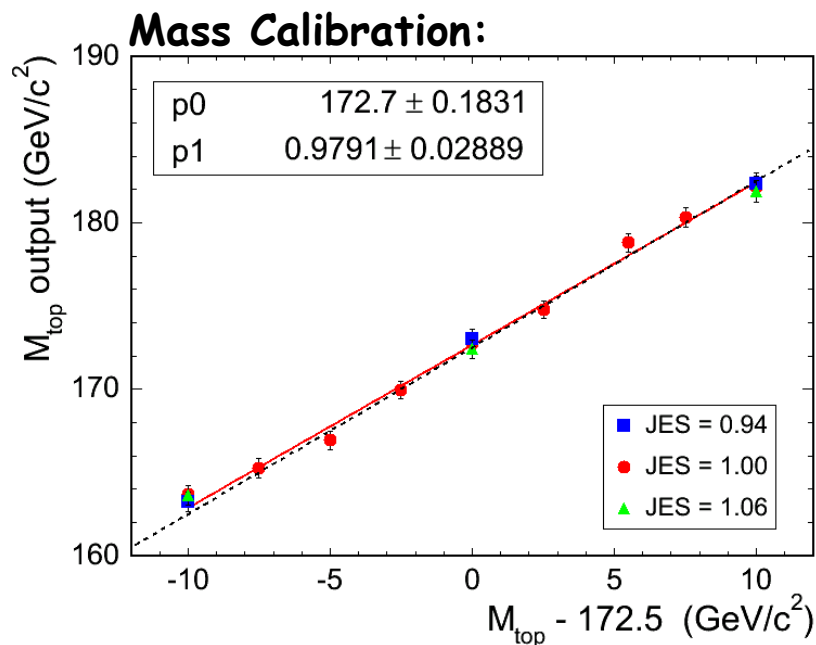
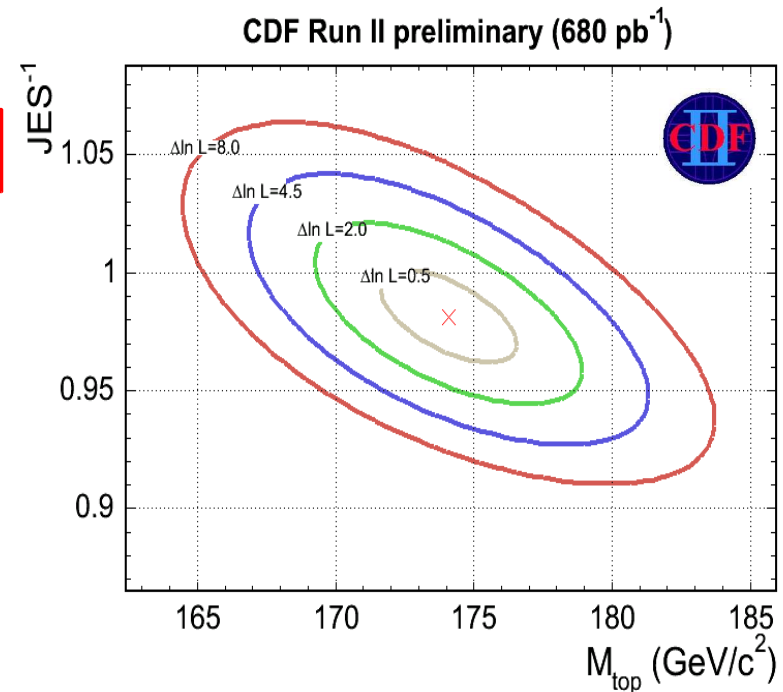
## Systematic uncertainties:

Source	$\Delta M_t$ (GeV/ $c^2$ )
Jet Energy Scale	2.6
Generator	0.5
Response uncertainty	0.3
Sample composition uncertainty	0.7
Background statistics	0.8
Background modeling	0.8
ISR modeling	0.5
FSR modeling	0.5
PDFs	0.6
Total	3.1

## Lepton+Jets-Result:

$$m_{\tau} = 174.1 \pm 2.5 \text{ (stat.+JES)} \pm 1.3 \text{ (syst.) GeV}$$

- More powerful technique than template method (p.5-7), but fewer events used (118/360)
  - exactly 4 calorimeter jets
  - at least one **b-tagged jet** (secondary vertex tag)



### Systematic uncertainties:

Source of systematic uncertainty	Magnitude (GeV/c <sup>2</sup> )
Residual JES	0.42
<i>b</i> -JES	0.60
Generator	0.19
ISR	0.72
FSR	0.76
<i>b</i> -tag $E_T$ dependence	0.31
Background composition	0.21
PDF	0.12
Monte Carlo statistics	0.04
<b>Total</b>	<b>1.35</b>



# DØ: Matrix Element Method (lepton+jets)

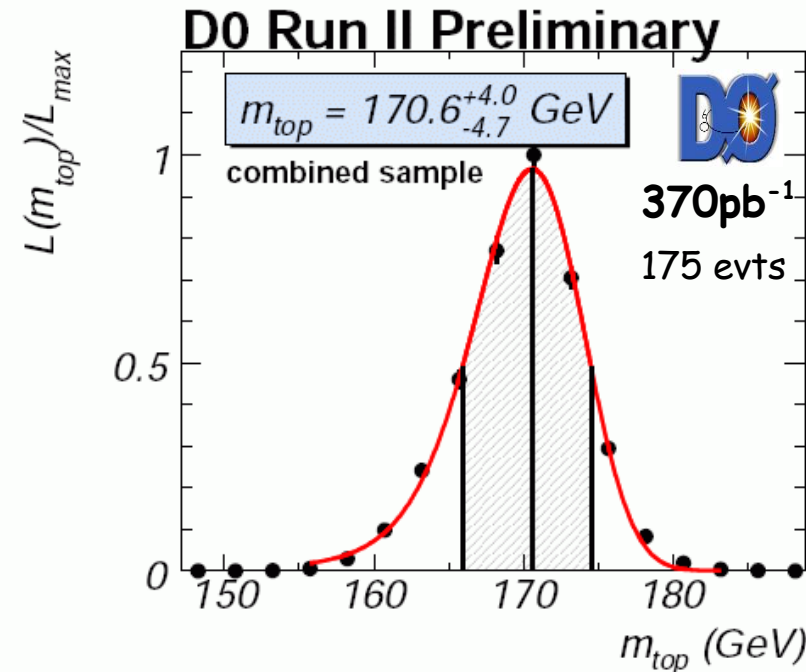


## Lepton+Jets-Result:

$$m_{\tau} = 170.6^{+4.0}_{-4.7} \text{ (stat.+JES)} \pm 1.4 \text{ (syst.) GeV}$$

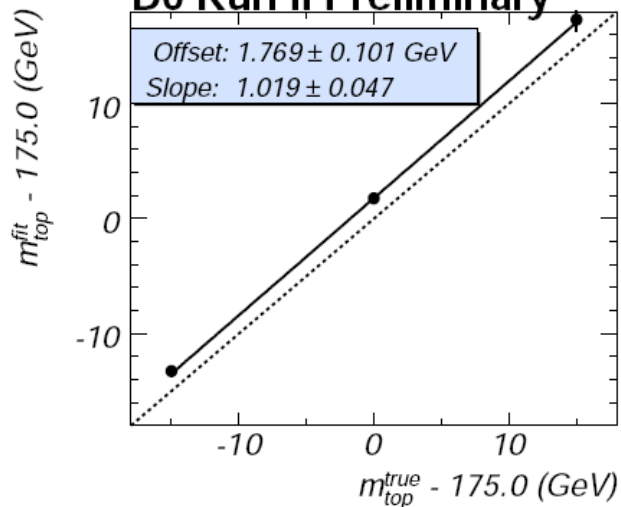
Single best DØ measurement

- Based on 370pb<sup>-1</sup> dataset
- Similar to the CDF template analysis, the sample is divided in subsamples with 0,1,or 2 **b-tagged jets**
  - ~20% improvement w.r.t analysis w/o b-tagging
  - ~30% improvement w.r.t. selecting events with at least 1 b-tagged jet



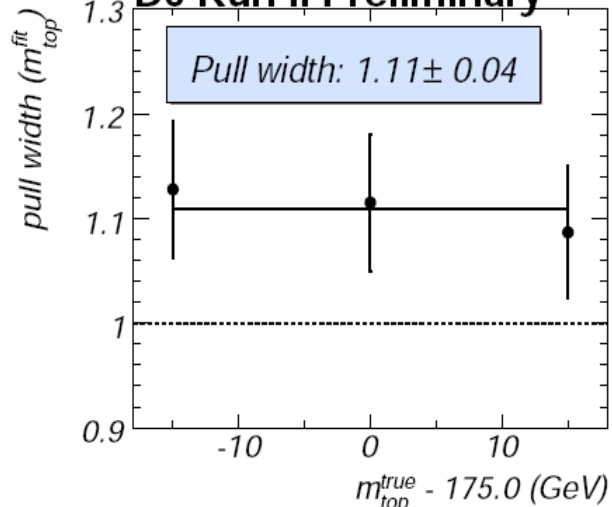
## Mass Calibration:

DØ Run II Preliminary

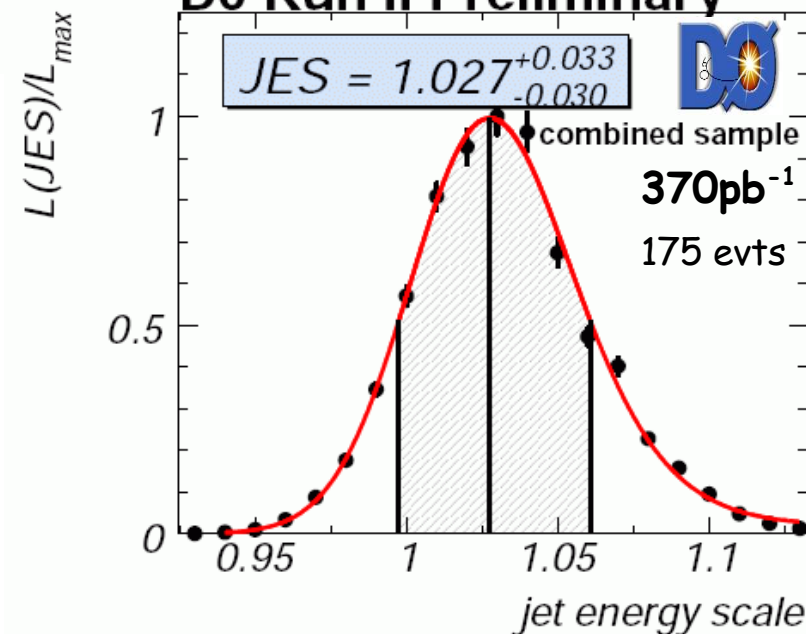


## Pull-width Calibration:

DØ Run II Preliminary



## DØ Run II Preliminary



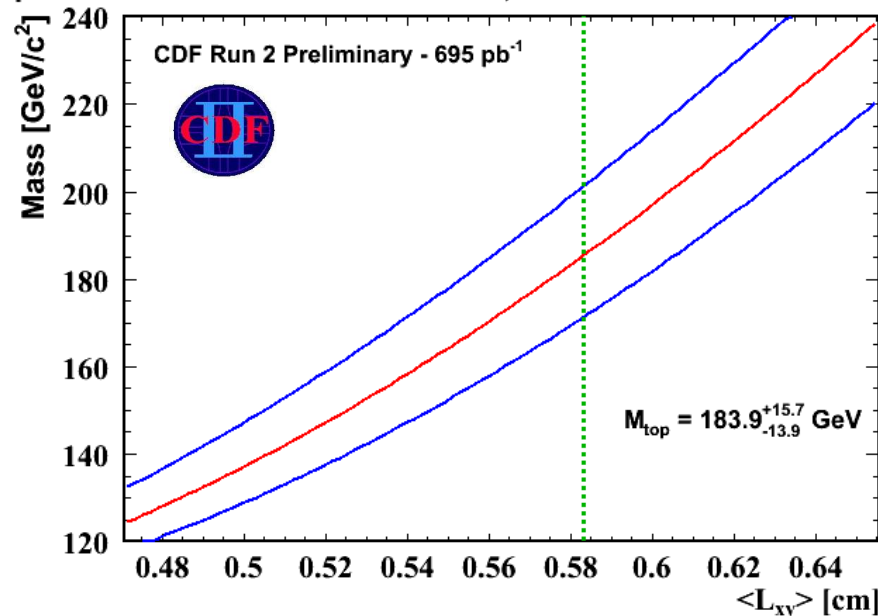
$$m_t = 183.9^{+15.7}_{-13.9} \text{ (stat.)} \pm 5.6 \text{ (syst.) GeV}$$

- At the Tevatron, where top pairs are produced approximately at rest, the boost given to the b-quark is correlated to the top mass:

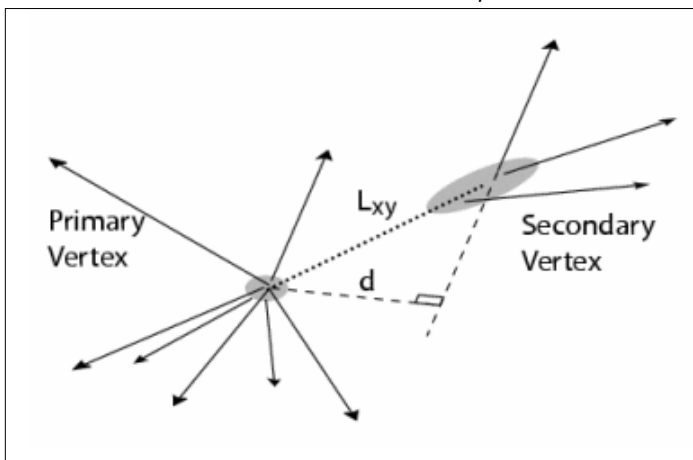
$$\gamma_b = \frac{m_t^2 + m_b^2 - m_W^2}{2m_t m_b} \approx 0.4 \frac{m_t}{m_b}$$

- boost  $\rightarrow$  avg. lifetime  $\rightarrow$  avg. transv. decay-length
- With current statistics, this method is not competitive to other measurements yet
- no jet energy scale uncertainty, as the method relies purely on tracking
- Uncorrelated with other measurements

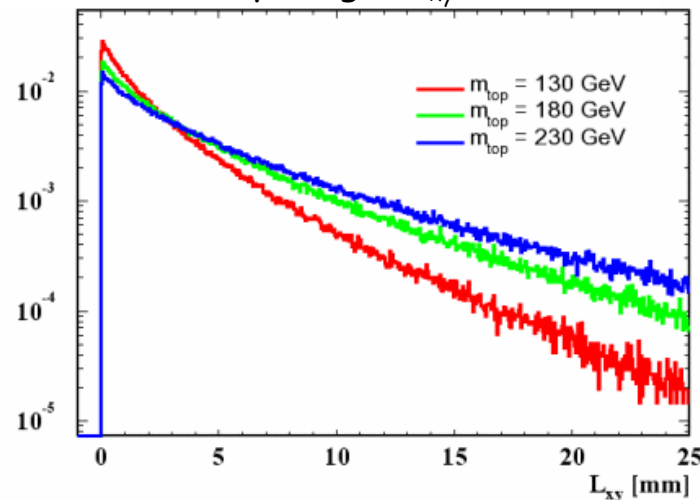
Top Mass  $1\sigma$  Confidence Intervals - Measured  $\langle L_{xy} \rangle$  Overlaid



Transverse Decay Length  $L_{xy}$ : Definition



Transverse Decay Length  $L_{xy}$  in MC





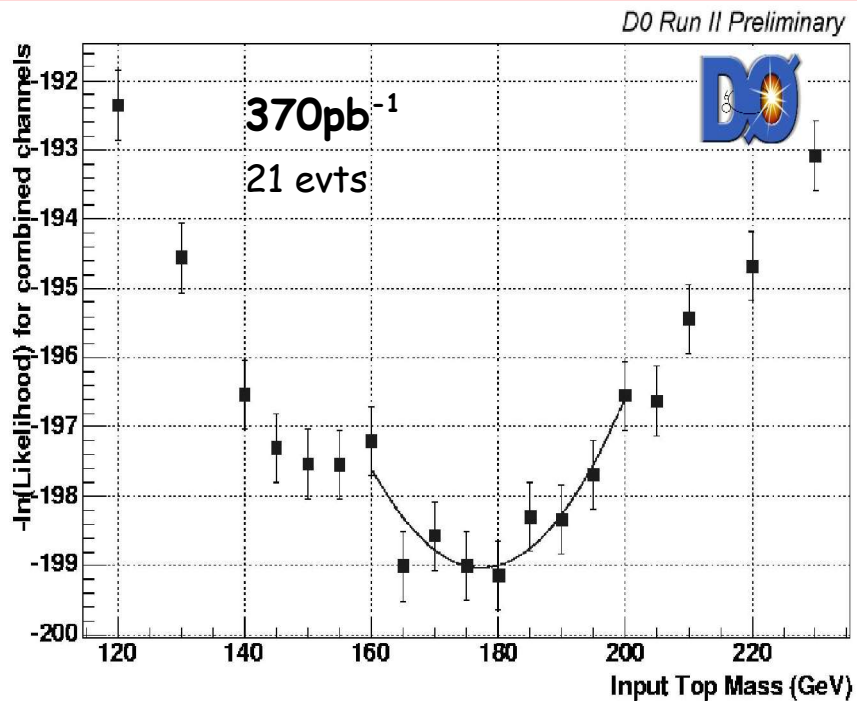
# DØ: Dilepton Analyses



## Neutrino Weighting Analysis

- Underconstrained kinematic fit
- Assume  $\eta$  distribution of neutrinos from MC
- Compute weights for each event,  $m_{\tau}$
- Compare **weight distribution** in data with MC templates

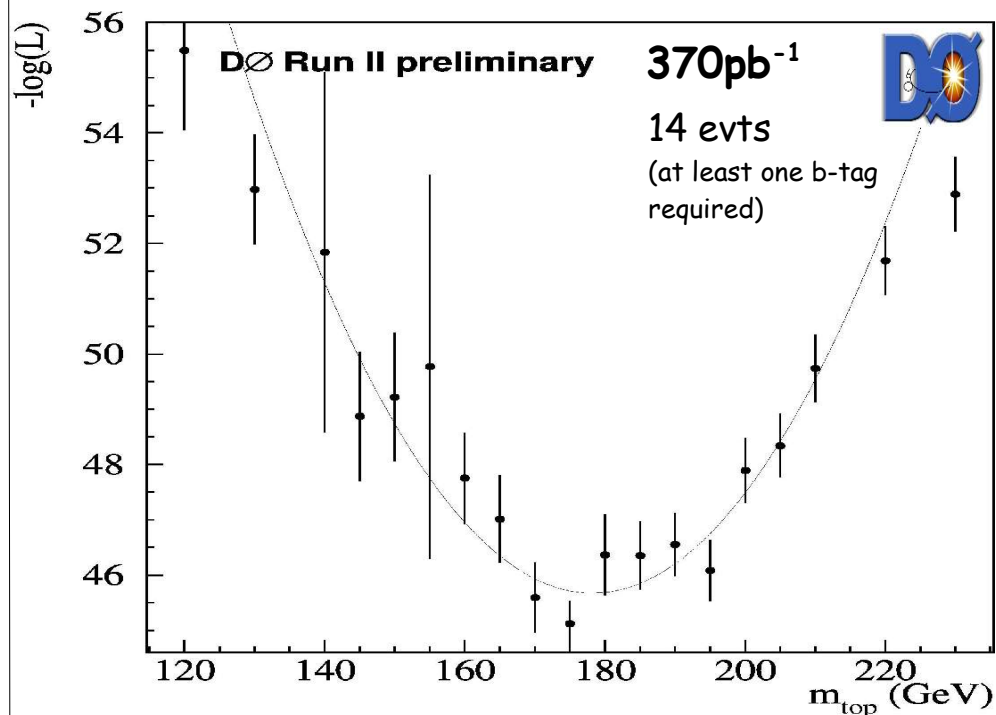
$$m_{\tau} = 175.6 \pm 10.7 \text{ (stat.)} \pm 6.0 \text{ (syst.) GeV}$$



## Matrix Weighting Analysis

- Use Matrix Element prediction and  $m_{\tau}$  to compute event weights
- For each event, choose  $m_{\tau}$  at the peak of the weight distribution
- Compare  **$m_{\tau}$  distribution** with MC templates

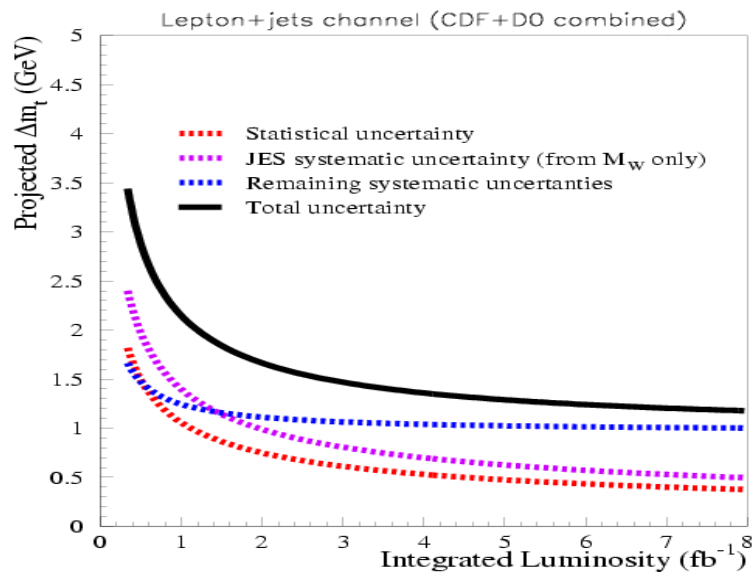
$$m_{\tau} = 176.6 \pm 11.2 \text{ (stat.)} \pm 3.8 \text{ (syst.) GeV}$$



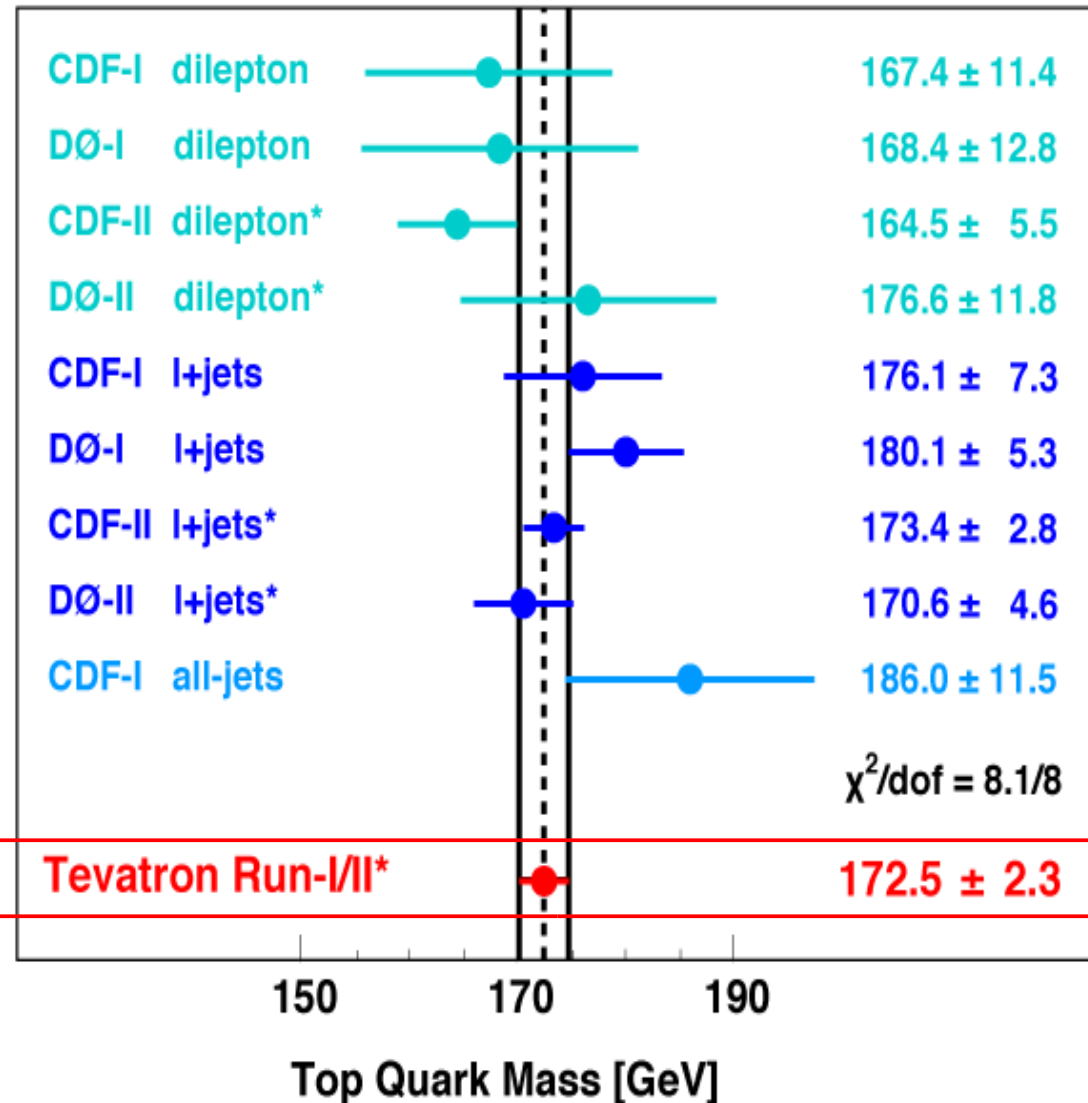
## World Average:

$$m_{\text{t}} = 172.5 \pm 1.3 \text{ (stat)} \pm 1.9 \text{ (syst)} \text{ GeV}$$

- Systematics limited!
- Precision Measurement:  $\Delta m_{\text{t}} \sim 1.3\%$
- In the  $4\text{-}8\text{fb}^{-1}$  future, we expect ...
  - ...  $\sim 1.5 \text{ GeV}$  total error
  - ... dilepton to become systematics limited
  - ... **all-hadronic** measurements to contribute significantly



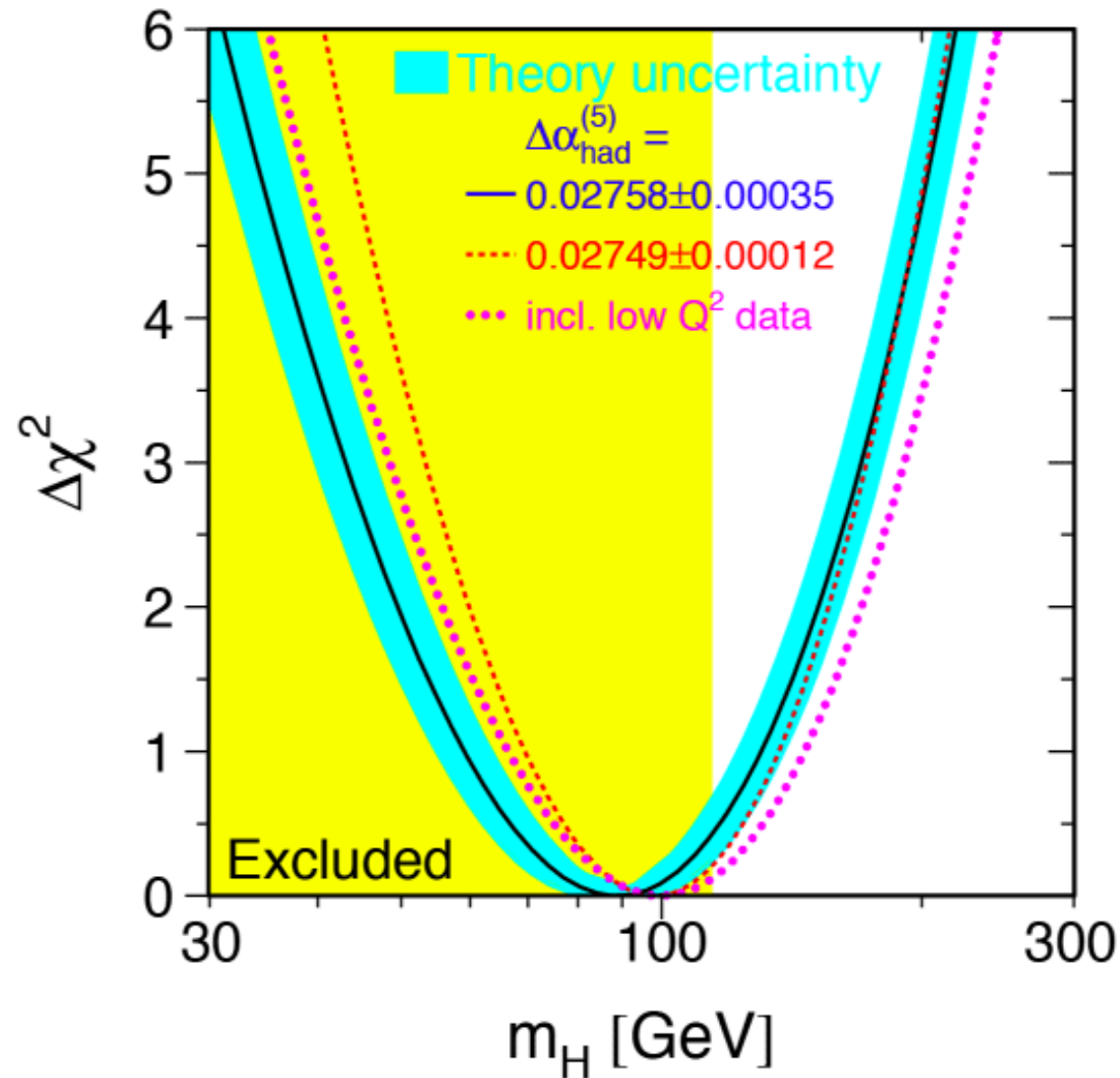
## Best Independent Measurements of the Mass of the Top Quark (\*=Preliminary)



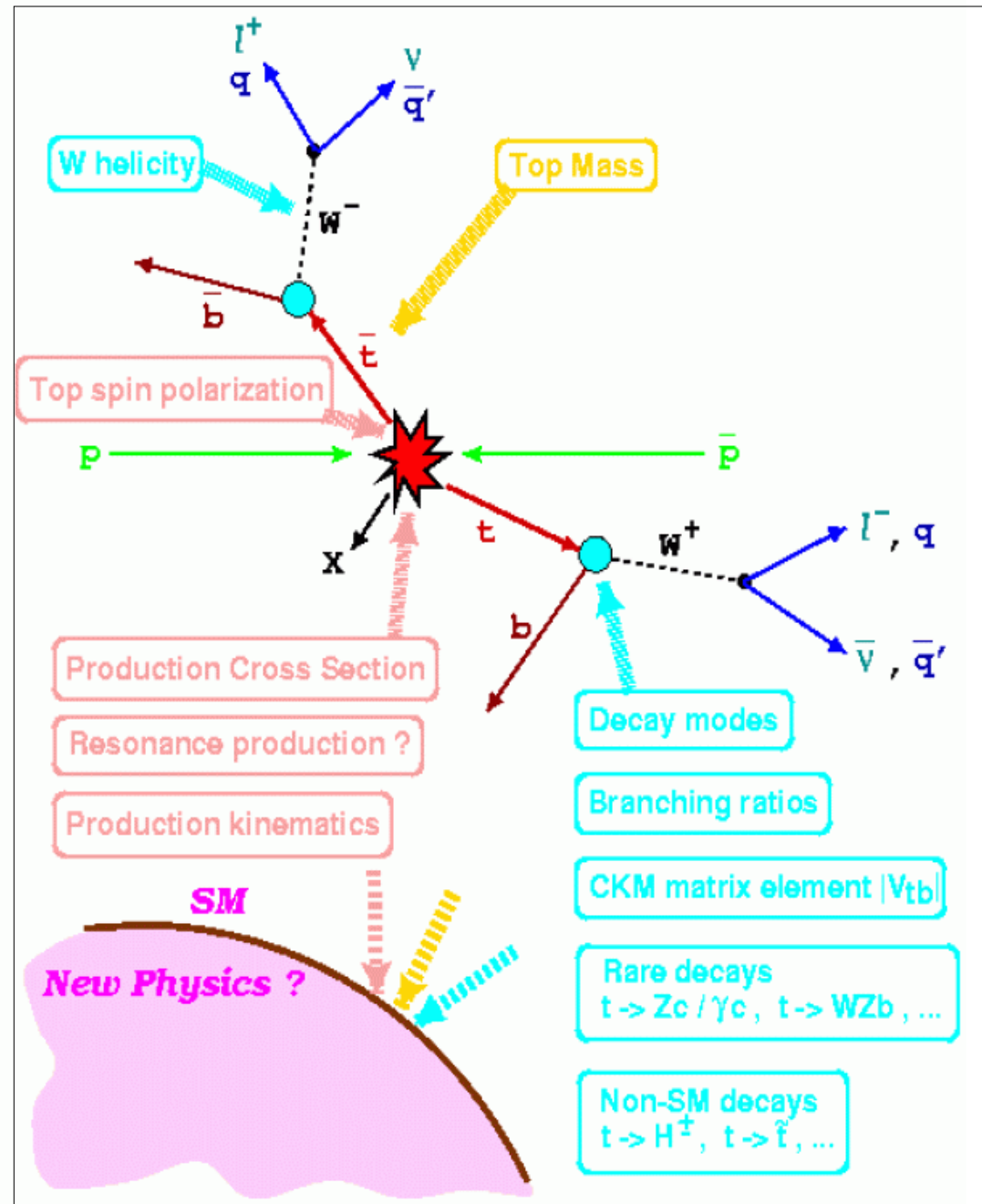


$$M_{\text{Higgs}} = 89^{+42}_{-30} \text{ GeV}$$

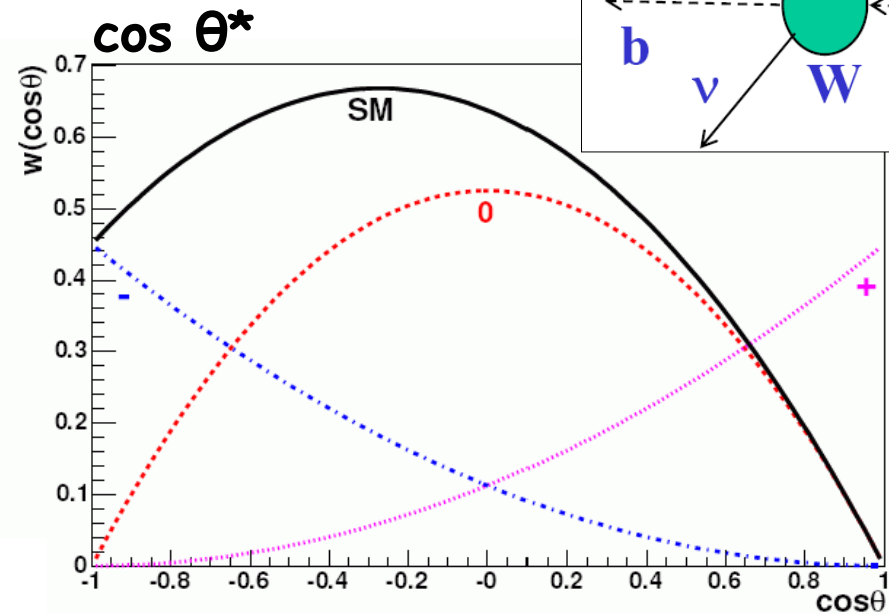
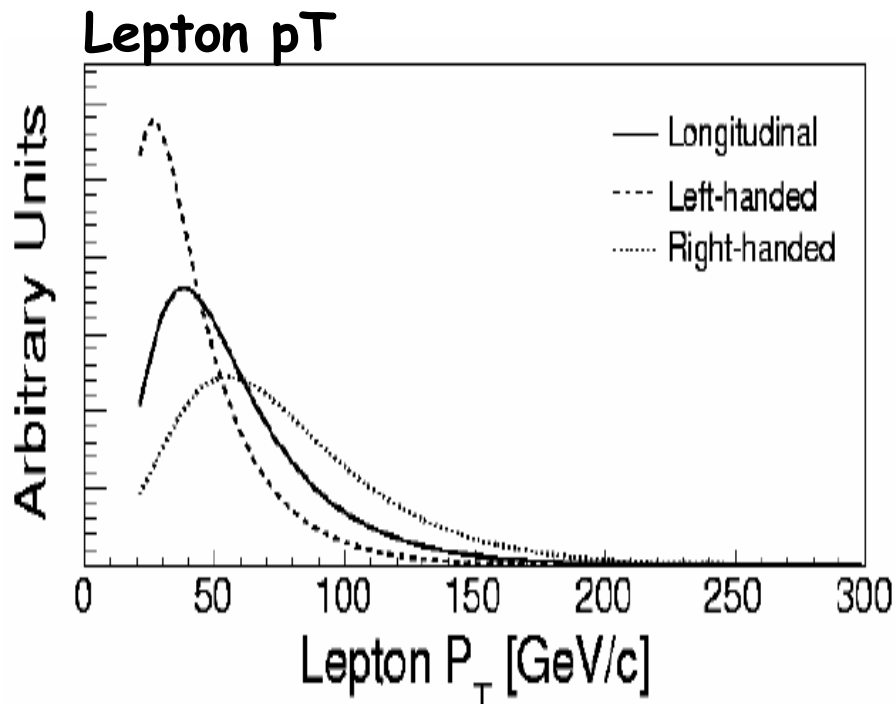
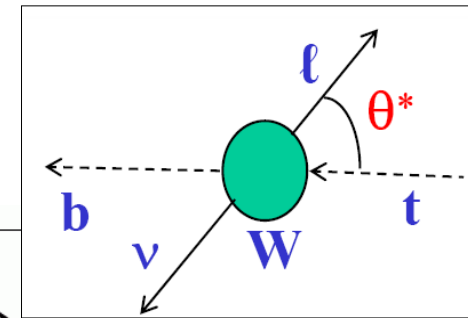
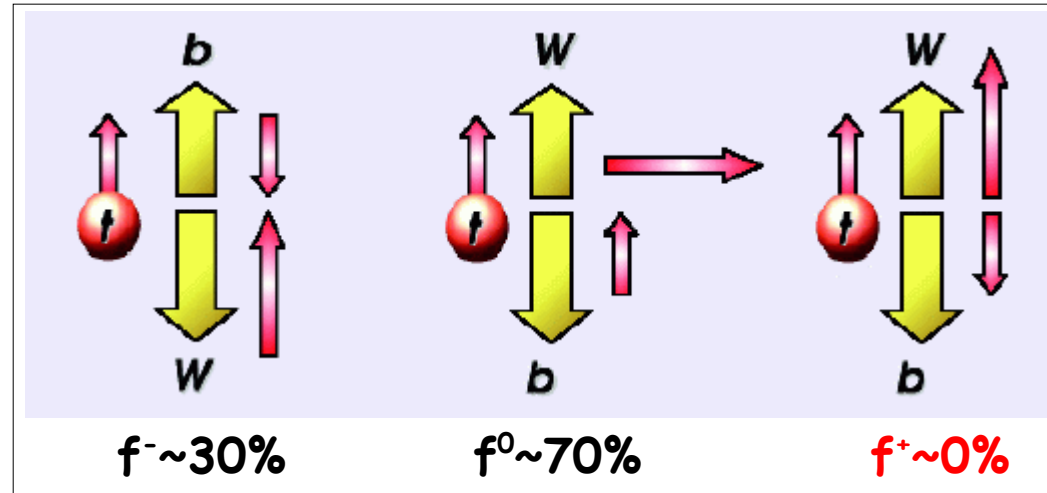
$M_{\text{Higgs}} < 175 \text{ GeV}$  (95% conf.)  
(207 GeV including LEP2)



- top pair decays offer countless opportunities for Standard Model tests
- Many of the top quark properties are just about to become accessible with Tevatron statistics
- Lots of room for exotic behavior
- The following slides show the latest measurements of
  - W Boson Helicity
  - Top Charge
  - Search for  $t\bar{t}$  resonances



- Standard Model: right-handed W from  $t \rightarrow Wb$  suppressed by V-A coupling,  $f^+ \sim 0\%$
- $f^+ > 0$  clear signature for non-SM physics
- Experimentally accessible via:
  - **Lepton  $p_T$** : Charged lepton from a right-handed W preferentially emitted along W boson direction, therefore larger  $p_T$
  - **$\cos \theta^*$** : angle between charged lepton and top quark in the W boson rest frame



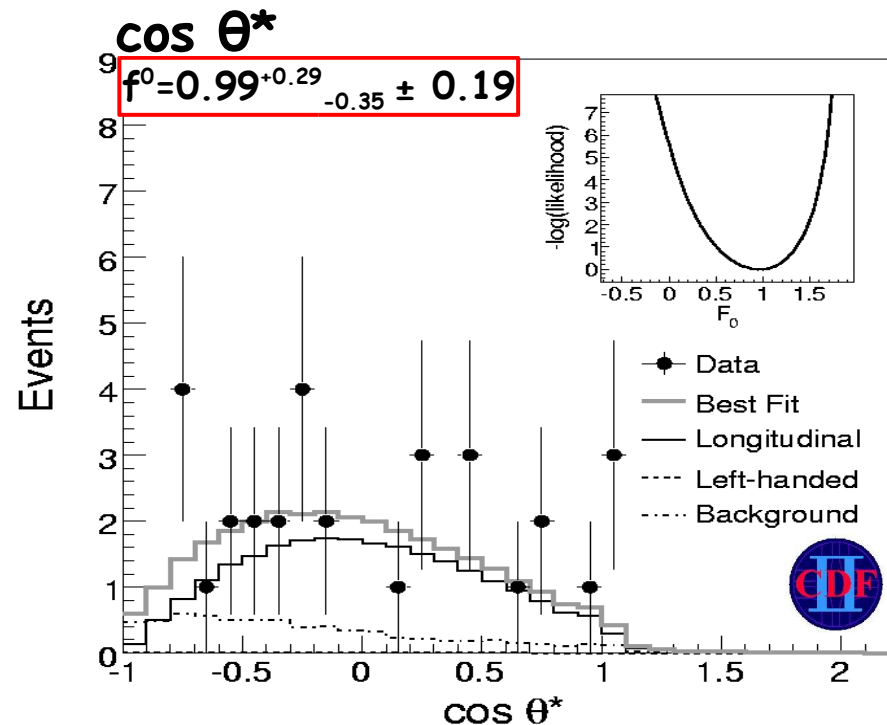
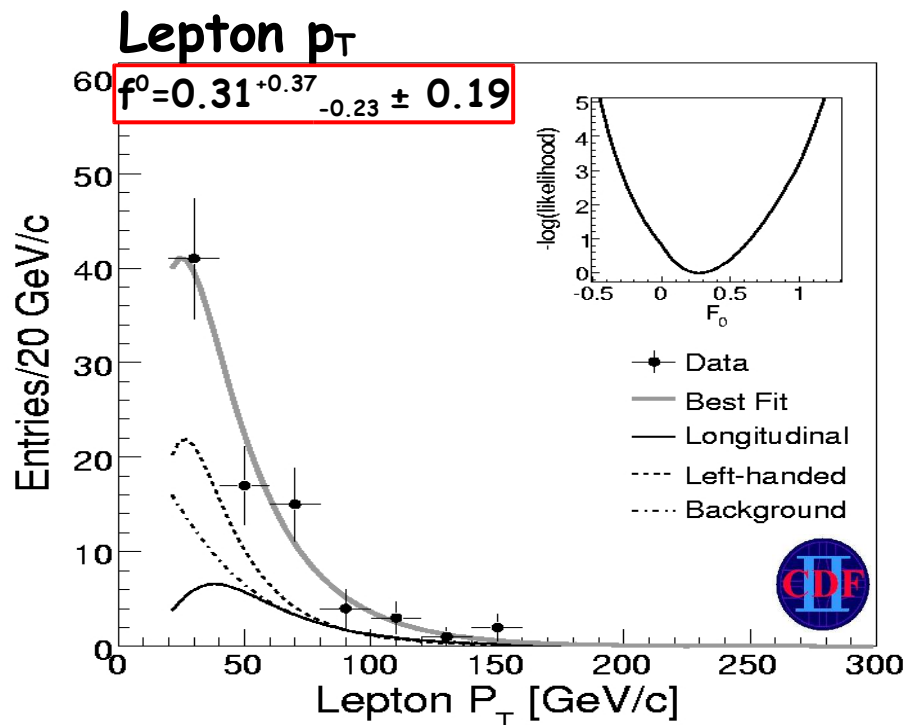
- Lepton  $p_T$  Analysis:
  - Dilepton and lepton+jets events
  - Lepton+Jets: at least 3 jets
- $\cos \theta^*$  Analysis:
  - Subsample of Lepton  $p_T$  lepton+jets sample, requiring at least 4 jets
- At least one b-tagged jet required in lepton+jets (secondary vertex tag)

Combined Results:

$$f^0 = 0.74^{+0.22}_{-0.34} \quad f^+ = 0.00^{+0.20}_{-0.19}$$

**$f^+ < 0.27$  @95% C.L.**

In agreement with SM prediction



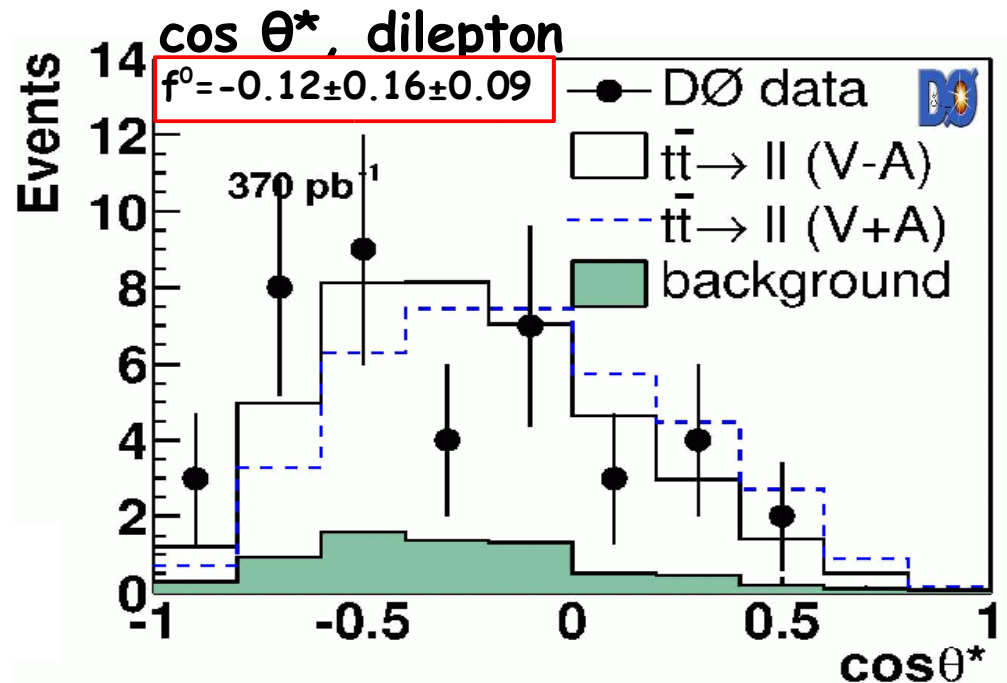
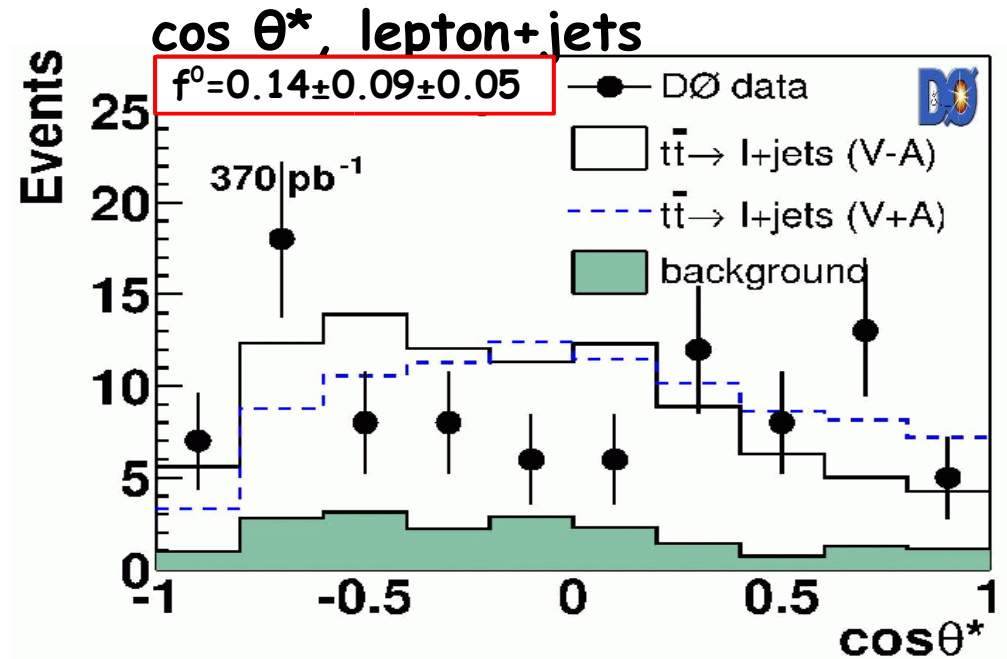
Combined Result:

$$f^+ = 0.08 \pm 0.08_{\text{stat}} \pm 0.06_{\text{syst}}$$

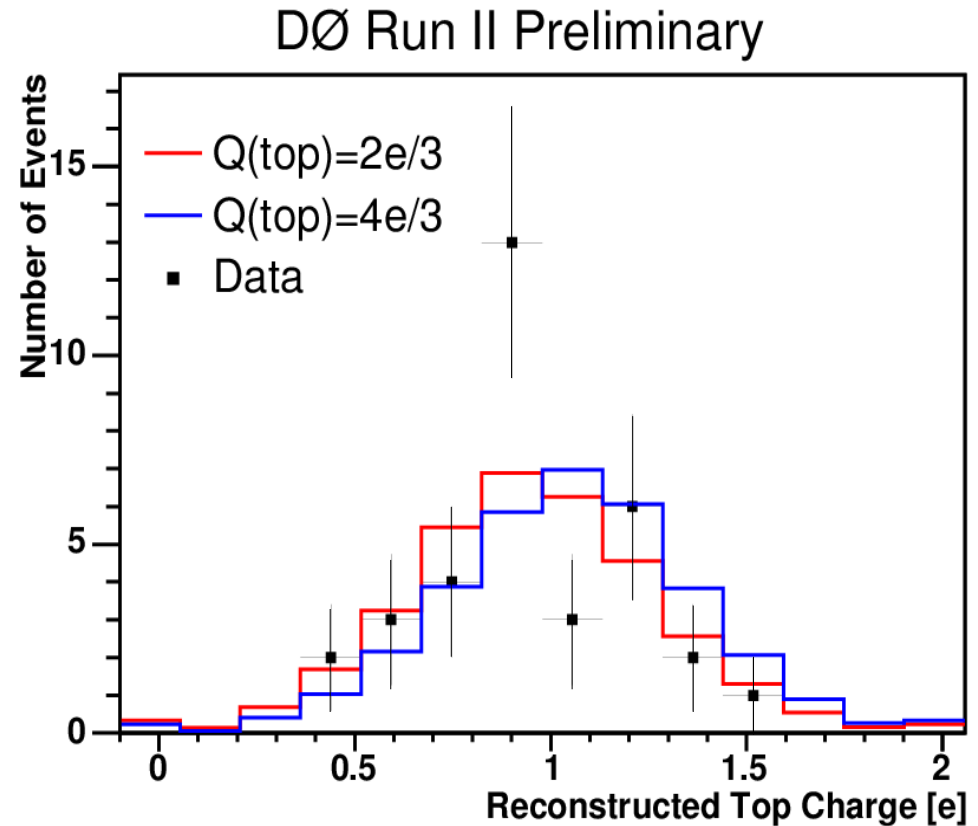
$$f^+ < 0.24 \text{ @95\%C.L.}$$

In agreement with SM prediction

- Use topological likelihood discriminant to select top pair enriched sample
- Use kinematic fit to reconstruct top pair and W boson rest frame
- Fit  $\cos \theta^*$  distributions with Monte Carlo templates, varying  $f^0$  from 0.0 to 0.3
- Extract  $f^0$  using binned likelihood technique



- Standard Model (SM):  $Q_{\top}=2/3e$
- Interpretation  $Q_{\top}=-4/3e$  possible as well
- lepton+jets selection, requiring 2 b-tagged jets (secondary vertex tag).  $\sim 95\%$  top pairs.
- Use kinematic fit to reconstruct top pairs
  - Correct  $t \rightarrow Wb$  assignment:  $\sim 78\%$ .
- Measure the jet-charge of the tagged jets to discriminate between  $b$  and  $\bar{b}$ , using tracks associated with each jet:
 
$$q_{jet} = \frac{\sum_i q_i \cdot p_{T_i}^{0.6}}{\sum_i p_{T_i}^{0.6}}$$
- Two measurements per event:
  - (1) lepton charge plus associated b-jet charge
  - (2) other b-jet charge minus lepton charge
- Construct  $Q_{\top}=2/3e$  and  $Q_{\top}=-4/3e$  templates and compare to top charge distribution derived from data



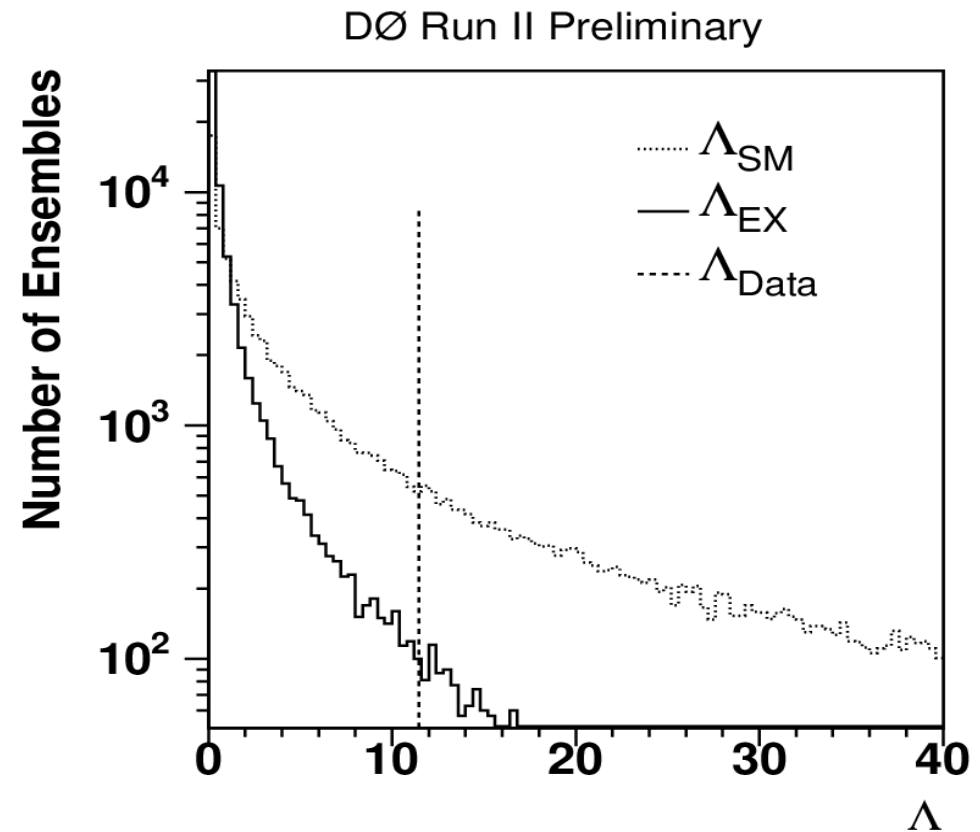
- To test the Standard Model, a likelihood ratio  $\Lambda$  is computed:

$$\Lambda = \frac{\prod_i p^{\text{SM}}(q_i)}{\prod_i p^{\text{EX}}(q_i)}$$

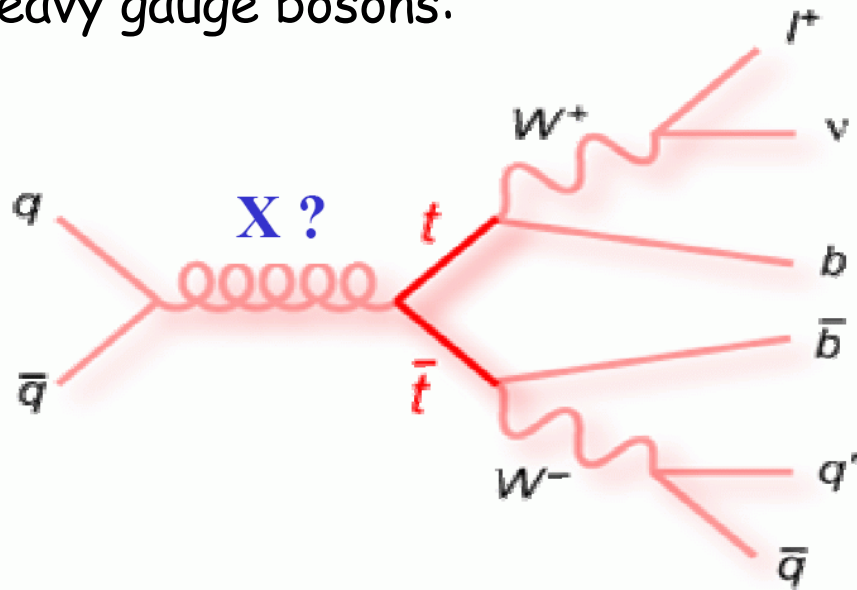
with

- $p^{\text{SM}}(q_i)$  = probability of charge  $q_i$  being observed for  $Q_{\top}=2/3e$  (SM)
- $p^{\text{EX}}(q_i)$  = probability of charge  $q_i$  being observed for  $Q_{\top}=-4/3e$  (EX=exotic models)
- The expected distributions of  $\Lambda$  are derived in Monte Carlo ensemble tests for both scenarios
- The data sample yields  $\Lambda=11.5$  (dashed line)

$Q_{\top}=-4/3e$  excluded @94% C.L.



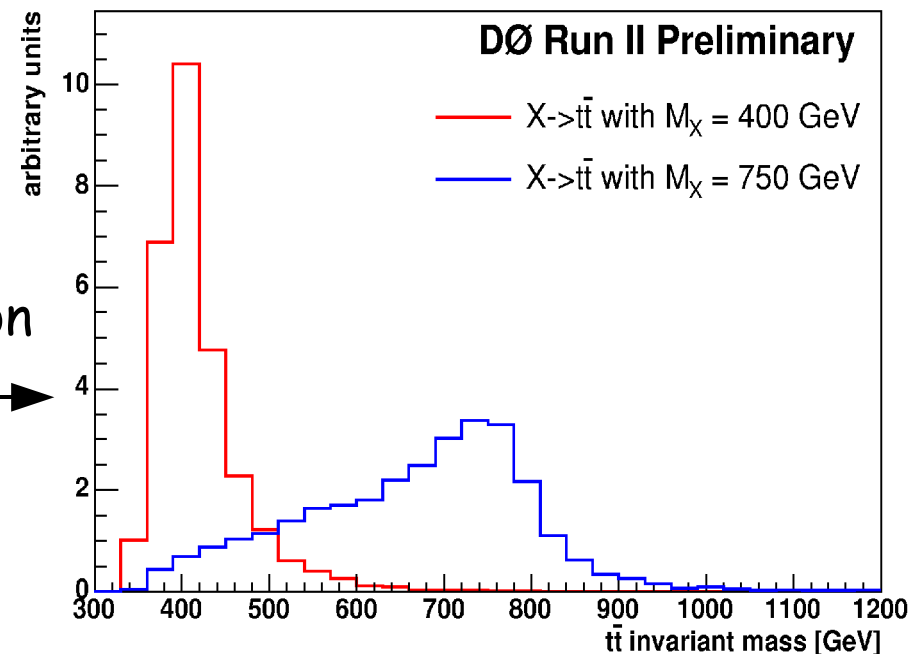
Exotic models predict top pair production through the decay of new heavy gauge bosons:



- Assume resonance mass  $M_X$  in the range [350-1000] GeV
- Assume resonance width  $\Gamma_X = 0.012 \cdot M_X$

Consequences:

- cross-section higher than SM expectation
- resonances in the  $t\bar{t}$  invariant mass distribution →





## CDF:

- lepton+jets selection, no b-tagging requirements
- top quarks reconstructed with matrix element method

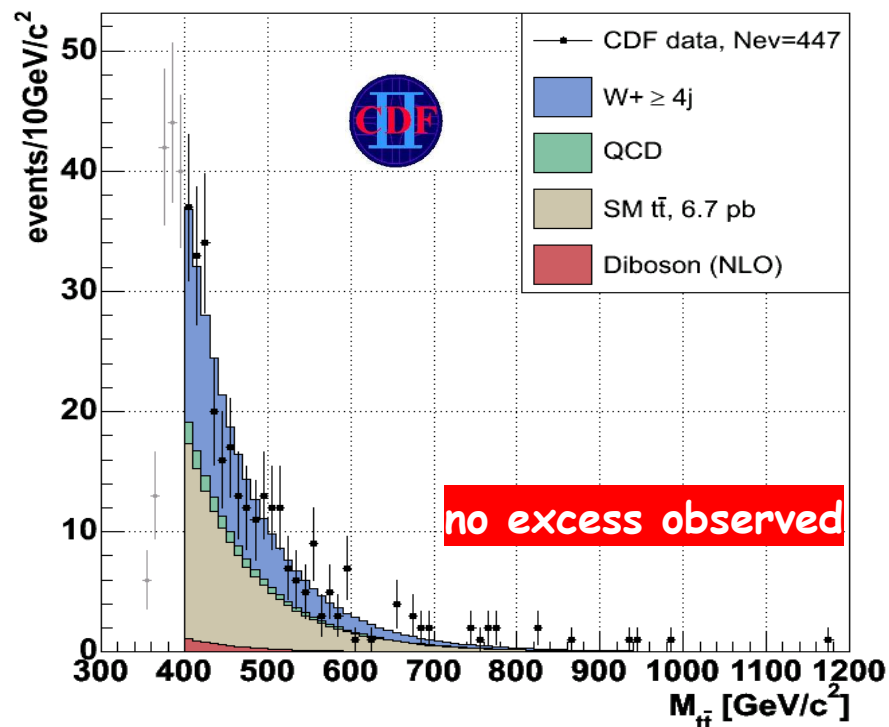
## DØ:

- lepton+jets selection, at least one b-tagged jet (secondary vertex tag)
- top quarks reconstructed with constrained kinematic fit

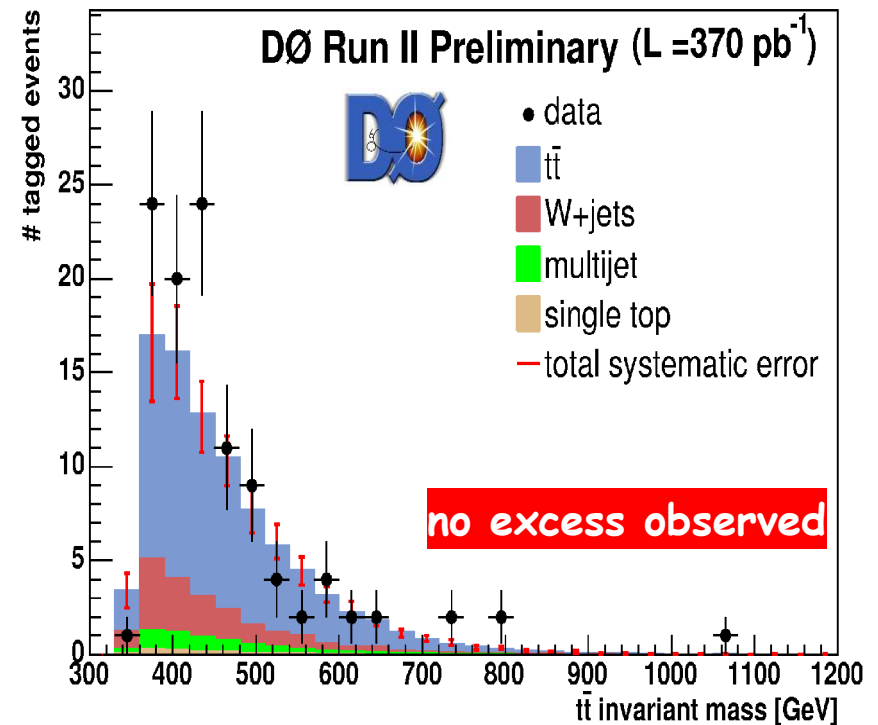
Limits on production of leptophobic  $Z'$ :

$M_x > 725 \text{ GeV @95\% C.L.}$

CDF Run 2 preliminary,  $L=682\text{pb}^{-1}$



$M_x > 680 \text{ GeV @95\% C.L.}$



- Top Mass Measurements at the Tevatron have entered high precision era:
  - Combination of results yields current world average:

$$m_t = 172.5 \pm 2.3 \text{ GeV}$$

- Expect total error  $\Delta m_t \sim 1.5 \text{ GeV}$  with full RunII sample (4-8fb<sup>-1</sup>)
  - These results will be relevant for years, even after LHC startup
- Tevatron Collaborations are zooming in on the top quark's other properties
  - Current measurements show good agreement with the Standard Model
  - Application to a larger dataset ( $\sim 1\text{fb}^{-1}$ ) forecasts interesting results for **this summer** with significantly improved sensitivity to potential non-SM physics