

# Infrared safe definition of jet flavour

Gavin P. Salam

(in collaboration with Andrea Banfi & Giulia Zanderighi)

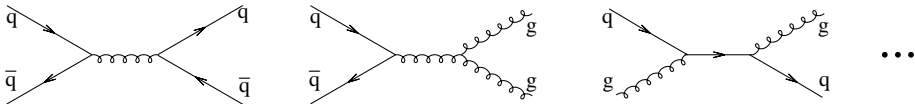
LPTHE, Universities of Paris VI and VII and CNRS

DIS 2006, Tsukuba, Japan

20 April 2006

QCD processes at hadron colliders involve many possible subprocesses.

E.g. dijet production:

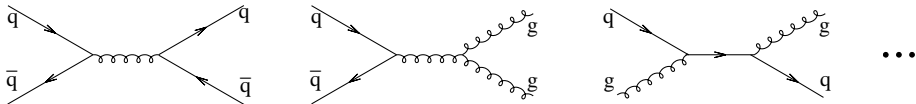


*Want to be able to discuss decomposition into subprocesses, beyond LO*

- To attribute more physical meaning to higher-order calculations  
e.g. which subprocesses get largest corrections
- To know relative numbers of quark v. gluon jets  
e.g. for multiplicity studies, Monte Carlo tuning
- When matching multi-leg calculations with Monte Carlo showering  
e.g. CKKW, Nagy-Soper NLO+showers
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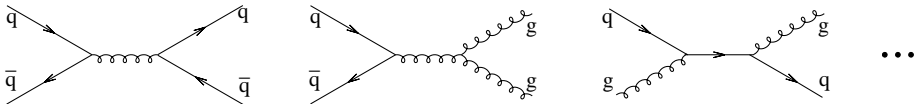


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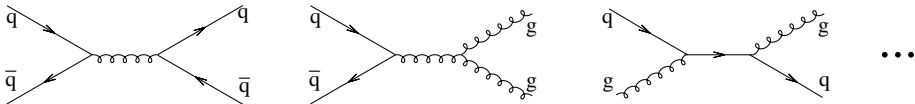


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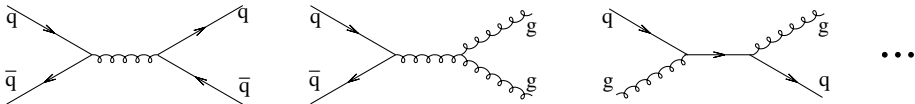


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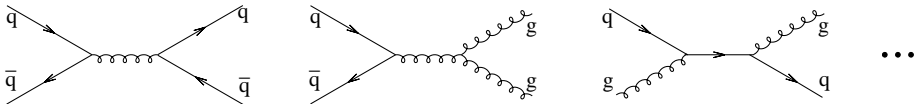


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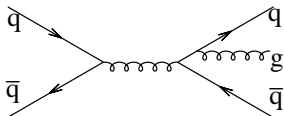
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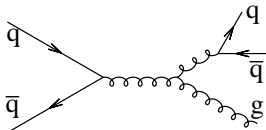
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Correction to  $q\bar{q} \rightarrow q\bar{q}$ ?



Correction to  $q\bar{q} \rightarrow gg$ ?

I.e. assignment to unique  $2 \rightarrow 2$  channel is *impossible* (e.g. the two diagrams interfere in squared amplitude).

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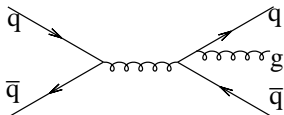
Cluster event into jets, channel defined according to number of jets with 'quark-flavour' v. 'gluon-flavour'

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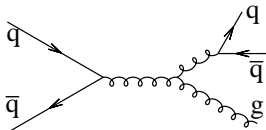
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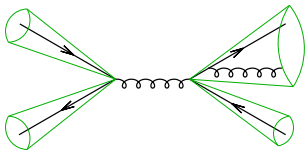
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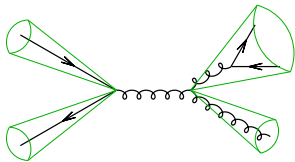
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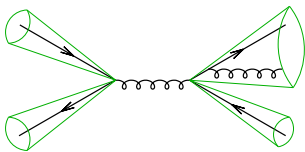
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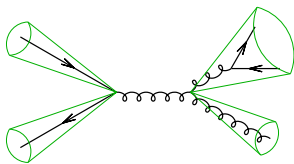
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[one initiated by a hard quark resp. gluon]

But with normal jet algorithms ( $k_t$ , cone), sum of flavours of partons in jet is *infrared unsafe*:

- Soft gluon  $\rightarrow$  large angle  $q\bar{q}$  is clustered into different jets and *contaminates* jet flavour.

Can the jet flavour be made infrared safe?

Feynman alleged to have said “no” (but we haven't found ref.)

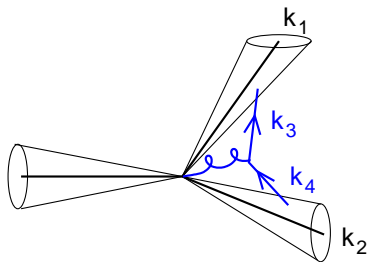
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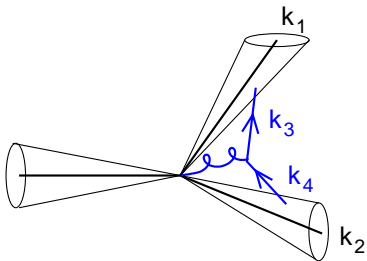
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$k_t$  algorithm clusters closest pair of particles, next closest pair, etc.

cf. talk by Cacciari

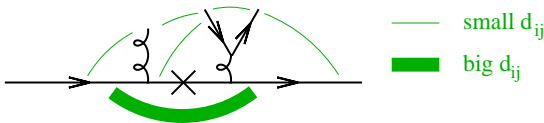
Key issue is *distance measure*:

$$d_{ij}^{(k_t)} = 2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij}),$$

This is a logical generic choice because of structure of divergences in gluon emission:

$$[dk_j] |M_{g \rightarrow g_i g_j}^2(k_j)| \simeq \frac{\alpha_s C_A}{\pi} \frac{dE_j}{\min(E_i, E_j)} \frac{d\theta_{ij}^2}{\theta_{ij}^2}, \quad (E_j \ll E_i, \theta_{ij} \ll 1).$$

For each divergent limit,  $E_j \rightarrow 0$ ,  $\theta_{ij} \rightarrow 0$ , distance vanishes ( $y_{ij} \rightarrow 0$ ).





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- $k_t$  distance does not match divergence structure for quark emission
- fatal** for jet flavour studies because soft large-angle  $q, \bar{q}$  from soft gluon are deemed similarly close to all particles in event

**Solution:** modify distance measure for quarks to reflect divergences

[Banfi, GPS & Zanderighi, hep-ph/0601139]

$$d_{ij}^{(F)} = 2(1 - \cos \theta_{ij}) \times \begin{cases} \max(E_i^2, E_j^2), & \text{softer of } i, j \text{ is quark-like,} \\ \min(E_i^2, E_j^2), & \text{softer of } i, j \text{ is gluon-like,} \end{cases}$$

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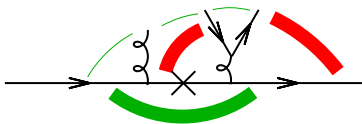
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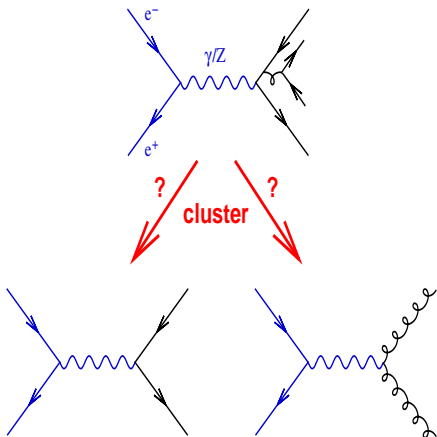
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*Analytical demonstration* of IR safety is *straightforward*.

Can also illustrate it numerically:

- Take  $e^+e^- \rightarrow 2$  jets (has known flavour structure)
- Calculate 3 and 4-parton configurations (with EVENT2)
- Cluster to 2 jets
- As function of  $y_3$  (measure of event hardness) *examine  $\sigma$  for events with mis-flavoured jets* (gluonic, multi-flavoured)

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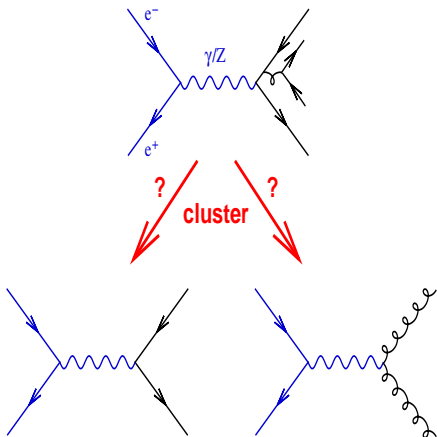
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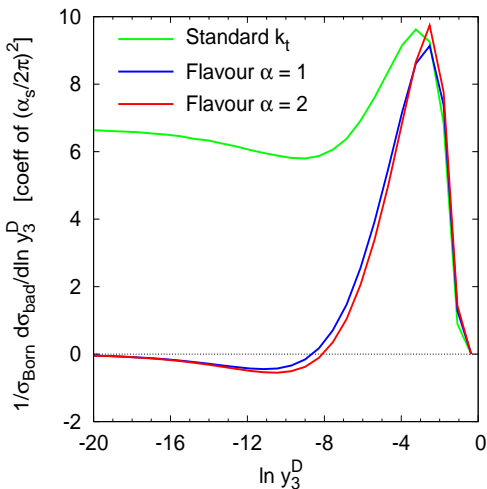
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How can we test it?

- NLO progs for DIS and pp *do not provide flavour info*  
A great shame...
- Instead, stress-test algo. with *parton-shower* events
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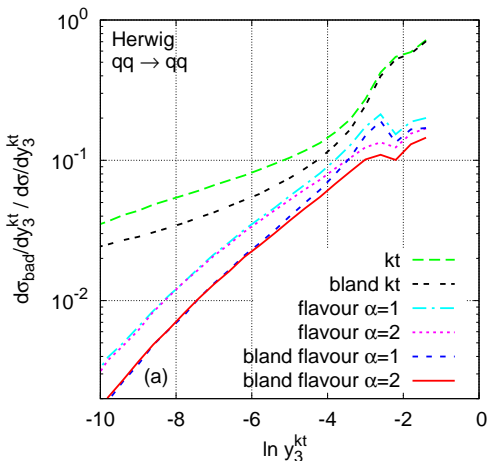


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Can it be done more simply? (Jade?)
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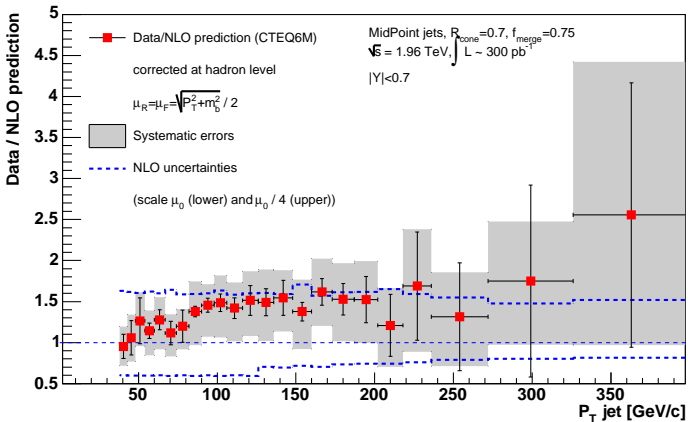
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An important motivation for studying  $b$ -jets was to reduce theory uncertainties.

Frixione & Mangano '96

But in practice NLO uncertainties are very large,  $\sim 40 - 60\%$  (10 - 20% is more usual for NLO).

CDF RunII Preliminary



## Use new jet-flav. algo., but treat only the b-hadrons as quark-like

Must identify all b-hadrons in event — feasible, cf. CDF '04

- Gives physical definition of various b-production channels (flavour excitation, flavour creation, ...) *i.e.* measurable in data, calculable at NLO
- flavour  $b$ -jet cross sections are *free of any  $\ln E_{\perp}/m_b$  enhancements* except those resummed in  $b$  PDFs

Theorem: in the calculation of any IRC safe quantity, quark masses can be neglected (modulo corrections suppressed by powers of  $m_Q/E_T$ ).

- ➡ Can set  $m_b = 0$  in NLO calculations — *i.e.* any light-flavour NLO program could be used to predict  $b$ -jet cross sections
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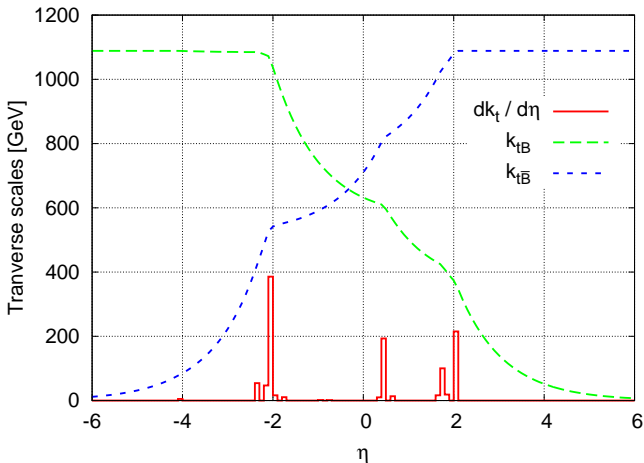
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- ➔ Can perhaps reduce PT uncertainties from current 40 – 60% (heavy  $b$ -jet calcs), down to 10 – 20% (standard light-jet calcs).

$$k_{tB}(\eta) = \sum_i k_{ti} (\Theta(\eta_i - \eta) + \Theta(\eta - \eta_i)e^{\eta_i - \eta}) ,$$

$$k_{t\bar{B}}(\eta) = \sum_i k_{ti} (\Theta(\eta - \eta_i) + \Theta(\eta_i - \eta)e^{\eta - \eta_i}) .$$



# *b*-production sub-processes (preliminary)

