## Infrared safe definition of jet flavour

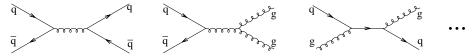
#### Gavin P. Salam (in collaboration with Andrea Banfi & Giulia Zanderighi)

LPTHE, Universities of Paris VI and VII and CNRS

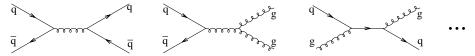
DIS 2006, Tsukuba, Japan 20 April 2006

# Subprocess decomposition

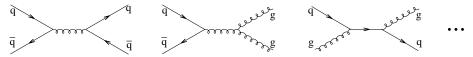
QCD processes at hadron colliders involve many possible subprocesses. E.g. dijet production:



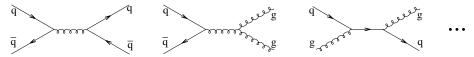
- To attribute more physical meaning to higher-order calculations *e.g.* which subprocesses get largest corrections
- To know relative numbers of quark v. gluon jets
   e.g. for multiplicity studies, Monte Carlo tuning
- When matching multi-leg calculations with Monte Carlo showering e.g. CKKW, Nagy-Soper NLO+showers
- When matching analytical final-state resummations with NLO calculations
   e.g. CAESAR + NLOJET



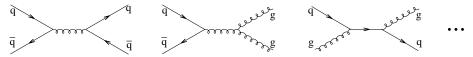
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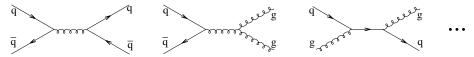
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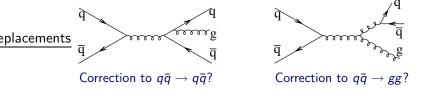


Want to be able to discuss decomposition into subprocesses, beyond LO

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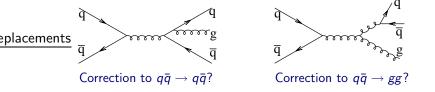


I.e. assignment to unique  $2 \rightarrow 2$  channel is *impossible* (*e.g.* the two diagrams interfere in squared amplitude).

Need a *convention to define channel* beyond LO:

Cluster event into jets, channel defined according to number of jets with 'quark-flavour' v. 'gluon-flavour'

#### e.g. as done in CKKW

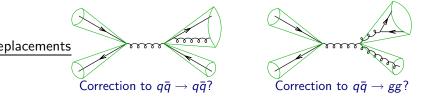


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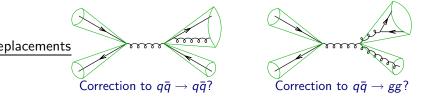


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#### Jet Flavour (p. 4) Quark v. gluon jets

## 376 papers with 'quark/gluon jet' in title

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But with normal jet algorithms ( $k_t$ , cone), sum of flavours of partons in jet is *infrared unsafe*:

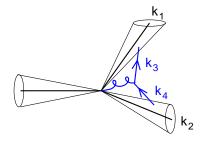
 Soft gluon → large angle qq̄ is clustered into different jets and contaminates jet flavour.

Can the jet flavour be made infrared safe?

Feynman alleged to have said "no" (but we haven't found ref.) ∃ hints of problems in reconciling IR safety and flavour: *e.g.* Nagy & Soper '05 Physical meaning of quark or gluon jet (jet *flavour*) is "obvious". [one initiated by a hard quark resp. gluon]

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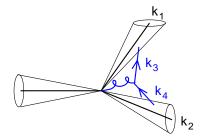


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 $k_t$  algorithm clusters closest pair of particles, next closest pair, etc. cf. talk by Cacciari

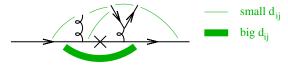
Key issue is *distance measure*:

$$d_{ij}^{(k_t)} = 2\min(E_i^2, E_j^2)\left(1 - \cos\theta_{ij}\right),$$

This is a logical generic choice because of structure of divergences in gluon emission:

$$[dk_j]|M_{g\to g_ig_j}^2(k_j)|\simeq \frac{\alpha_s C_A}{\pi} \frac{dE_j}{\min(E_i,E_j)} \frac{d\theta_{ij}^2}{\theta_{ij}^2}, \qquad (E_j\ll E_i, \ \theta_{ij}\ll 1).$$

For each divergent limit,  $E_j \rightarrow 0$ ,  $\theta_{ij} \rightarrow 0$ , distance vanishes  $(y_{ij} \rightarrow 0)$ .



Quark production only has collinear divergence, but no soft divergence

$$[dk_j]|M_{g\to q_i\bar{q}_j}^2(k_j)| \simeq \frac{\alpha_s T_R}{2\pi} \frac{dE_j}{\max(E_i, E_j)} \frac{d\theta_{ij}^2}{\theta_{ij}^2}, \qquad (E_j \ll E_i, \ \theta_{ij} \ll 1),$$

- $k_t$  distance does not match divergence structure for quark emission
- *fatal* for jet flavour studies because soft large-angle  $q, \bar{q}$  from soft gluon are deemed similarly close to all particles in event

Solution: modify distance measure for quarks to reflect divergences [Banfi, GPS & Zanderighi, hep-ph/0601139]

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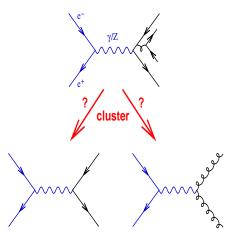
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## Analytical demonstration of IR safety is straightforward.

Can also illustrate it numerically:

- Take e<sup>+</sup>e<sup>-</sup> → 2 jets (has known flavour structure)
- Calculate 3 and 4-parton configurations (with EVENT2)
- Cluster to 2 jets
- As function of y<sub>3</sub> (measure of event hardness) examine σ for events with mis-flavoured jets (gluonic, multi-flavoured)

NB:  $\exists$  class of flavour algos. That shown earlier is  $\alpha = 2$ 



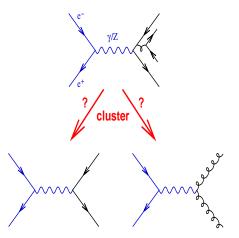
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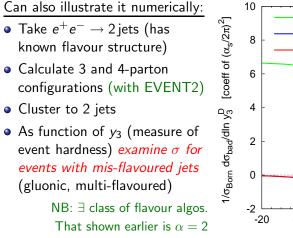
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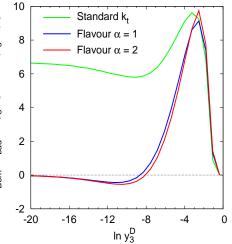
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# Jet flavour at hadron colliders

Extension from  $e^+e^-$  to hadron-collisions requires extra ingredient: *beam* hardness  $k_{tB}(\eta) \equiv$  estimate of DGLAP evolution scale at a given rapidity.

$$d_{iB}^{(F)} = \begin{cases} \max(k_{ti}^2, k_{tB}^2(\eta_i)), & i \text{ is quark-like,} \\ \min(k_{ti}^2, k_{tB}^2(\eta_i)), & i \text{ is gluon-like.} \end{cases}$$

How can we test it?

- NLO progs for DIS and pp do not provide flavour info A great shame...
- Instead, stress-test algo. with parton-shower events
- IR (un)safety ⇔ different scalings with y<sub>3</sub>.
- Require blandness (forbid multi flavoured recomb.), to improve algorithms
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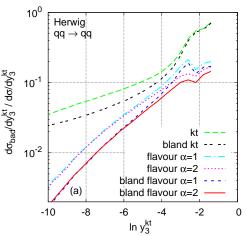
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- Key new idea is different clustering for quarks and gluons

Can it be done more simply? (Jade?)

 Practical use hampered because most NLO codes don't provide access to flavour information
 Could easily be fixed by NLO authors

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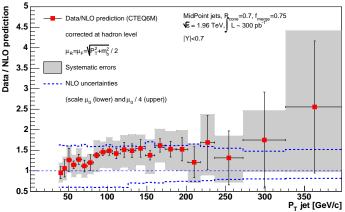
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# Current B-jet measurements

An important motivation for studying *b*-jets was to reduce theory uncertainties. Frixione & Mangano '96

But in practice NLO uncertainties are very large,  $\sim 40-60\%$  (10 - 20% is more usual for NLO).



CDF RunII Preliminary

Must identify all b-hadrons in event — feasible, cf. CDF '04

- Gives physical definition of various b-production channels (flavour excitation, flavour creation, ...) *i.e.* measurable in data, calculable at NLO
- flavour *b*-jet cross sections are *free of any*  $\ln E_{\perp}/m_b$  *enhancements* except those resummed in *b* PDFs

- Can set m<sub>b</sub> = 0 in NLO calculations *i.e. any light-flavour NLO program could be used to predict b-jet cross sections*
- Can perhaps reduce PT uncertainties from current 40 60% (heavy b-jet calcs), down to 10 – 20% (standard light-jet calcs).

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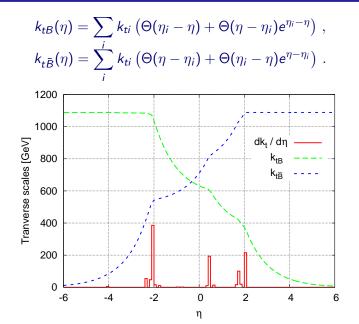
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Jet Flavour (p. 13) Extras Beam scale

## Beam Scale



# b-production sub-processes (preliminary)



