

HYP-X , Tokai, Japan, Sep. 17, 2009

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**$^3\text{He}(\text{in-flight } K^-, n)$  spectrum  
and  
moving pole of a deeply-bound  $K^-pp$  state  
in complex energy plane**

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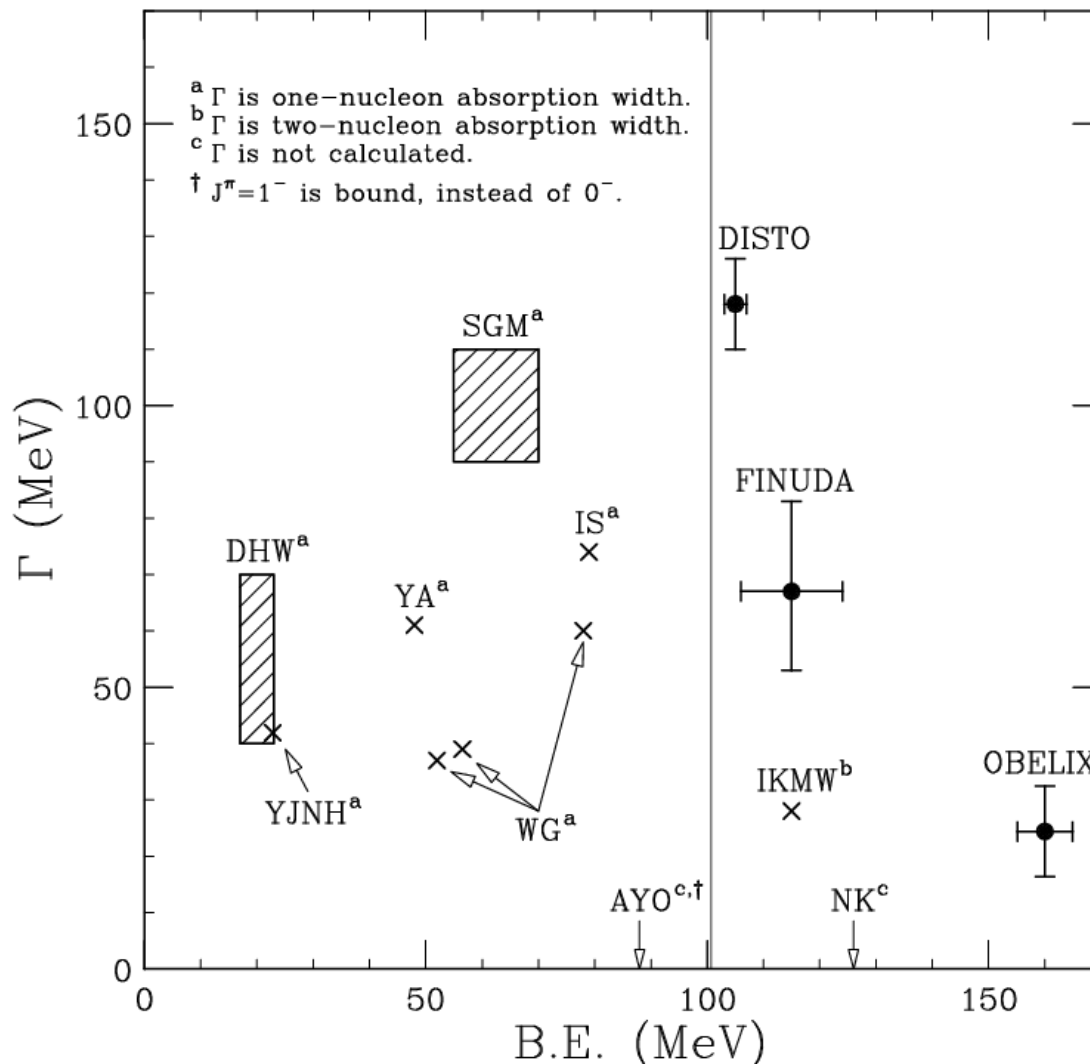
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**Toru Harada**

**Osaka Electro-Communication Univ.**

**“ $K^-pp$ ”** is suggested to be the lightest and most fundamental kaonic nuclei, but the theoretically-calculated and experimentally-measured  $B.E.$  and  $\Gamma$  are not converged!



### Theory

- **YA: Yamazaki, Akaishi**
- **SGM: Shevchenko, Gal, Mares**
- **IS: Ikeda, Sato**
- **DHW: Dote, Hyodo, Weise**
- **IKMW: Ivanov, Kienle *et al.***
- **NK: Nishikawa & Kondo**
- **AYO: Arai, Yasui, Oka**
- **YJNH: Yamagata, Jido *et al.***
- **WG: Wycech, Green,**

### Experiment

- **FINUDA**
- **OBELIX**
- **DISTO**

◆ New measurement for searching “K<sup>-</sup>pp”

★ M. Iwasaki, T. Nagae *et al.* , **J-PARC E15 experiment**

**<sup>3</sup>He(In-flight K<sup>-</sup>, n) “K<sup>-</sup>pp”**  
at  $p_{K^-} = 1 \text{ GeV}/c$  and  $\theta_n = 0^\circ$

missing-mass  
spectroscopy

+

Simultaneous measurement

“K<sup>-</sup>pp”  $\rightarrow \Lambda p \square \pi^- pp$   
detecting all charged particles  
from the decay of “K<sup>-</sup>pp”

invariant-mass  
spectroscopy

Our purpose:

Theoretical calculation of **<sup>3</sup>He(In-flight K<sup>-</sup>, n) inclusive/semi-exclusive spectra** within the DWIA framework using Green’s function method.

◆ **Theoretical calculations of  $^3\text{He}(\text{In-flight } K^-, n)$  reaction spectrum for J-PARC E15 experiment**

▪ **Our approach:**

**Phenomenological optical potential model  
using phase space factor**

**→ Examine a possible evidence for the various cases.**

Refs. T. Koike & T. Harada, Phys. Lett. B652 (2007) 262-268.

T. Koike & T. Harada, Nucl. Phys. A804 (2008) 231-273.

T. Koike & T. Harada, arXiv: 0906.3659 [nucl-th].

▪ **Other approach within a similar framework:**

**Optical potential model based on chiral unitary approach**

Ref. J. Yamagata-Sekihara *et al.*, arXiv: 0812.4359 [nucl-th].

# ◆ Distorted-Wave Impulse Approximation (DWIA)

$$\frac{d^2\sigma}{dE_n d\Omega_n} = \beta \left[ \frac{d\sigma}{d\Omega_n} \right]^{(\text{elem})} S(E)$$

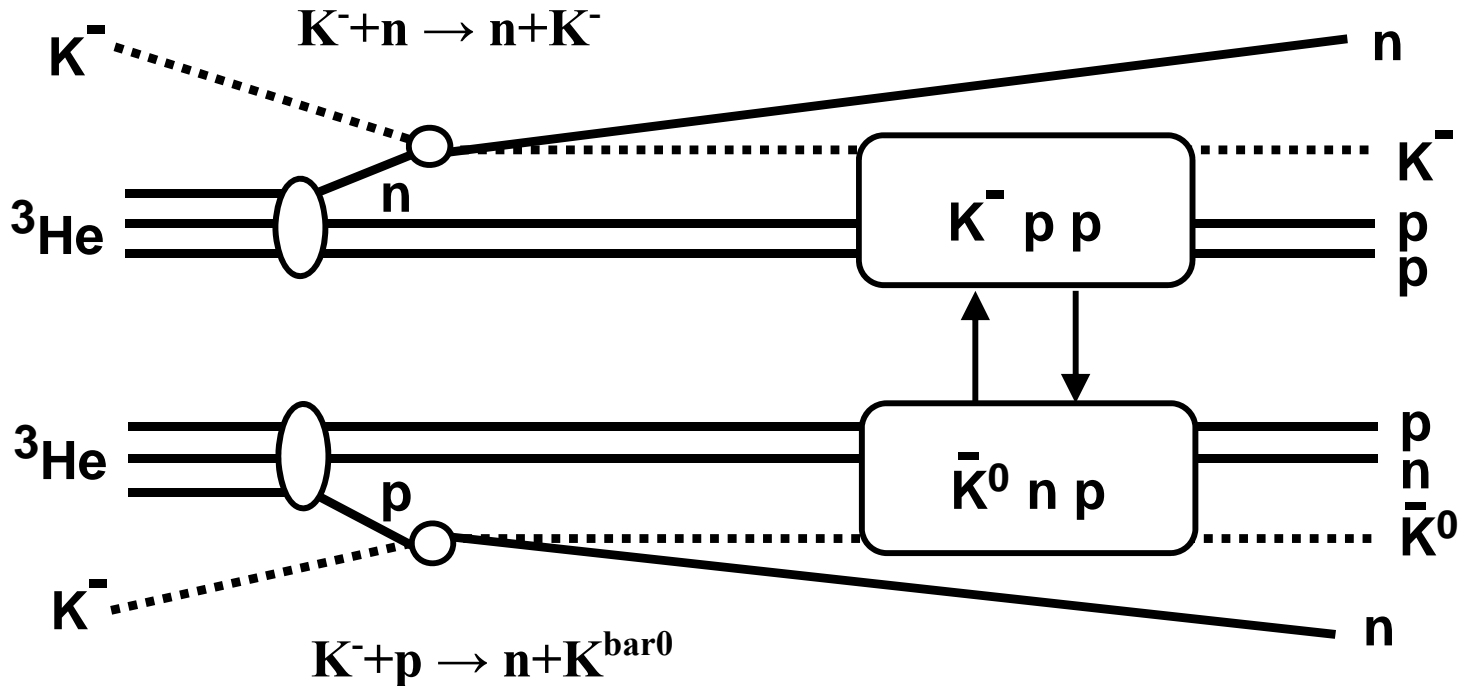
Kinematical factor  $\nearrow$   $\beta$   $\uparrow$  Fermi-averaged elementary cross-section  $\nwarrow$  **Strength function**  
 $\mathbf{K^- + n \rightarrow N + K^{bar}}$  in lab. system

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$$\frac{d^2\sigma}{dE_n d\Omega_n} = \beta \left[ \frac{d\sigma}{d\Omega_n} \right]^{(\text{elem})} S(E)$$

Kinematical factor  $\beta$  ↑ ↑ **Strength function**  
↑ **Fermi-averaged elementary cross-section**  
↑  $K^- + n \rightarrow N + K^{\text{bar}}$  in lab. system

In charge basis,

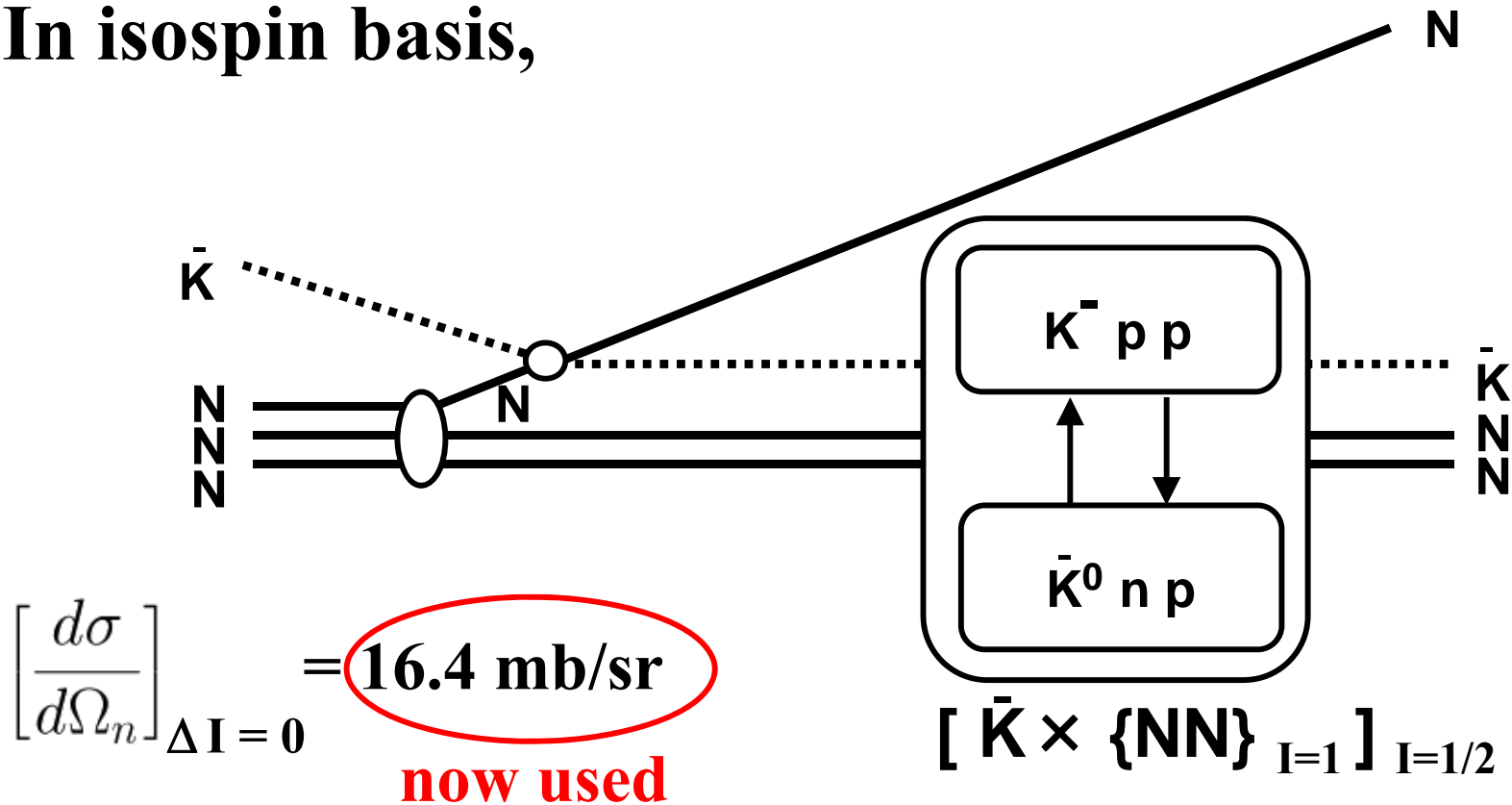


# ◆ Distorted-Wave Impulse Approximation (DWIA)

$$\frac{d^2\sigma}{dE_n d\Omega_n} = \beta \left[ \frac{d\sigma}{d\Omega_n} \right]^{(\text{elem})} S(E)$$

Kinematical factor  $\beta$  Fermi-averaged elementary cross-section Strength function  
 $K^- + n \rightarrow N + K^{\text{bar}}$  in lab. system

In isospin basis,



# ◆ Distorted-Wave Impulse Approximation (DWIA)

$$\frac{d^2\sigma}{dE_n d\Omega_n} = \beta \left[ \frac{d\sigma}{d\Omega_n} \right]^{(\text{elem})} S(E)$$

Kinematical factor  $\beta$   $\nearrow$   $\left[ \frac{d\sigma}{d\Omega_n} \right]^{(\text{elem})}$   $\uparrow$   $S(E)$   
**Fermi-averaged elementary cross-section**  
 $K^- + n \rightarrow N + K^{\text{bar}}$  in lab. system  $\swarrow$  **Strength function**

Morimatsu & Yazaki's Green function method Prog.Part.Nucl.Phys.33(1994)679.

$$S(E) = -\frac{1}{\pi} \text{Im} \left[ \sum_{\alpha, \alpha'} \int d\mathbf{r} d\mathbf{r}' f_{\alpha}(\mathbf{r}) G_{\alpha, \alpha'}(E; \mathbf{r}, \mathbf{r}') f_{\alpha'}(\mathbf{r}') \right]$$

$\uparrow$   
**Green's function  $K^-pp$  system**  
 $\rightarrow$  employing  $K^-$ -“pp” optical potential

$$f_{\alpha}(\mathbf{r}) = \chi^{(-)*} \left( \mathbf{p}_n, \frac{M_{pp}}{M_{3\text{He}}} \mathbf{r} \right) \chi^{(+)} \left( \mathbf{p}_{K^-}, \frac{M_{pp}}{M_{3\text{He}}} \mathbf{r} \right) \langle \alpha | \psi_n(\mathbf{r}) | i \rangle$$

$\nwarrow$  **Distorted wave for**  
**incoming(+)/outgoing(-) particles**  
 $\rightarrow$  Eikonal approximation

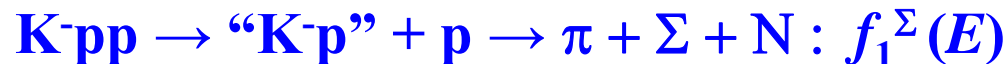
$\uparrow$   
**neutron wave function**  
 $\rightarrow$  (0s)<sup>3</sup> harmonic oscillator model



# ◆ Phenomenological $K^-$ -“pp” optical potential

$$U^{\text{opt}}(E; r) = (V_0 + i W_0 \underline{f(E)}) \exp[-(r/b)^2]$$

## • 1-nucleon $K^-$ absorption

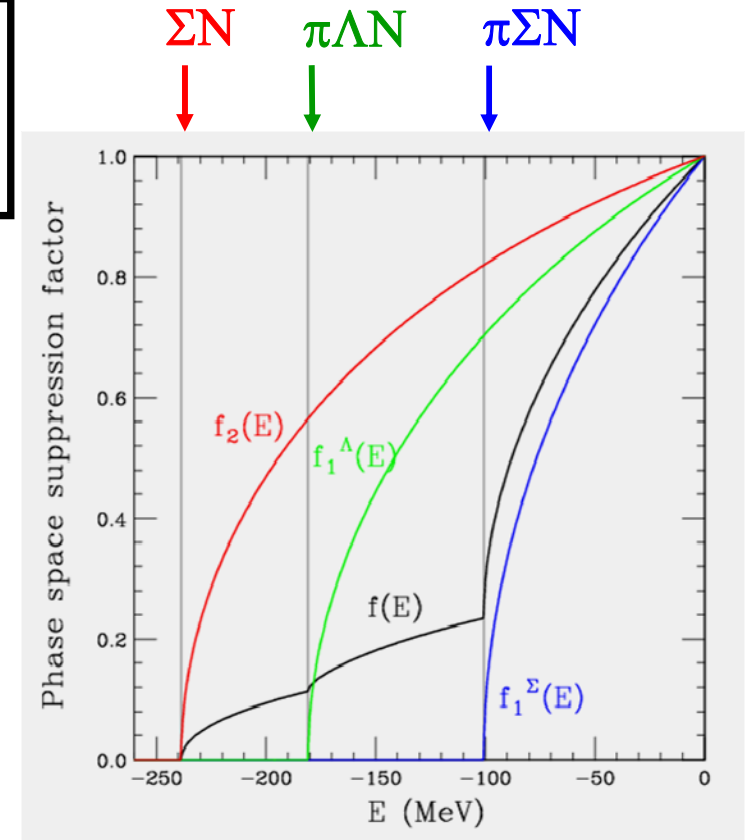


## • 2-nucleon $K^-$ absorption



## • Total phase space factor

$$f(E) = \underbrace{B_1^{(\pi\Sigma N)}}_{= 0.7} f_1^\Sigma(E) + \underbrace{B_1^{(\pi\Lambda N)}}_{= 0.1} f_1^\Lambda(E) + \underbrace{B_2^{(YN)}}_{= 0.2} f_2(E)$$



Refs. J. Mares, E. Friedman, A. Gal, PLB606 (2005) 295.

D. Gazda, E. Friedman, A. Gal and J. Mares, PRC76 (2007) 055204.

J. Yamagata, H. Nagahiro, S. Hirenzaki, PRC74 (2006) 014604.

## ◆ Single-channel Green's function

$$\{(\underbrace{E}_{\text{Real}} - V_{\text{Coul}}(\mathbf{r}))^2 + \nabla^2 - \mu^2 - 2\mu \underline{U^{\text{opt}}(E; \mathbf{r})}\} G(E; \mathbf{r}, \mathbf{r}') = \delta^3(\mathbf{r} - \mathbf{r}'),$$

## ◆ Determining pole position

The Klein-Gordon equation is solved self-consistently in complex  $E$ -plane;

$$\{(\underbrace{\omega(E)}_{\text{Complex}} - V_{\text{Coul}}(\mathbf{r}))^2 + \nabla^2 - \mu^2 - 2\mu \underline{U^{\text{opt}}(E; \mathbf{r})}\} \Phi(E; \mathbf{r}) = 0,$$

$$\longrightarrow \begin{cases} \text{Re } \omega(E) = -B.E. = E, \\ \text{Im } \omega(E) = -\Gamma/2 \end{cases}$$

**$B.E.$  and  $\Gamma$  are determined from these relations.**

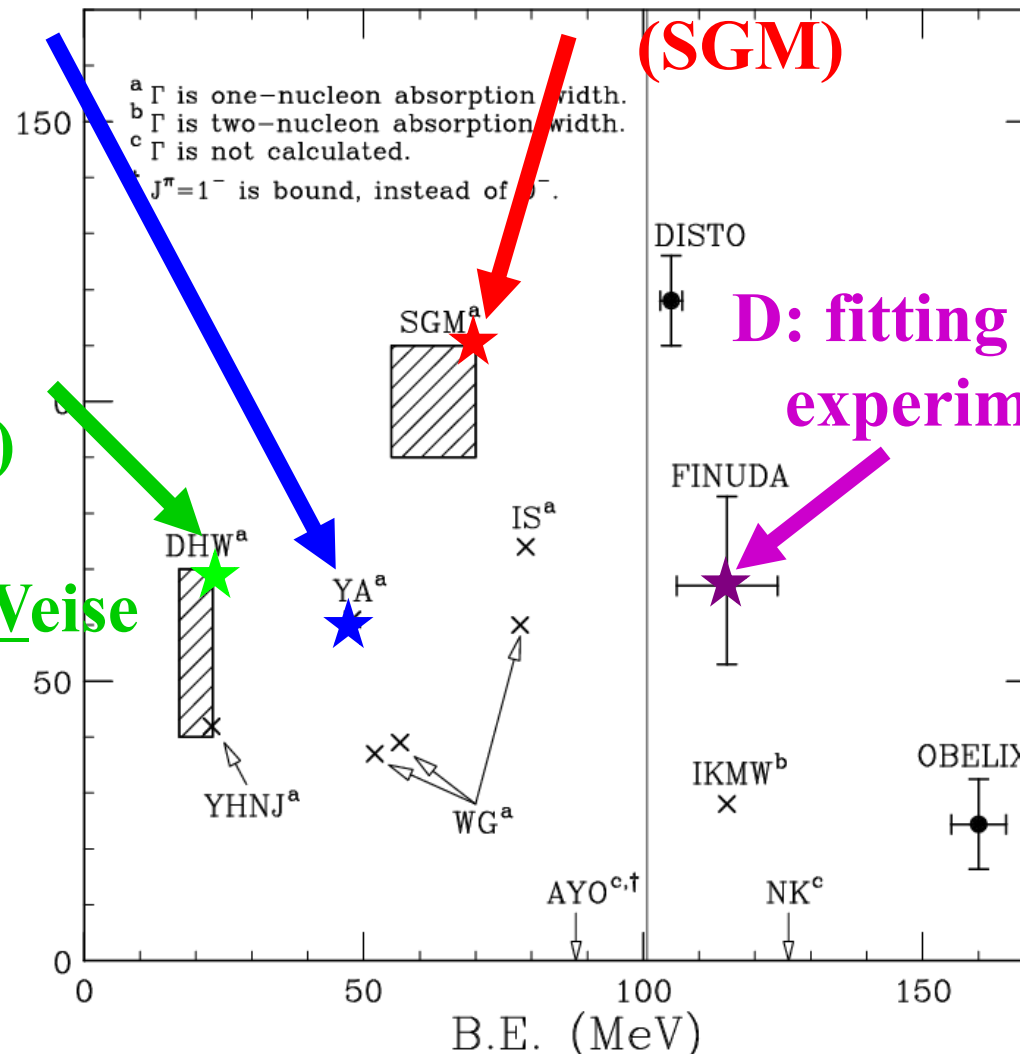
We consider the following 4 cases of the calculations/experiment;

**B:** variational cal. with phenomenological  $K^{\text{bar}}N$  int. by Yamazaki-Akaishi (YA)

**C:** Faddeev cal. with phenomenological  $K^{\text{bar}}N$  int. by Shevchenko-Gal-Mares (SGM)

**A:** variational cal. with Chiral SU(3) based  $K^{\text{bar}}N$  int. by Dote-Hyodo-Weise (DHW)

**D:** fitting to FINUDA experimental data



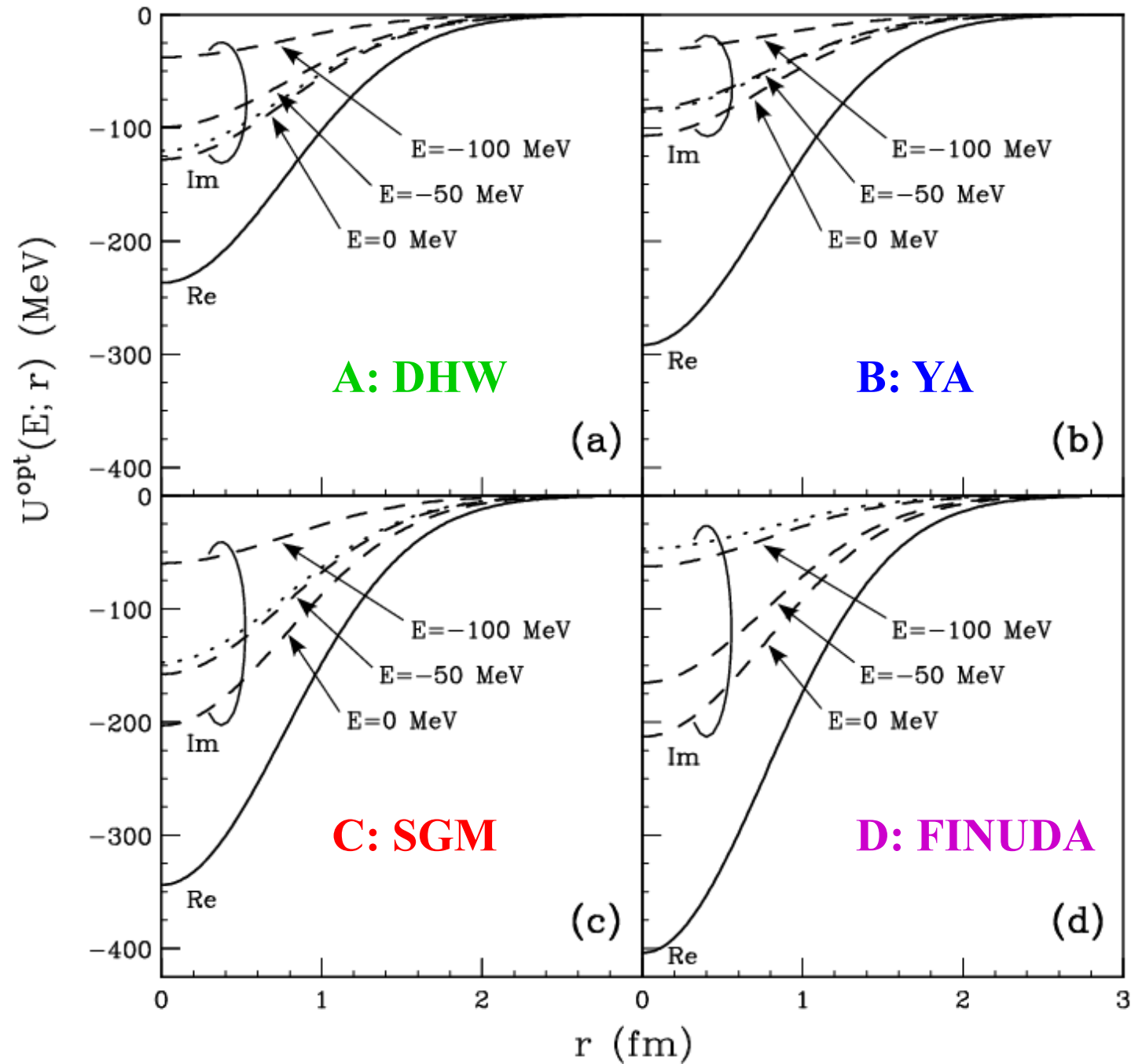
# ◆ Parameters of our optical potentials

	$V_0$ (MeV)	$W_0$ (MeV)	$B_2^{(YN)} = 0.0$		$B_2^{(YN)} = 0.2$	
			B.E. (MeV)	$\Gamma$ (MeV)	B.E. (MeV)	$\Gamma$ (MeV)
<b>A</b>	<b>-237</b>	<b>-128</b>	<b>22</b>	<b>70</b>	<b>15</b>	<b>92</b>
<b>B</b>	<b>-292</b>	<b>-107</b>	<b>48</b>	<b>61</b>	<b>45</b>	<b>82</b>
<b>C</b>	<b>-344</b>	<b>-203</b>	<b>70</b>	<b>110</b>	<b>59</b>	<b>164</b>
<b>D</b>	<b>-404</b>	<b>-213</b>	<b>116</b>	<b>19</b>	<b>115</b>	<b>67</b>

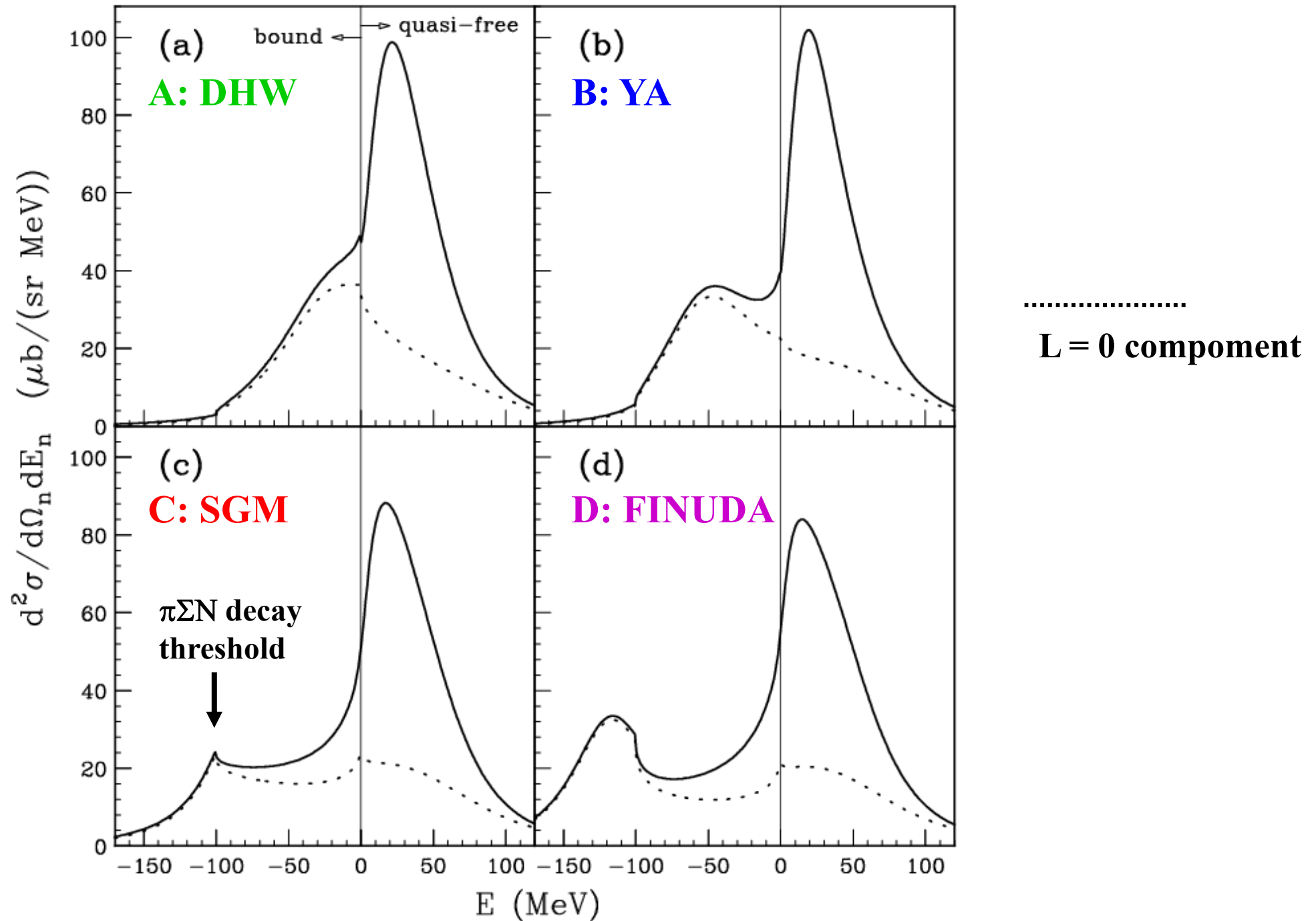
**Fitted values**

**\*  $b = 1.09$  fm for all potentials; the range effect is small.**

# ◆ Employed $K^-$ - $pp$ optical potentials



# ◆ Calculated results of inclusive spectrum



◆ **Decomposition of strength function into  $K^-$  escape /  $K^-$  conversion part**

$$\text{Im } G = (1 + G^\dagger U^\dagger)(\text{Im } G_0)(1 + UG) + G^\dagger(\text{Im } U)G,$$

where  $G = G_0 + G_0 U G$ ,  $G_0$ ; Free Green's function

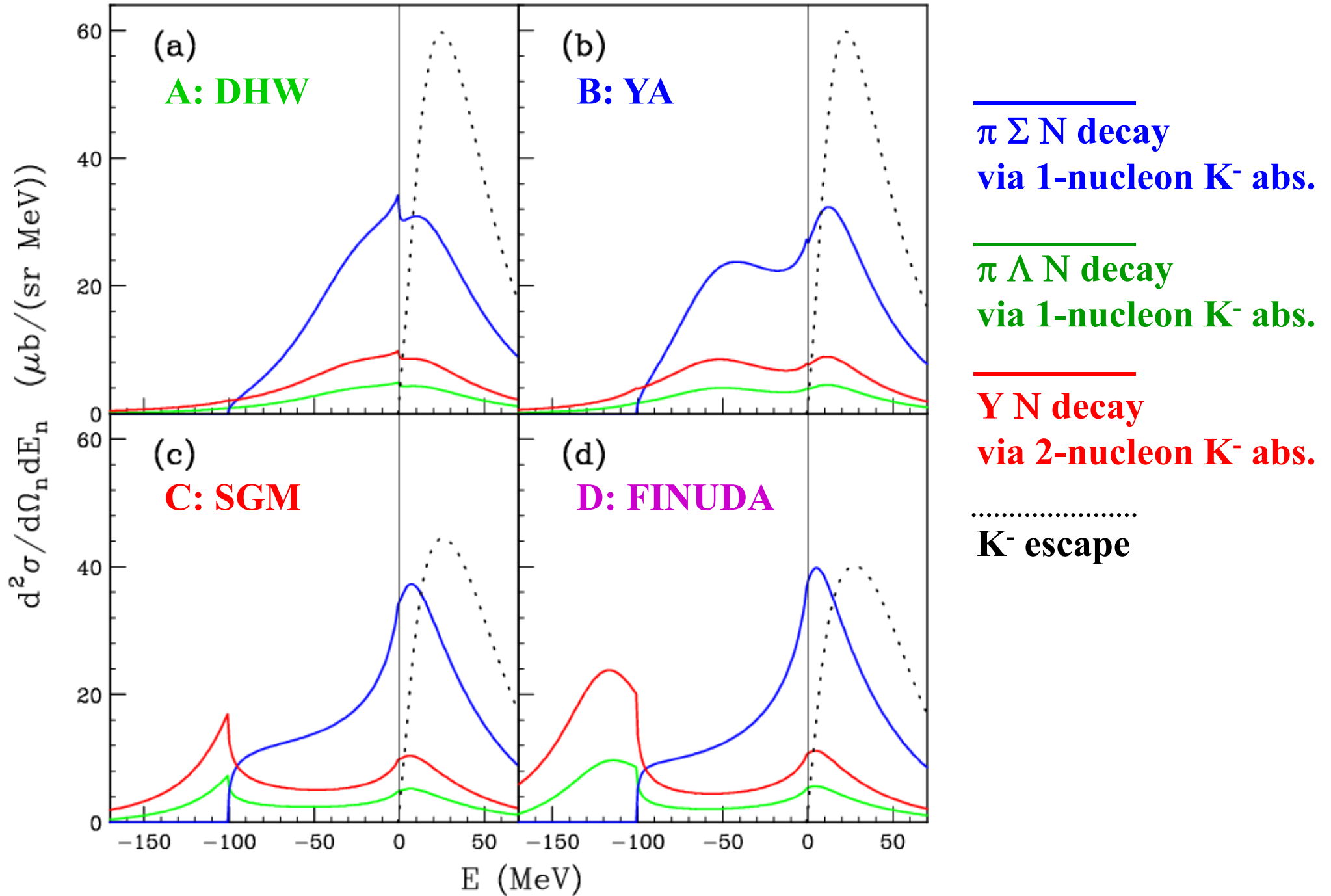
$$S = S^{\text{esc}} + S^{\text{con}}$$

$$\left\{ \begin{array}{l} S^{\text{esc}} = -\frac{1}{\pi} F^\dagger (1 + G^\dagger U^\dagger)(\text{Im } G_0)(1 + UG)F ; \mathbf{K^- \text{ escape}} \\ S^{\text{con}} = -\frac{1}{\pi} F^\dagger G^\dagger (\text{Im } \underline{U})GF ; \mathbf{K^- \text{ conversion}} \end{array} \right.$$

↶ optical potential

★  **$K^-$  conversion spectrum is actually measured in J-PARC experiment.**

# ◆ Decomposition into semi-exclusive spectra

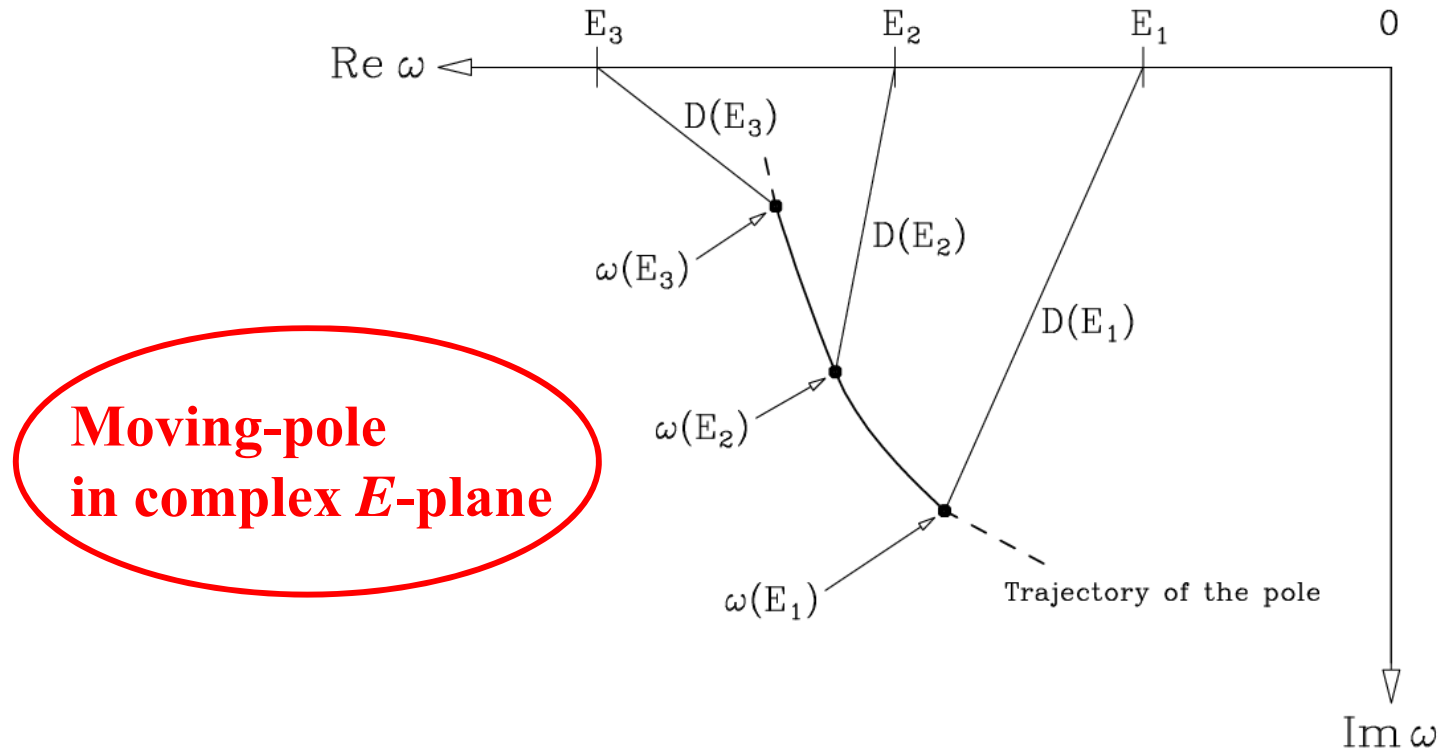




## ◆ Definition of $D(E)$

$$\{(\omega(E) - V_{\text{Coul}}(\mathbf{r}))^2 + \nabla^2 - \mu^2 - 2\mu U^{\text{opt}}(E; \mathbf{r})\} \Phi(E; \mathbf{r}) = 0,$$

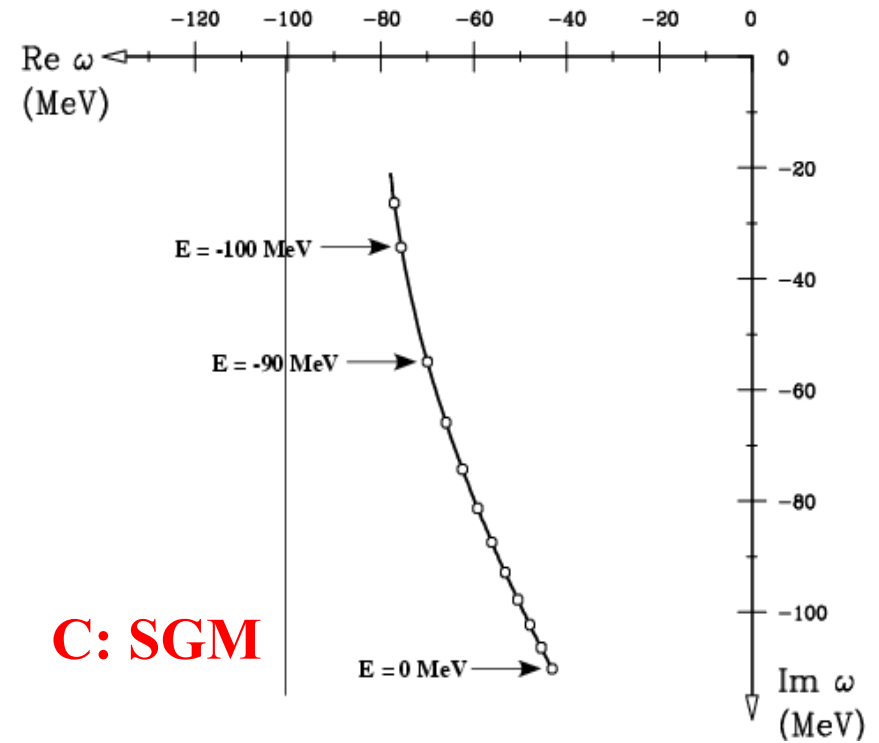
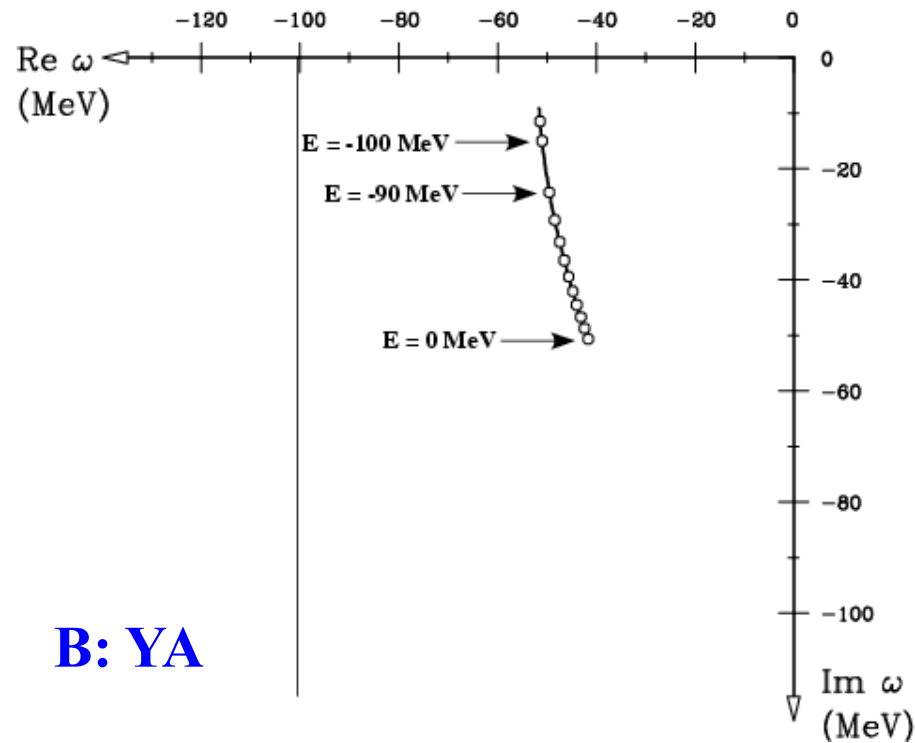
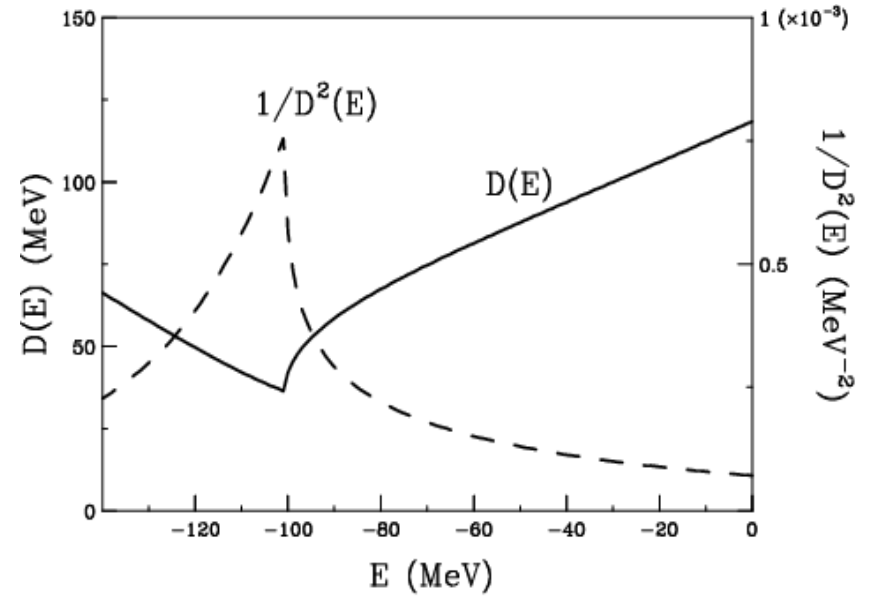
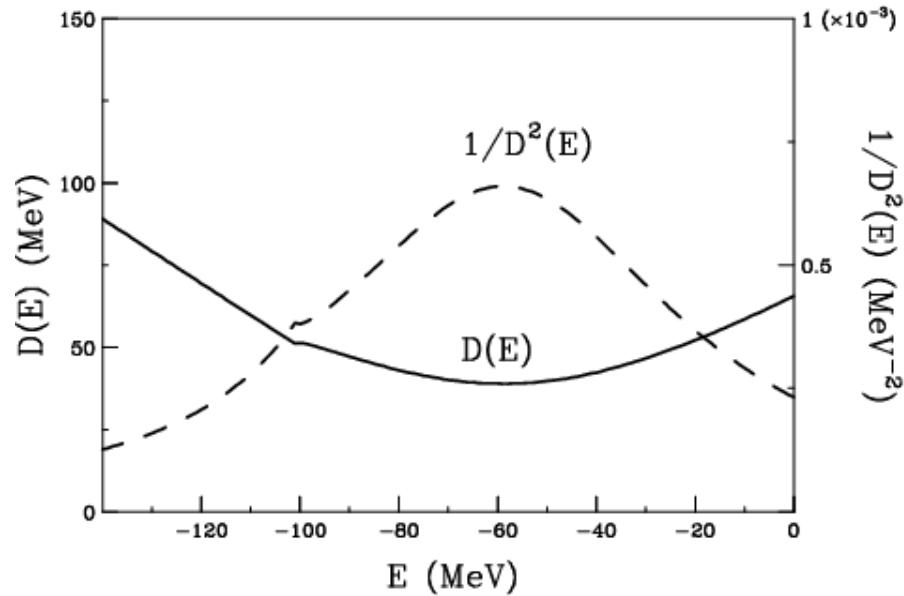
$E$ -dependent complex eigenvalue



$$S_2^{\text{con}}(E) \approx \text{const.} \times \frac{f_2(E)}{D^2(E)} \approx \text{const.} \times \frac{1}{D^2(E)}$$

$$D(E) \equiv \sqrt{(E - \text{Re} \omega(E))^2 + (\text{Im} \omega(E))^2}$$

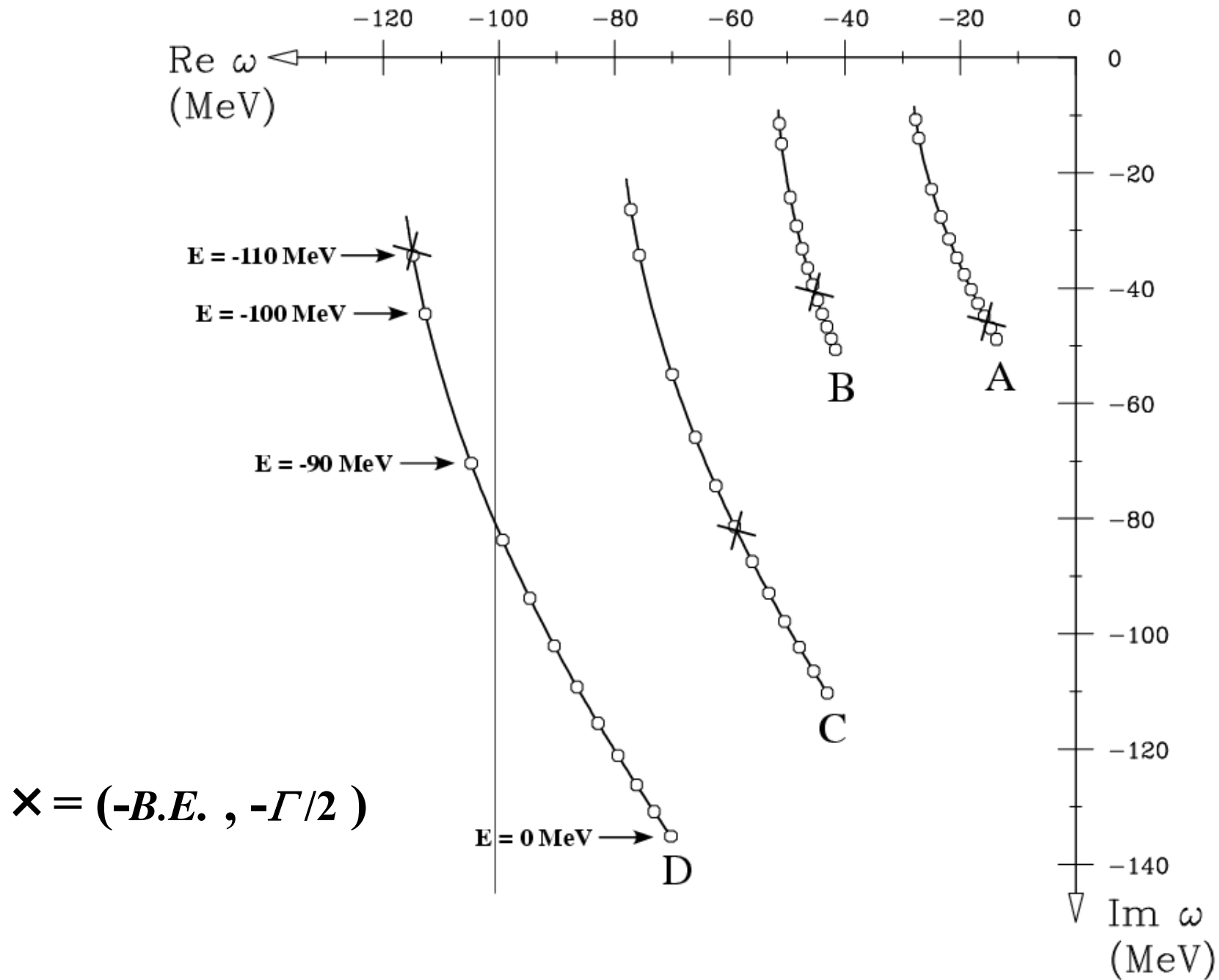
# ◆ Examples of the relation between $D(E)$ and $\omega(E)$



**B: YA**

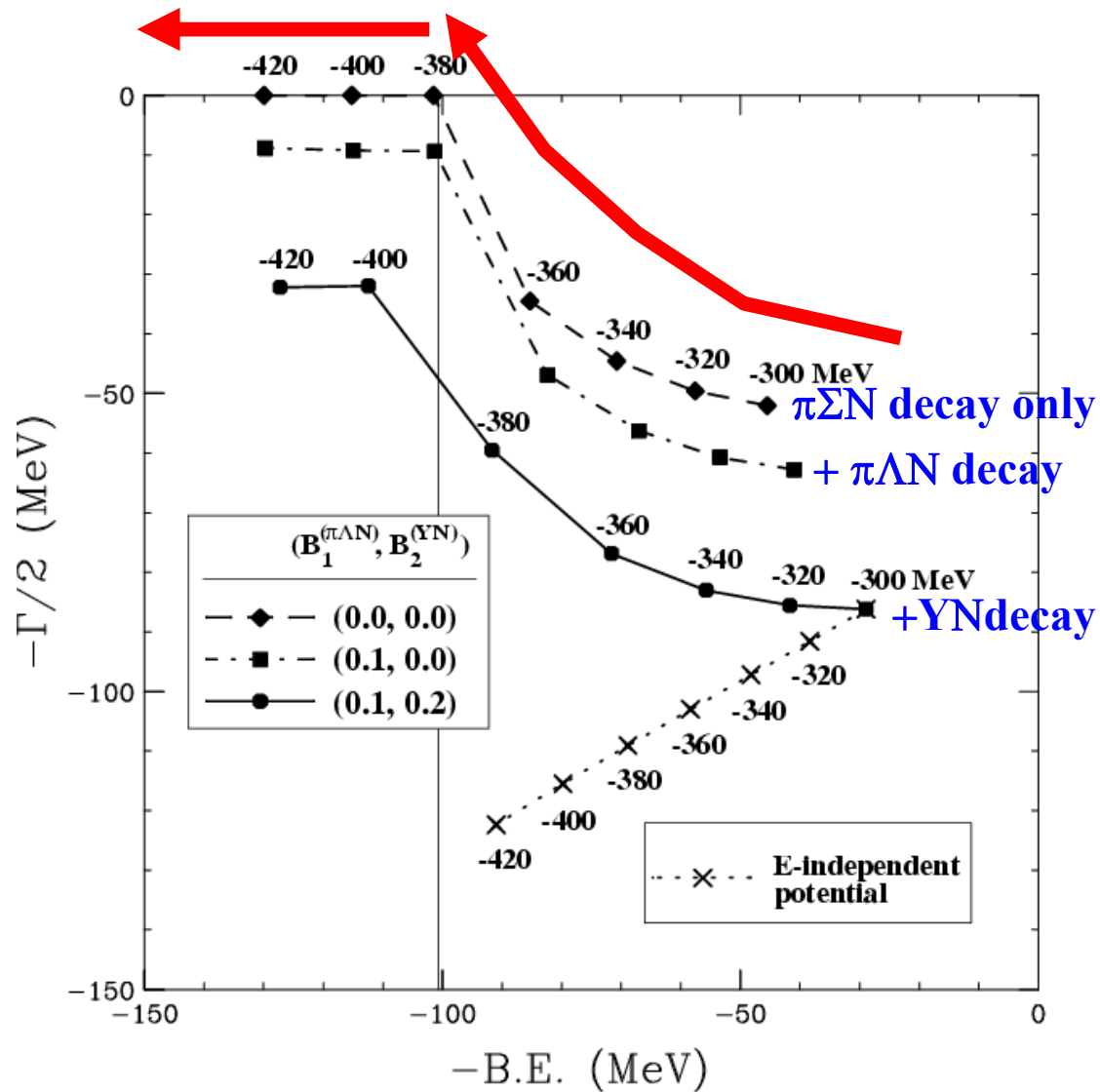
**C: SGM**

# ◆ Pole trajectory $\omega(E)$ in complex $E$ -plane

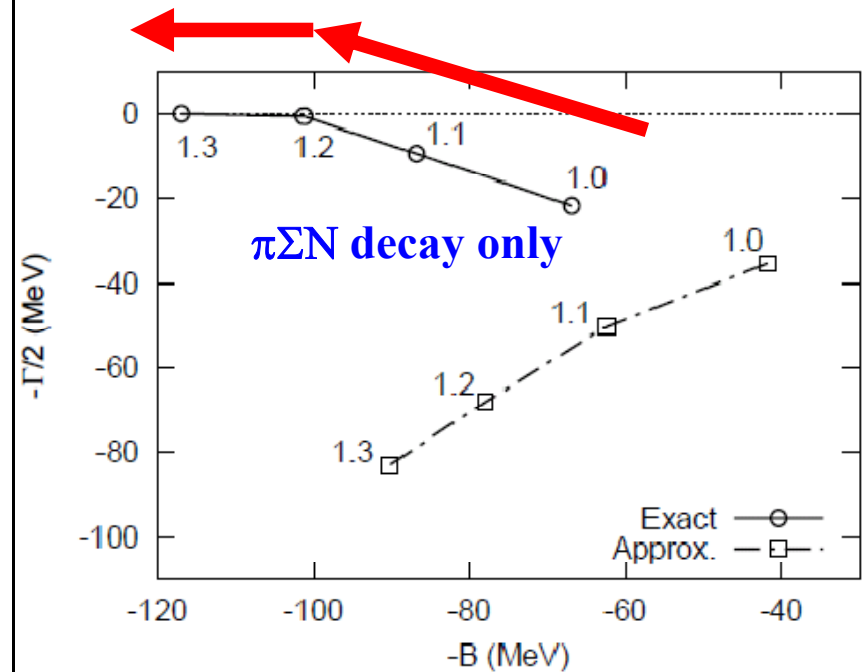


# ◆ Validity of $E$ -dependence of our optical potential

$V_0$  is made deeper  
in our optical potential model.



$K^{\text{bar}}N$  attraction is  
artificially enhanced  
in Faddeev calculation.



Ikeda&Sato,  
Phys. Rev. C79 (2009) 035201.

## ◆ Summary

- Within the  $K^{\text{bar}}NN$  single channel picture, the spectrum shape can be understood by relating to **the trajectory of the moving pole** in the complex  $E$ -plane, rather than the static values of  $B.E.$  and  $\Gamma$ .
- The  $E$ -dependence of the optical potential determines the trajectory of the moving pole.
- The  $E$ -dependence of our phenomenological potential is qualitatively agree with that in the  $K^{\text{bar}}NN - \pi \Sigma N$  Faddeev calculation.