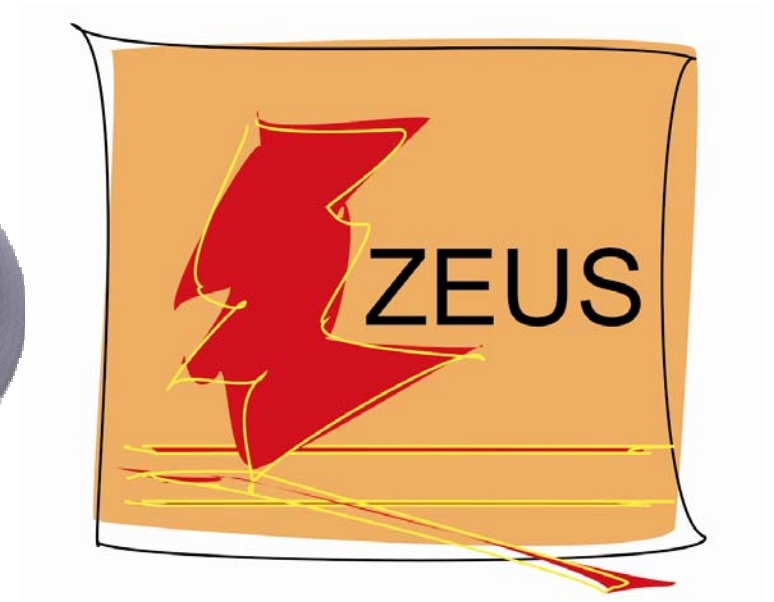


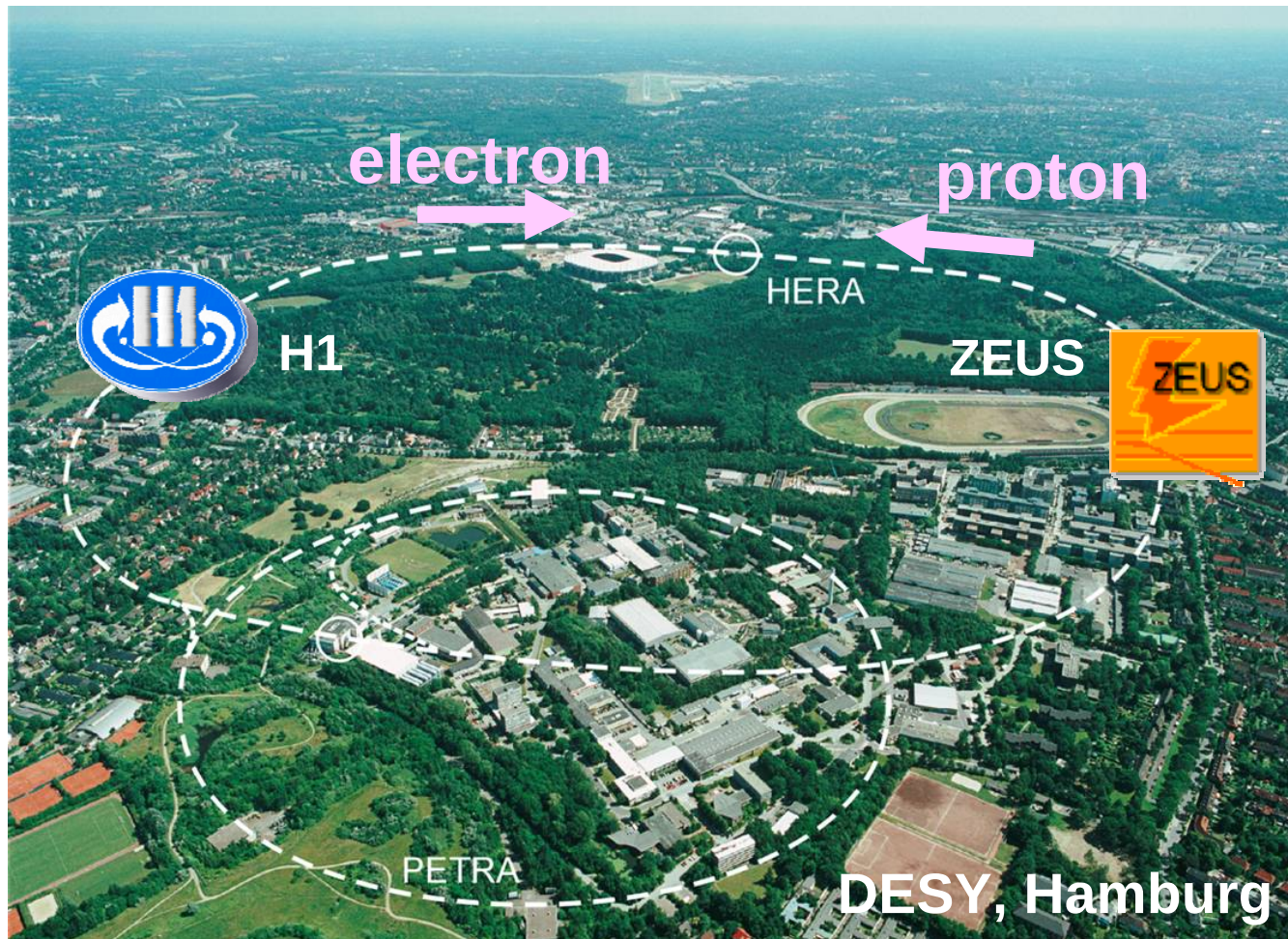
# Results on the proton structure from HERA

Shima Shimizu (CERN)



7/Jan/2011 @ KEK

# The world only e-p collider: HERA



A unique collider at  
DESY, Hamburg

Circumference:  
6.3 km

Operated  
since 1992 to 2007

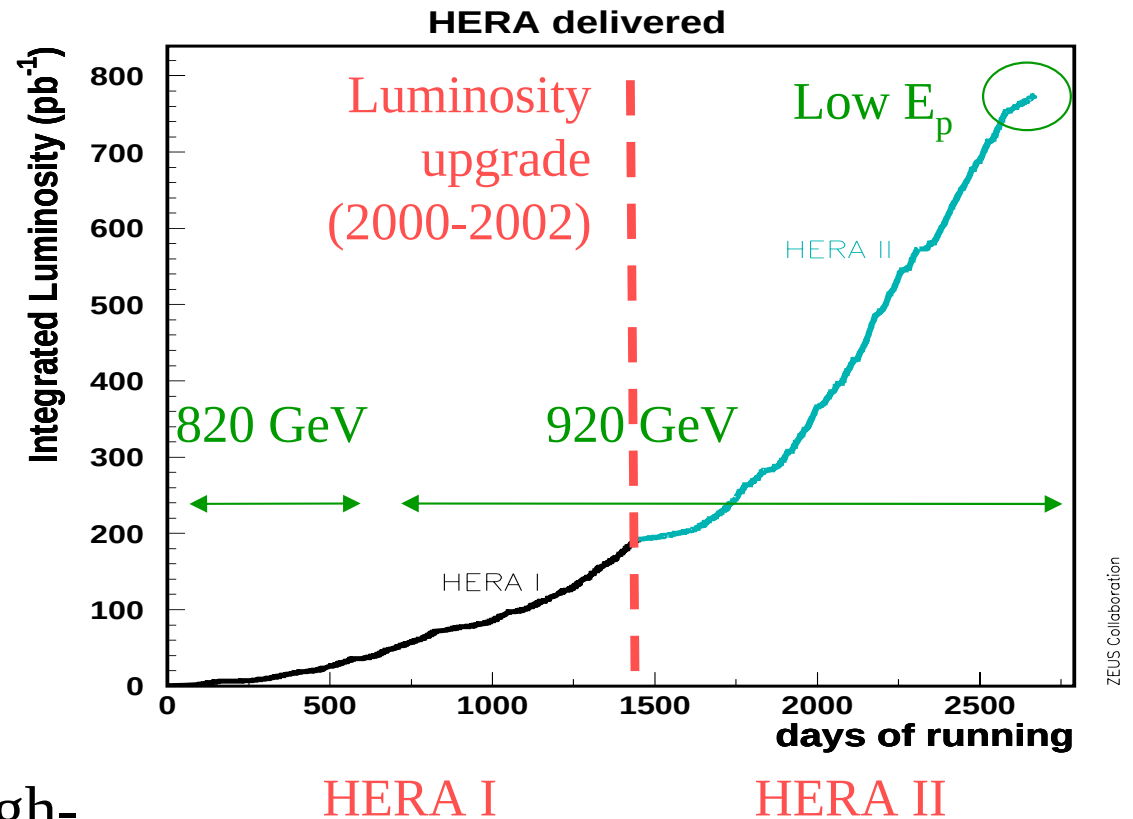
2 collider experiments:  
H1 & ZEUS

Beam energy

- proton : (460, 575, 820,) 920 GeV
  - electron/positron: 27.5 GeV
- center of mass energy  
 $\longrightarrow \sqrt{s} = (225 \sim) 318 \text{ GeV}$

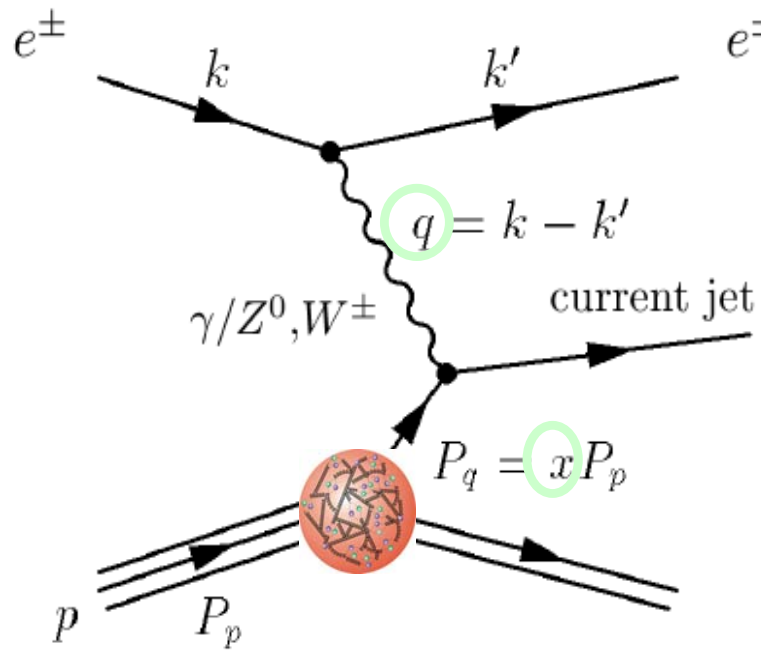
# History of HERA

- 1992-2000: HERA-I  
(started with  $E_p = 820 \text{ GeV}$ , until 1997)  
→ Make full use of large kinematic region.  
 $1.5 \text{ GeV}^2 < Q^2 < 30000 \text{ GeV}^2$
- 2002-2007: HERA-II
  - High luminosity to collect high- $Q^2$  data.  
(high- $Q^2 \leftrightarrow$  Weak boson exchange)
  - lepton beams are polarized.
  - Reduced  $E_p$  runs at the end.



In total, each H1 and ZEUS gains  $\sim 0.5 \text{ fb}^{-1}$ .

# Deep Inelastic Scattering (DIS)



$e^\pm, (\bar{\nu})$  ♦ Kinematic variables to describe DIS

$Q^2$ : Virtuality

→ probing power

$x$ : Bjorken scaling variable

→ momentum fraction of struck quark

$y$ : Inelasticity

$\sqrt{s}$ : center of mass energy

$$Q^2 = sxy$$

$$Q^2 = -q^2 = -(k - k')^2$$

$$x = \frac{Q^2}{2p \cdot q}$$

$$y = \frac{p \cdot q}{p \cdot k}$$

- Inclusive DIS cross sections can be written with structure functions.

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4} Y_\pm \left[ F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \mp \frac{Y_-}{Y_+} xF_3(x, Q^2) \right] \quad Y_\pm = 1 \pm (1 - y^2)$$

cross section with  
point-like particle

**Structure functions** reflect momentum  
distribution of partons in the proton.



# Structure functions and PDFs

Measured quantity: reduced cross section

$$Y_{\pm} = 1 \pm (1 - y^2)$$

$$\sigma_r(e^{\pm} p) = \frac{Q^4 Y_{\pm}}{2\pi\alpha^2} \frac{d^2\sigma}{dx dQ^2} = F_2(x, Q^2) - \frac{y^2}{Y_{\pm}} F_L(x, Q^2) \mp \frac{Y_{\mp}}{Y_{\pm}} xF_3(x, Q^2)$$

Structure functions are used for determination of the parton distribution functions (**PDFs**),  $q(x, Q^2)$  and  $g(x, Q^2)$

- $F_2$  : [Sea + valence] quarks, (gluon)

$$F_2 = \sum A_q x(q + \bar{q}) \quad \frac{\partial F_2}{\partial \ln Q^2} \propto xg$$

- $F_L$  : longitudinal structure function

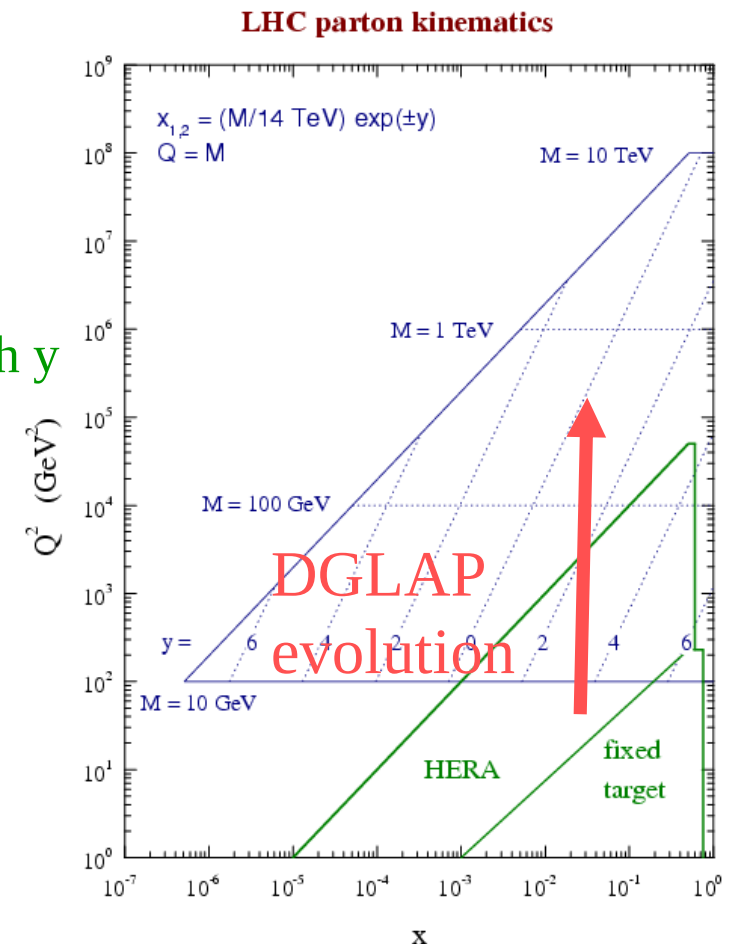
→ gluon (see later) sizable only at high  $y$

- $xF_3$  : parity violation term (Electroweak)

$$xF_3 = \sum B_q x(q - \bar{q}) \quad \text{high } Q^2 \text{ only}$$

→ Valence quarks

The  $Q^2$  evolution can be described by perturbative QCD, using **DGLAP equation**.

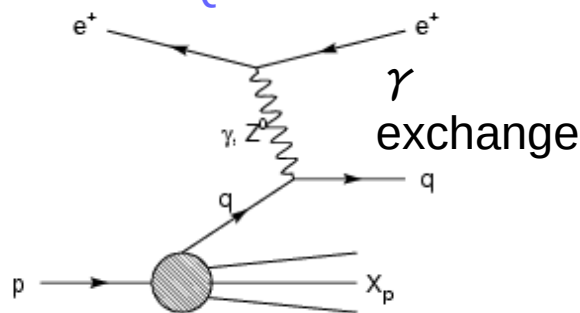


# DIS at HERA

Pure proton target

→ Free from target correction, nuclear effect.

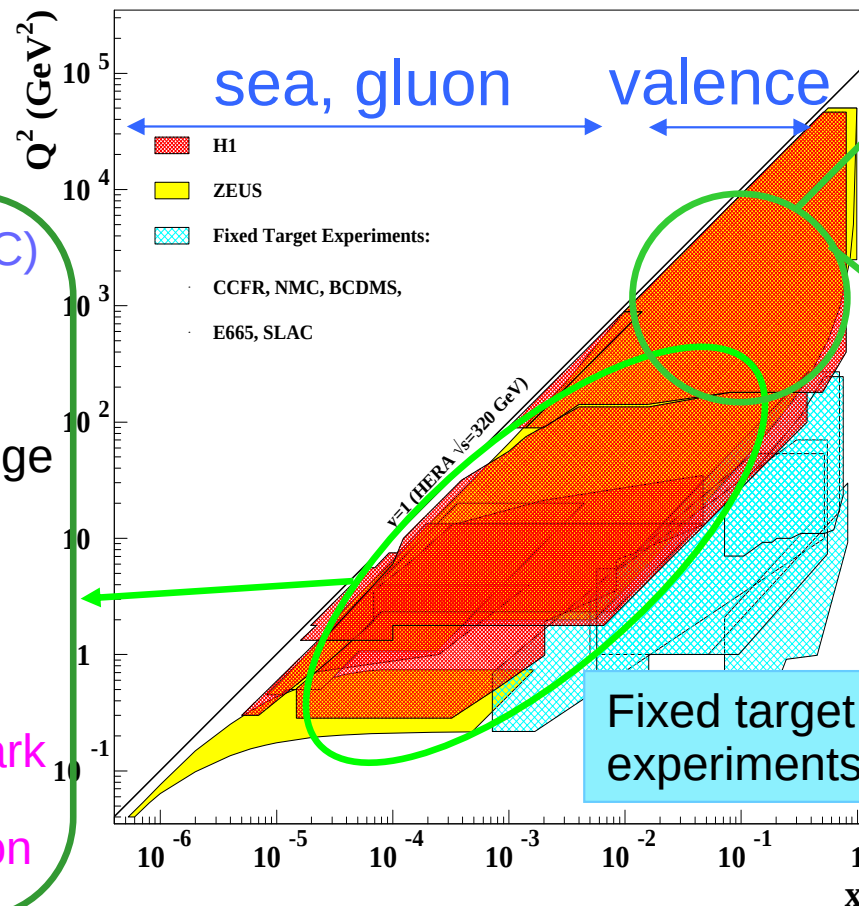
## ♦ Neutral current DIS (NC) at low $Q^2$



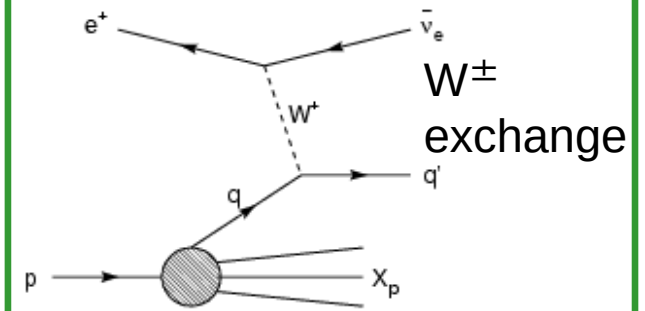
$$\gamma \rightarrow F_2 \propto \sum x(q + \bar{q})$$

Sea + valence quark

$$\frac{\partial F_2}{\partial \ln Q^2} \propto xg \quad \text{gluon}$$

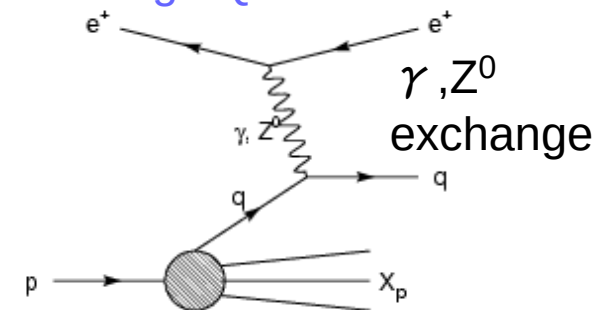


## ♦ Charged current DIS (CC)



Charge selective interaction  
 $e^- : u \text{ quark}$      $e^+ : d \text{ quark}$

## ♦ Neutral current DIS (NC) at high $Q^2$



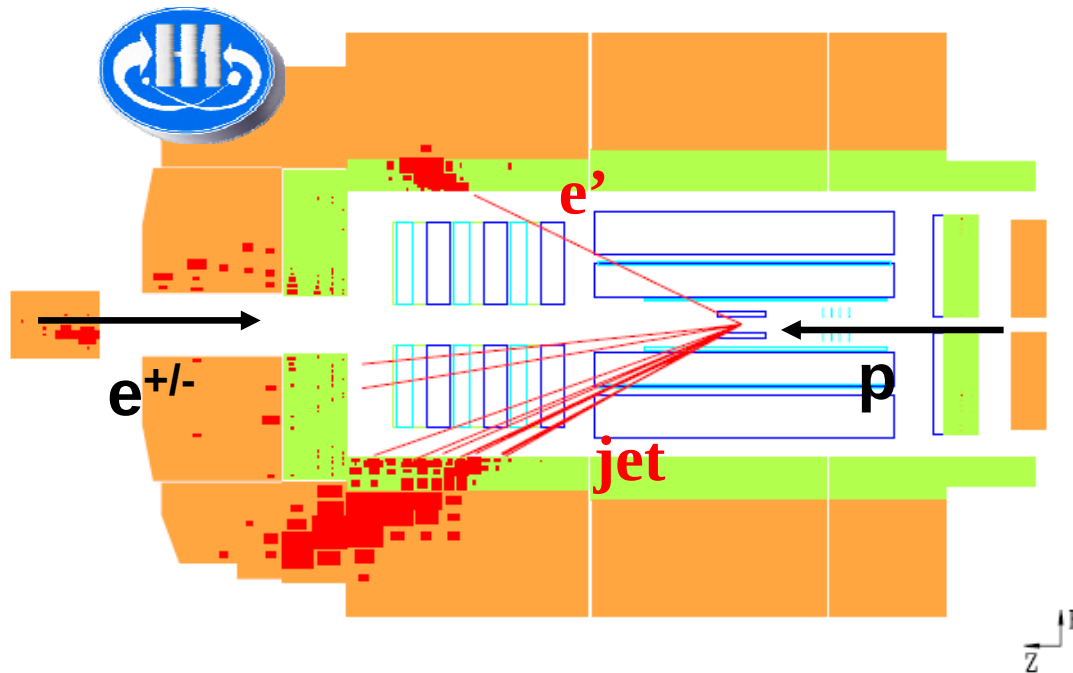
Sea + valence quark  
 $Z^0$  introduces parity violation.  
 $\rightarrow xF_3 \propto \sum x(q - \bar{q})$   
 valence quark

# DIS in the detectors

## Neutral current (NC) process

$\gamma / Z^0$  exchange

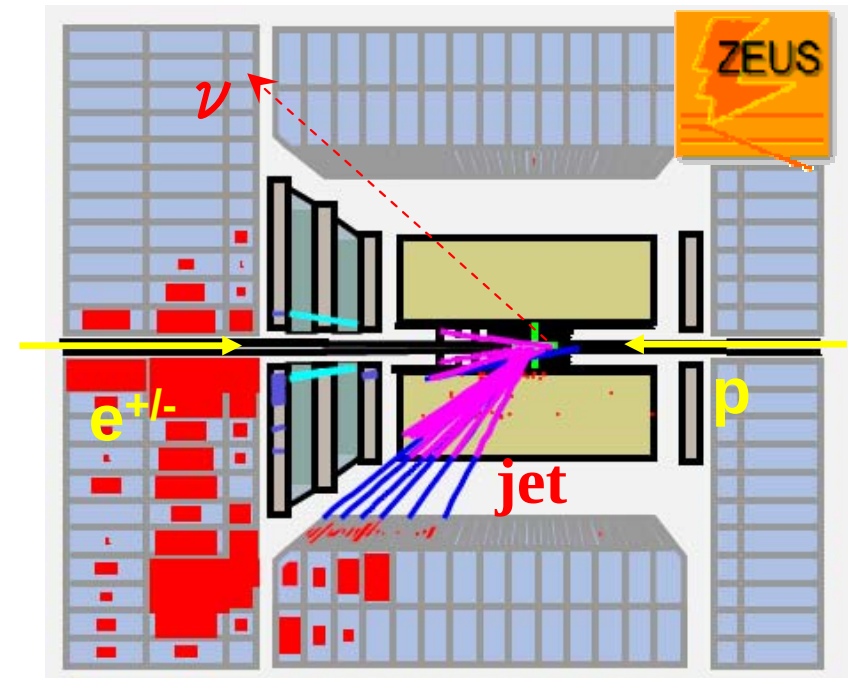
$ep \rightarrow e' X$



## Charged current (CC) process

$W^{+-}$  exchange

$ep \rightarrow \nu X$



- Kinematic variables are reconstructed by two of measured variables;

$\begin{bmatrix} \text{energy} \\ \text{angle} \end{bmatrix}$  of  $\begin{bmatrix} \text{scattered electron} \\ \text{jet } (\sim \text{struck quark}) \end{bmatrix}$

# HERA I inclusive DIS cross sections and HERA PDF1.0

published: JHEP01 (2010) 109



# Combining H1 and ZEUS cross sections

Combining all the HERA-I inclusive DIS cross sections from H1 and ZEUS:

- ◆ HERA I:  $e^+p \sim 100\text{pb}^{-1}$ ,  $e^-p \sim 16\text{pb}^{-1}$
- ◆ NC:  $0.045 < Q^2 < 30000 \text{ GeV}^2$ , CC:  $280 < Q^2 < 30000 \text{ GeV}^2$
- ◆ 1402 points (14 papers)

→ After combination: 741 points

Combination is done by averaging each data point by simultaneous  $\chi^2$  fit.

- ◆ Assumption:

H1 and ZEUS measure the same cross sections.

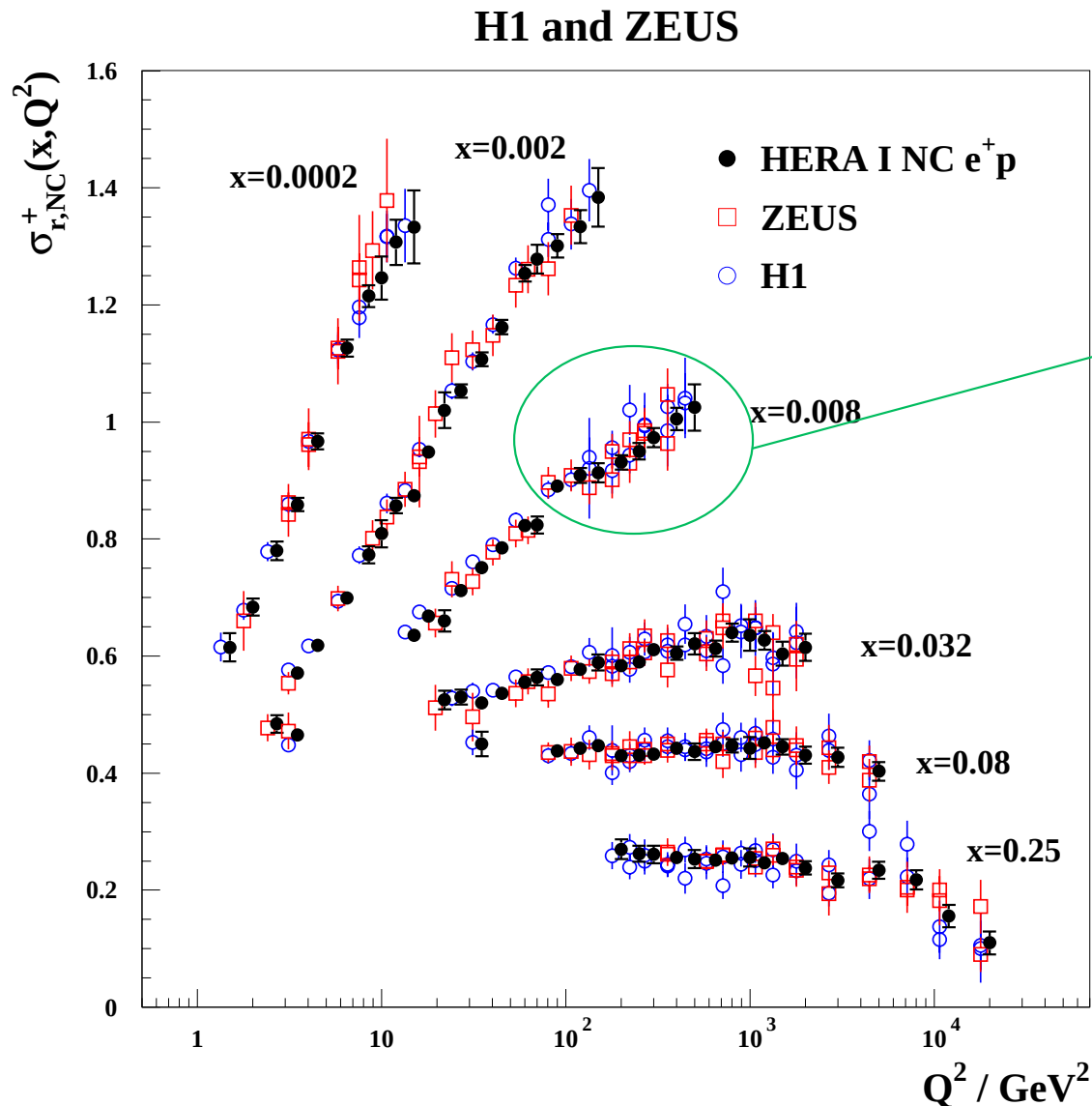
- ◆ Taking account of correlated systematics within/between experiments.

Different detectors and analysis techniques bring different sensitivities to similar source of correlated systematic uncertainties.

→ Cross calibration of experiments

Reduction of systematic uncertainties.

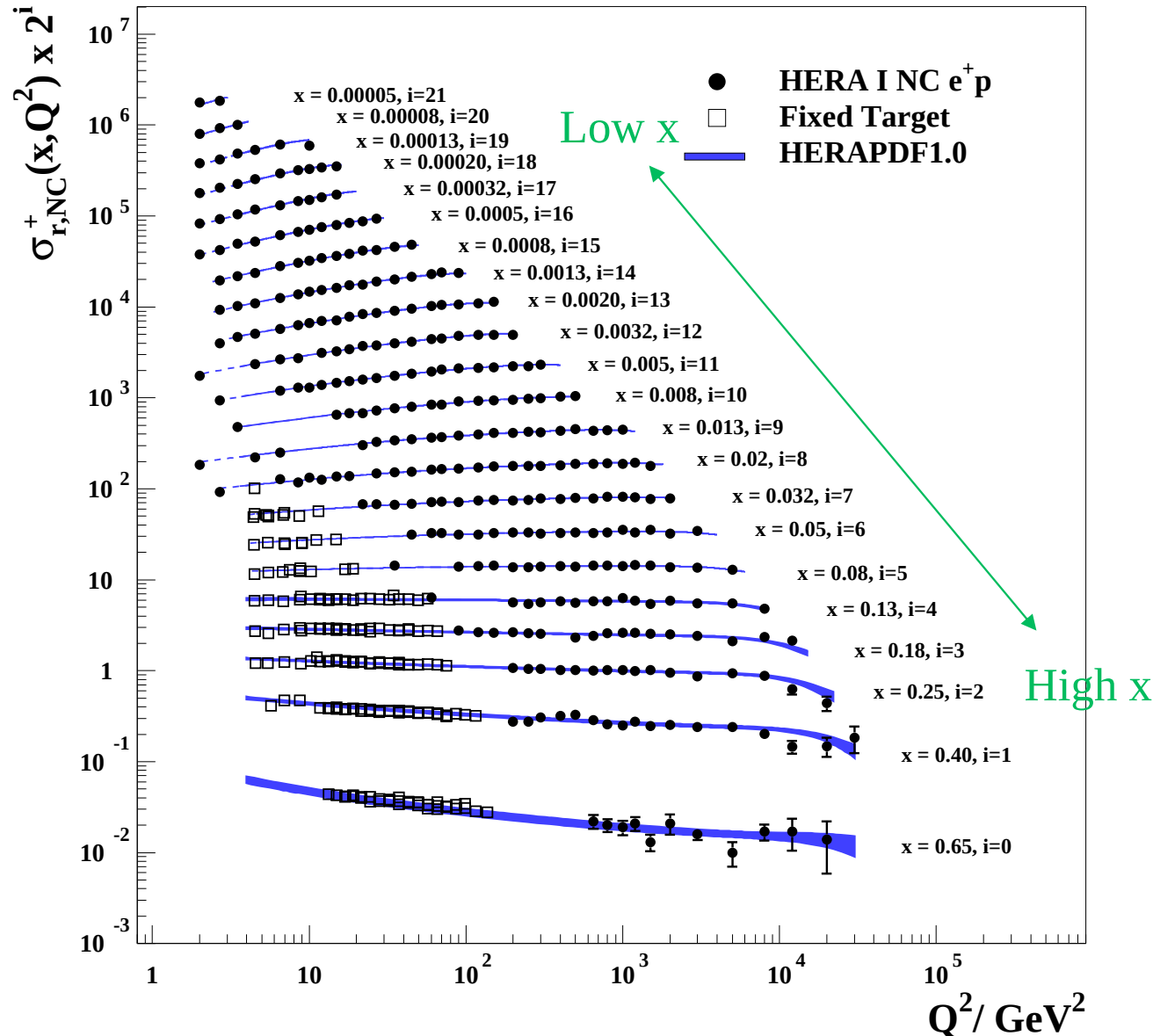
# Combining H1 and ZEUS cross sections



Uncertainty gets improved  
by more than  $\sqrt{2}$ .  
← Main reduction in  
systematic uncertainties.

# Combined inclusive DIS cross sections

H1 and ZEUS



- ◆ Precision of 1-2% for  $3 < Q^2 < 500 \text{ GeV}^2$ .
- ◆ Scaling violation is clearly seen.

$$\frac{\partial F_2}{\partial \ln Q^2} \propto xg$$

JHEP01 (2010) 109

# HERA PDF 1.0

## Data sets

- ◆ Combined HERA I inclusive DIS cross sections  
e<sup>-</sup>p CC, e<sup>+</sup>p CC, e<sup>-</sup>p NC ( $Q^2 > 100 \text{ GeV}^2$ ), e<sup>+</sup>p NC ( $Q^2 > Q_{\text{min}}^2$ )

## Settings

- ◆ PDF parameterized at the starting scale  $Q_0^2$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g},$$

$$xu_v(x) = A_{uv} x^{B_{uv}} (1-x)^{C_{uv}} (1 + E_{uv} x^2)$$

$$xd_v(x) = A_{dv} x^{B_{dv}} (1-x)^{C_{dv}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \quad \bar{U} = \bar{u} + \bar{c}$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}, \quad \bar{D} = \bar{d} + \bar{s} + \bar{b}$$

Central fit has 10 free parameters:

← chosen by saturation of  $\chi^2$

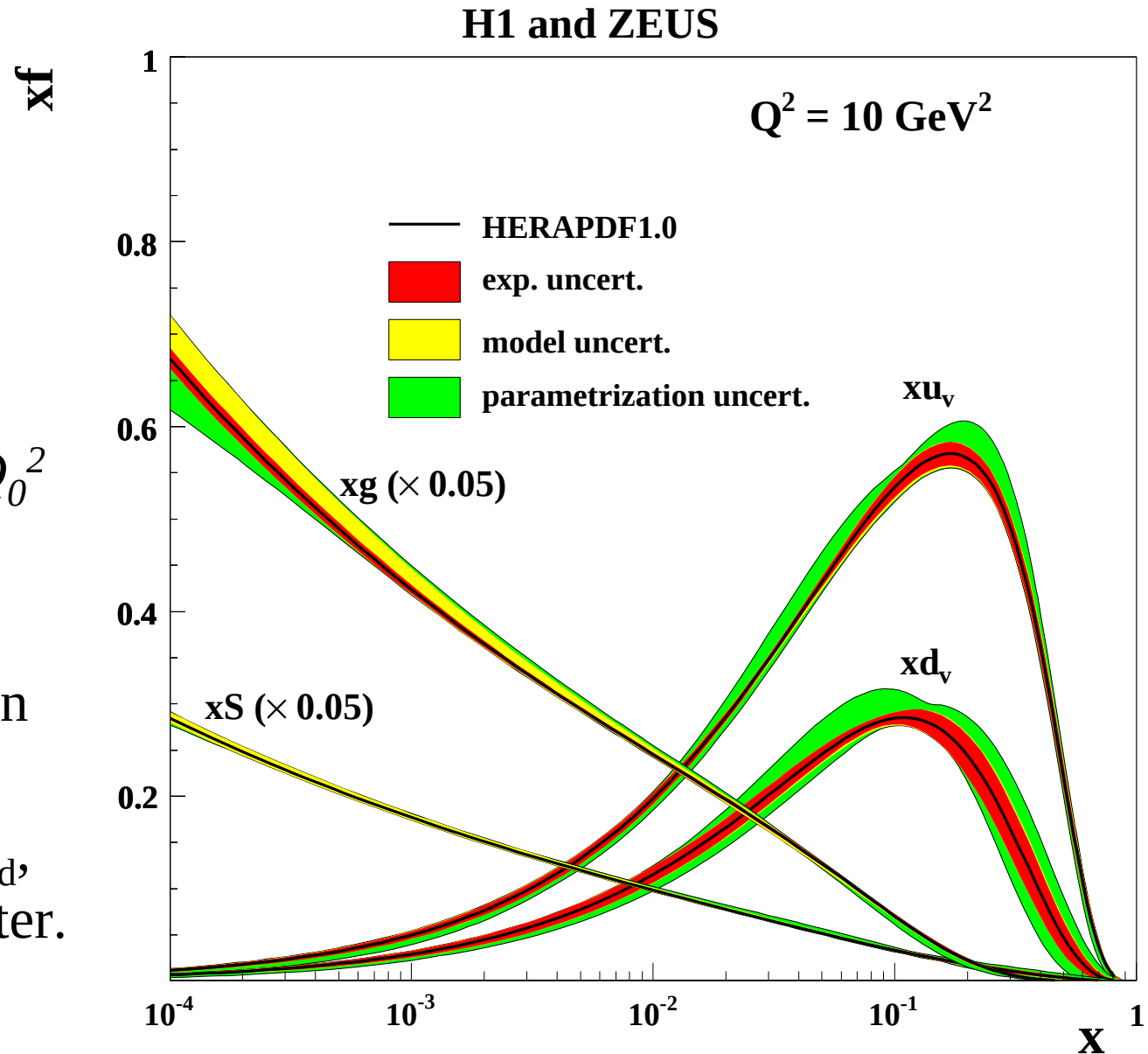
- ◆ RT-VFN scheme
- ◆ NLO DGLAP evolution using QCDNUM17.02
- ◆ Scales:  $\mu_R = \mu_F = Q^2$

|                                        |        |
|----------------------------------------|--------|
| $\alpha_s(M_Z)$                        | 0.1176 |
| $f_s = s/D$                            | 0.31   |
| $m_c$ (GeV)                            | 1.4    |
| $m_b$ (GeV)                            | 4.75   |
| $Q_{\text{min}}^2$ (GeV <sup>2</sup> ) | 3.5    |
| $Q_0^2$ (GeV <sup>2</sup> )            | 1.9    |

# HERA PDF 1.0

## Uncertainties

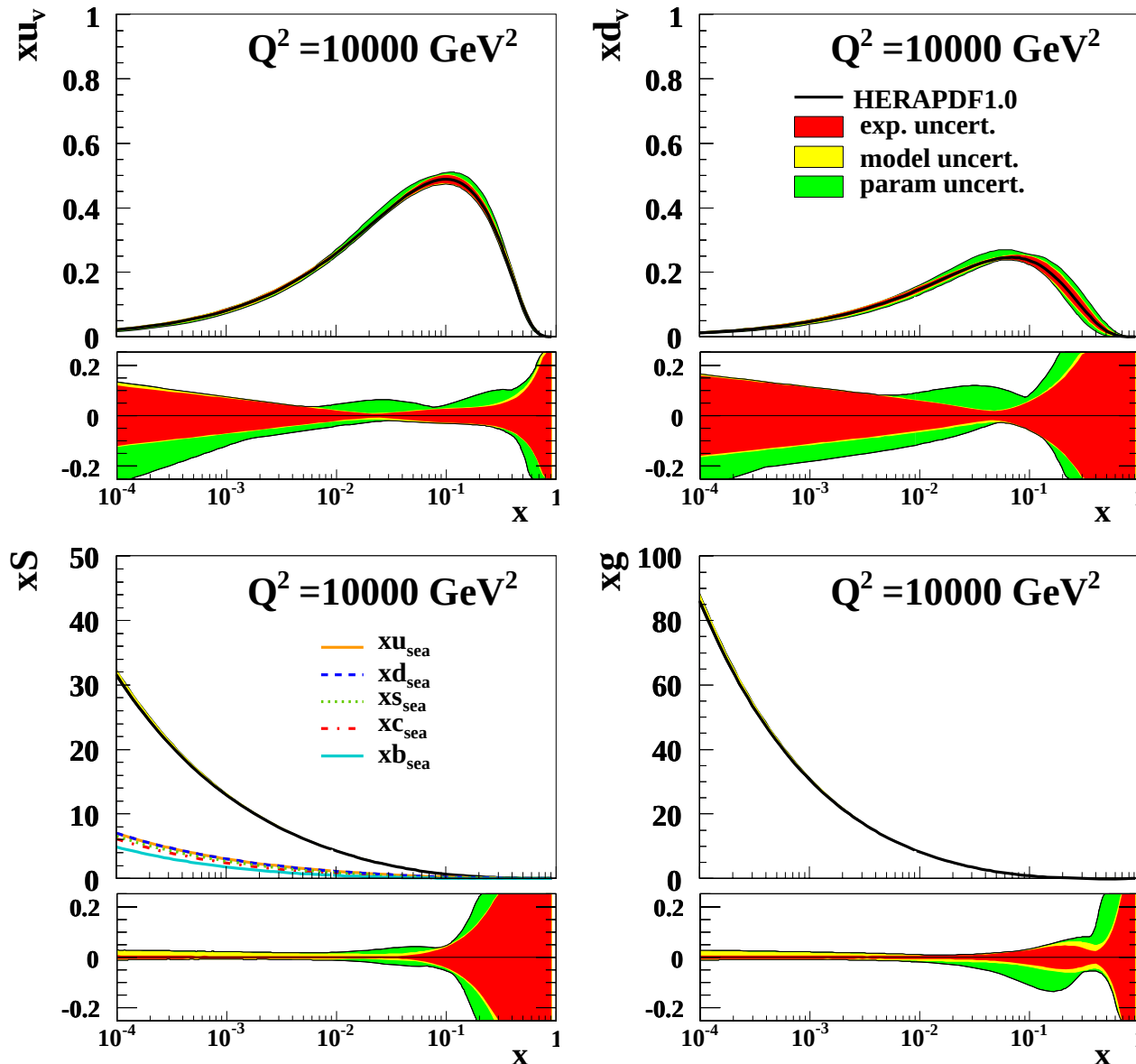
- experimental:  $\Delta \chi^2=1$
- model:  
Different set of values of  $f_s, m_c, m_b, Q_{min}^2, Q_0^2$
- parameterization:  
envelope of parameter variation  
e.g.  $Q_0^2$ , negative gluon, relax  $B_u=B_d$ , additional parameter.





# Relative Uncertainties at High $Q^2$

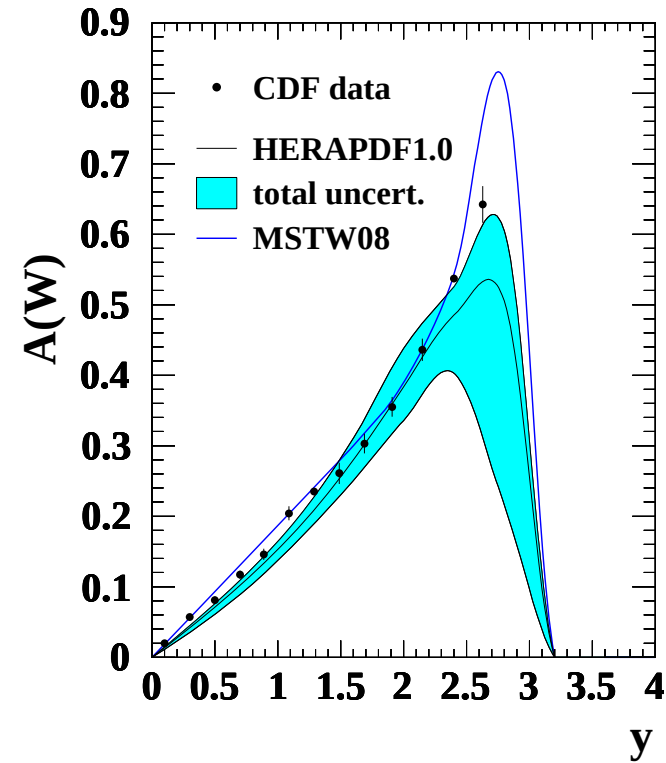
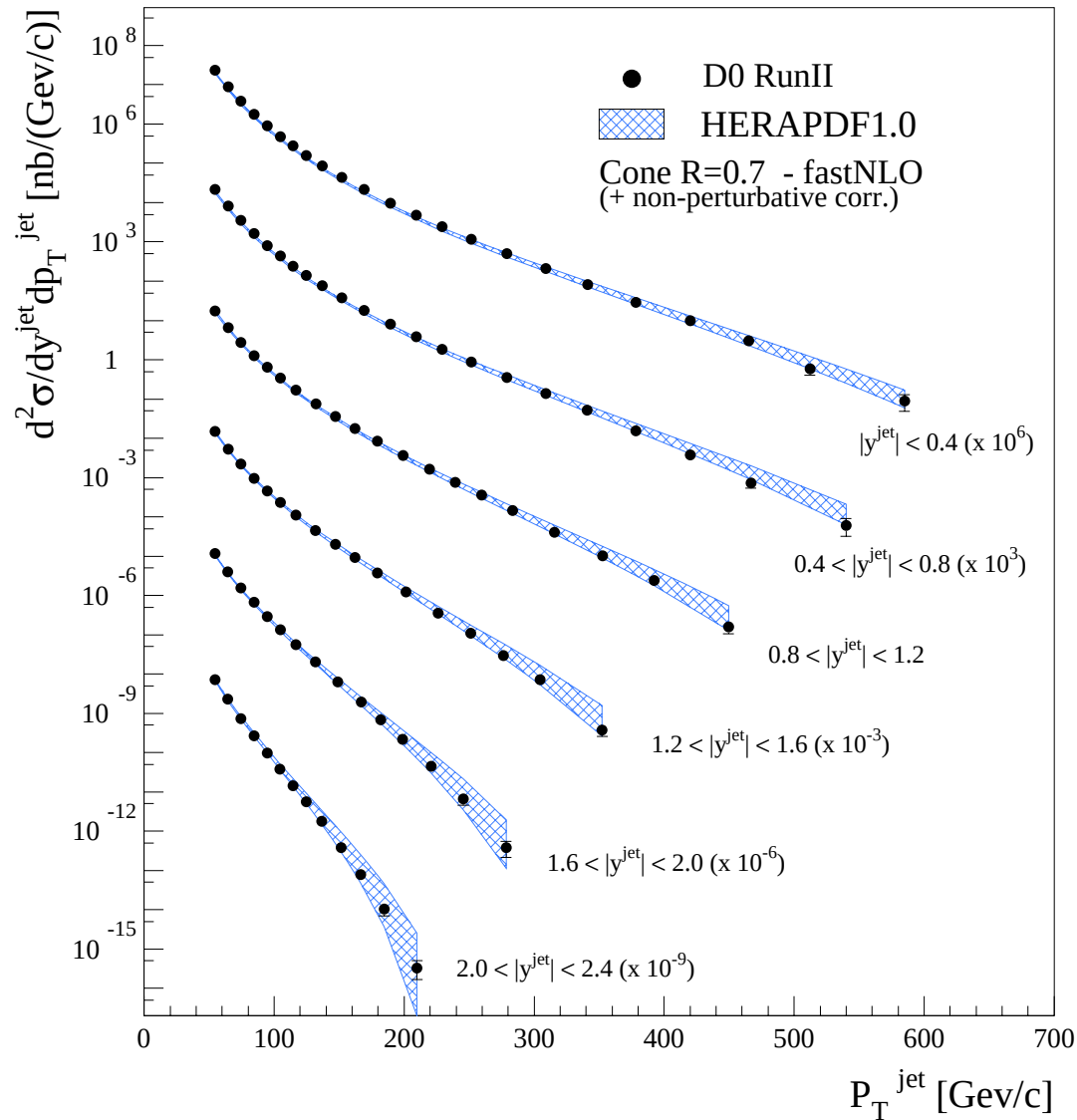
## H1 and ZEUS



At  $Q^2 = 10000 \text{ GeV}^2$ ,  
2% uncertainty on  
gluon for  $x < 0.01$ .

# HERA PDF and Tevatron Data

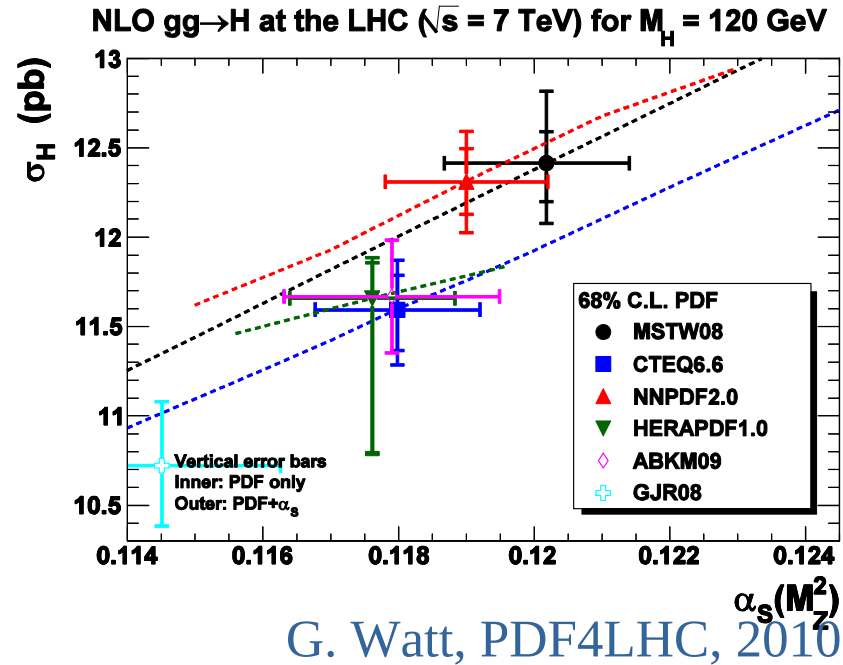
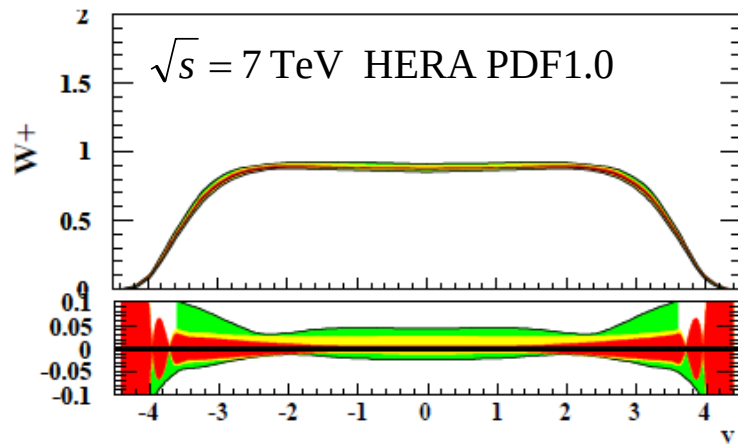
Tevatron Jet Cross Sections



Good description of Tevatron data by HERA PDF.

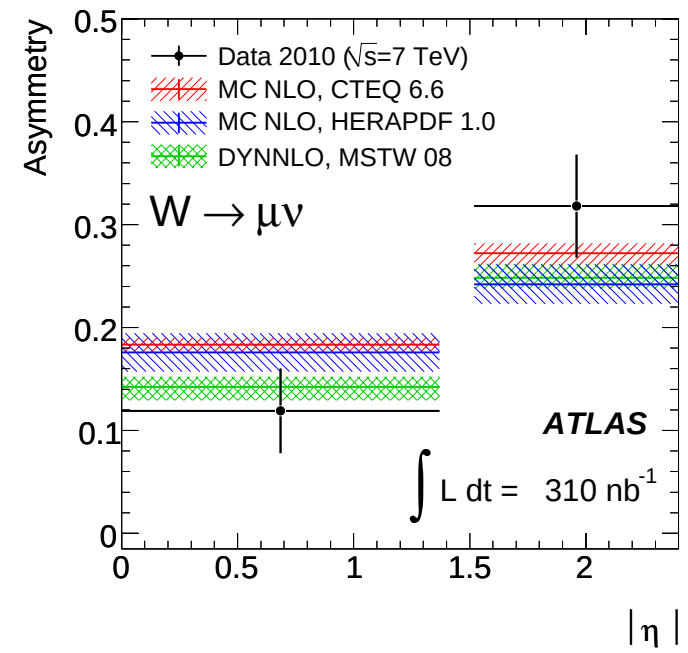
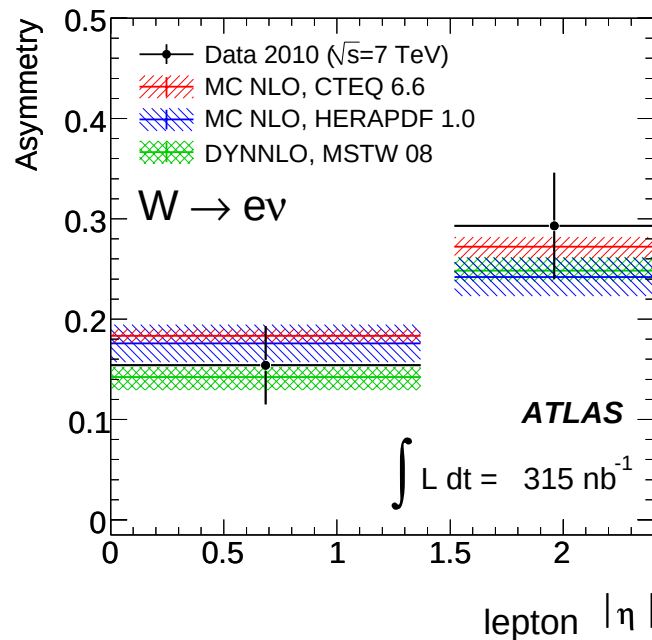
# HERA PDFs for LHC

Several predictions are calculated with reasonable uncertainties.



Comparison with data has started.

CERN-PH-EP-2010-037  
arXiv:hep-ex 1010.2130



**Further measurements at HERA**

# Further input from HERA

HERA PDF1.0 uses inclusive DIS cross section in HERA I only.

- ◆ HERA II High  $Q^2$  NC/CC cross sections

- Increase of electron data

- NC: More sensitivity to  $xF_3$   
i.e. valence quarks (u+d)

- Increase of positron data

- CC: More sensitivity to d quark

|        | HERA-I              | HERA-II             |
|--------|---------------------|---------------------|
| $e^-p$ | $20\text{pb}^{-1}$  | $180\text{pb}^{-1}$ |
| $e^+p$ | $100\text{pb}^{-1}$ | $170\text{pb}^{-1}$ |

- ◆ Inclusive Jet cross sections

- ◆ Longitudinal structure functions

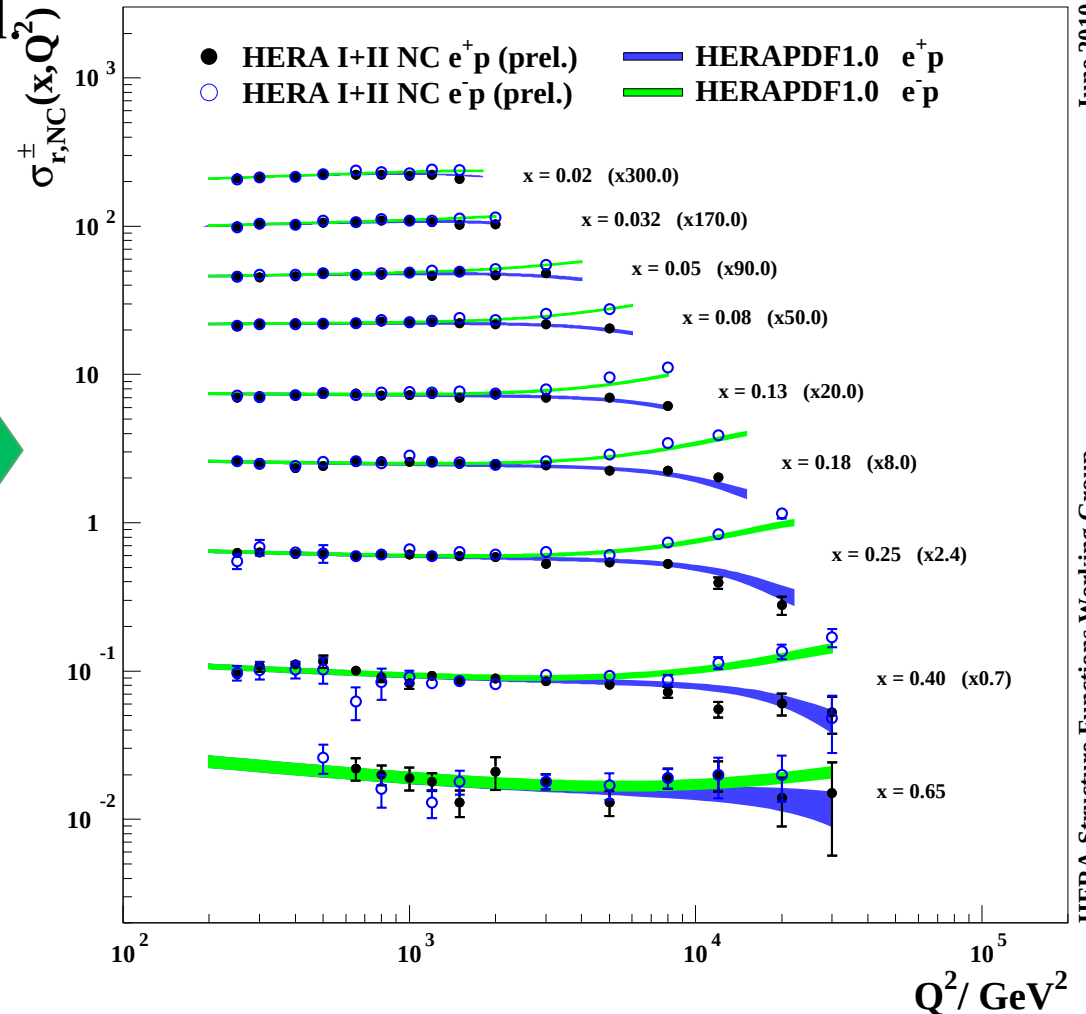
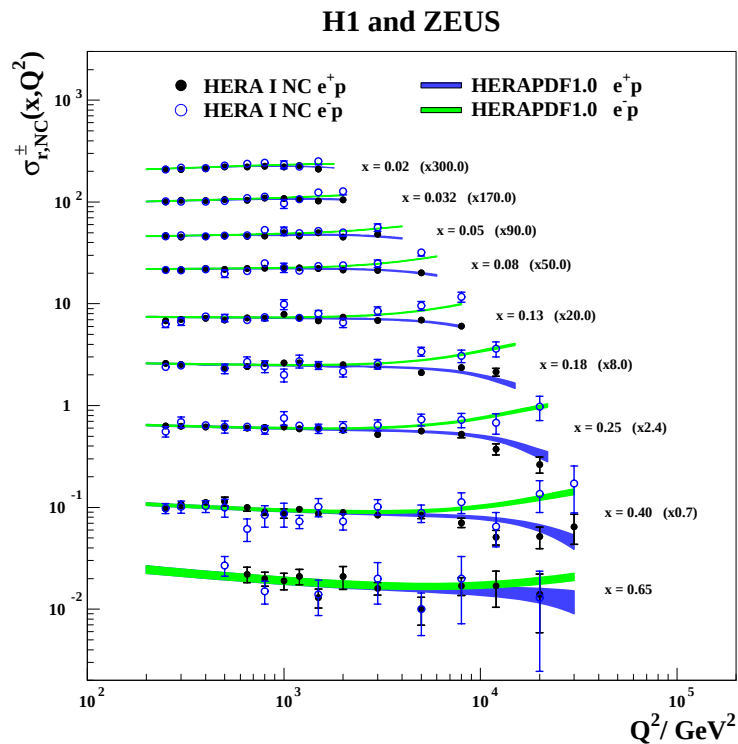
- ◆ Heavy flavour structure functions

# HERA I+II NC cross sections

HERA II NC are also combined,

- H1  $e^+p$ ,  $e^-p$
- ZEUS  $e^-p$

H1 and ZEUS



June 2010

HERA Structure Functions Working Group

- ◆ Improved precision.
  - ◆ Clear separation of  $e^+p$  and  $e^-p$  at high  $Q^2$
- $\Rightarrow xF_3 = \sum B_q x(q - \bar{q})$  valence quark

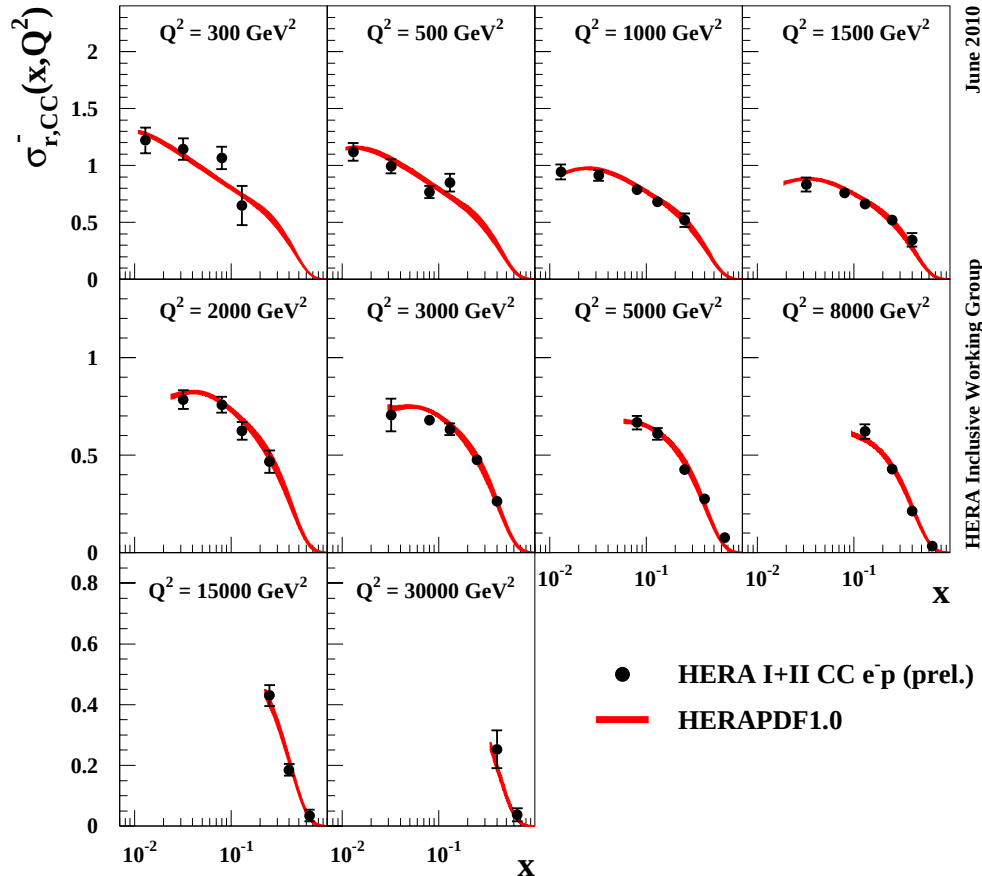
to be included:  
ZEUS 06-07  $e^+p$  NC

# HERA I+II combined CC cross sections

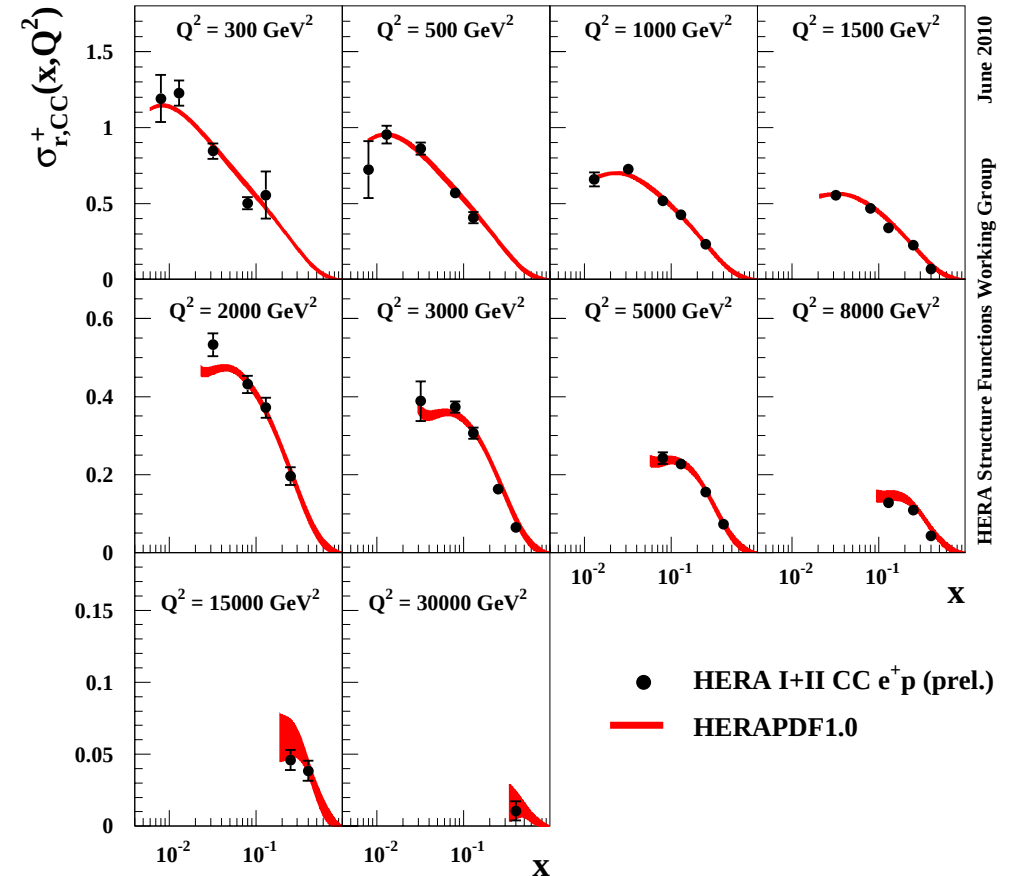
$$\sigma_r^{CC}(e^- p) \propto [u + c + (1-y)^2(\bar{d} + \bar{s})]$$

$$\sigma_r^{CC}(e^+ p) \propto [\bar{u} + \bar{c} + (1-y)^2(d + s)]$$

H1 and ZEUS



H1 and ZEUS

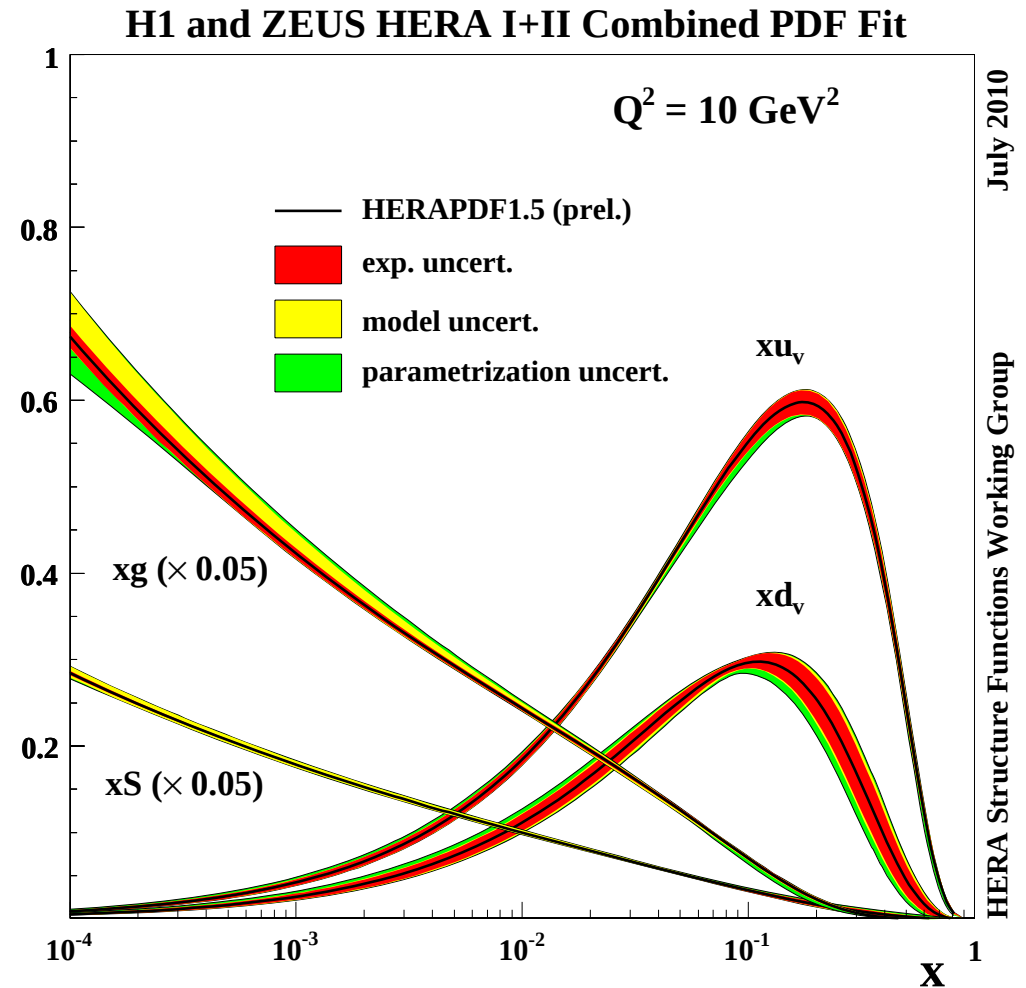
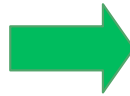
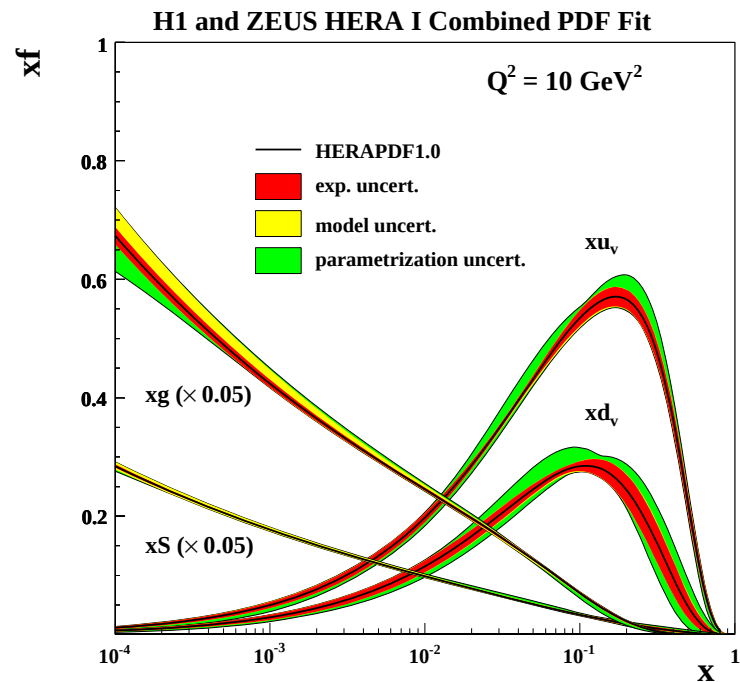


Sensitive to valence quarks.



# HERA PDF 1.5 (prel.)

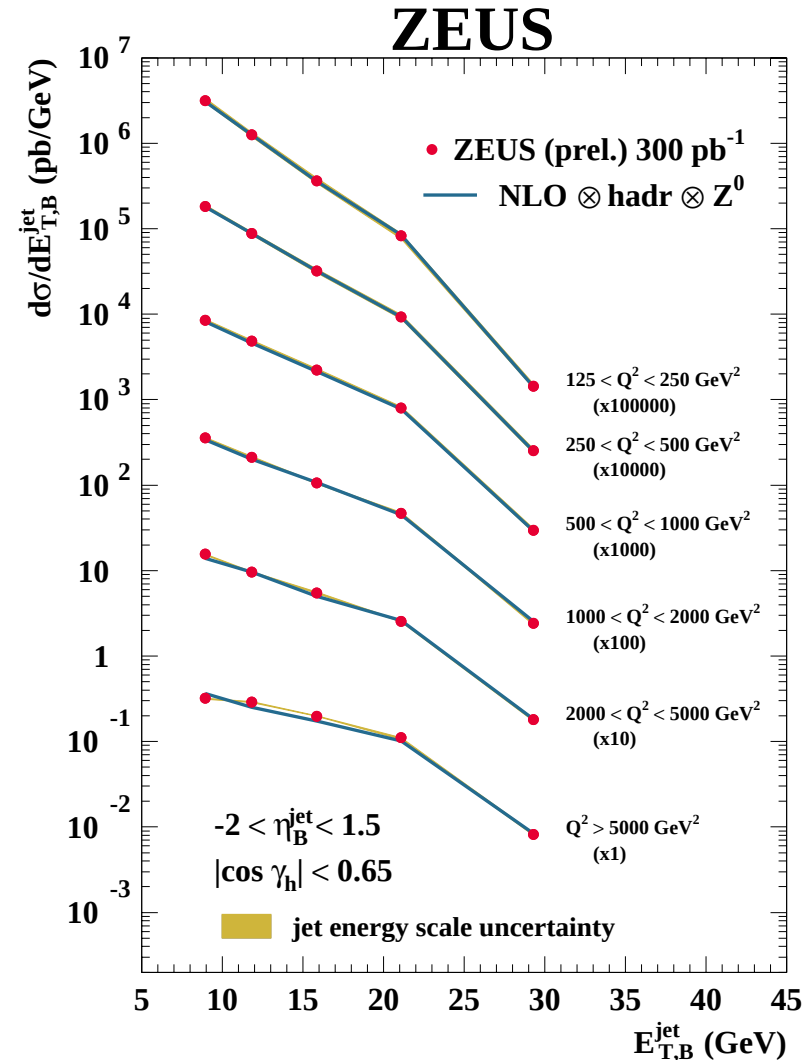
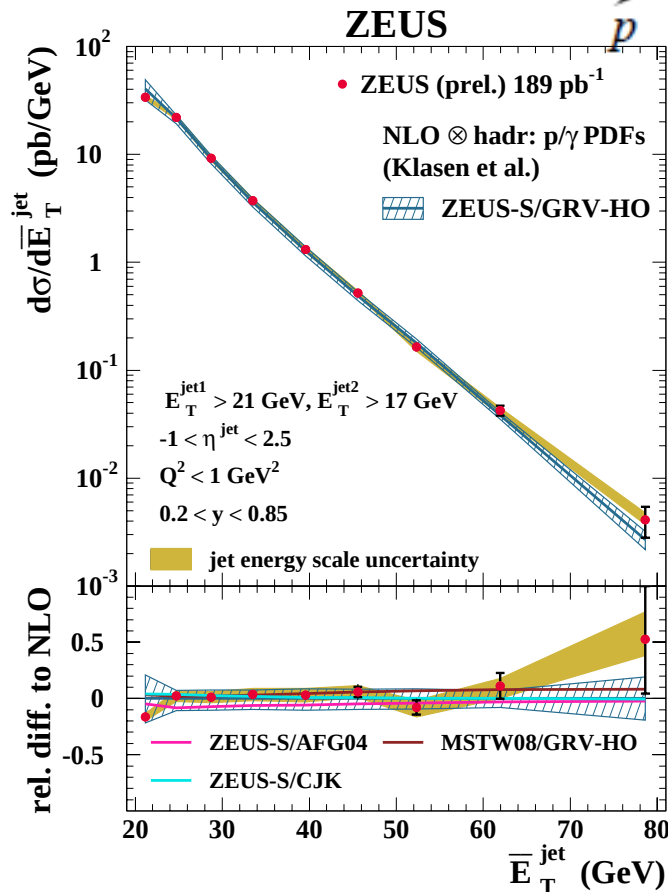
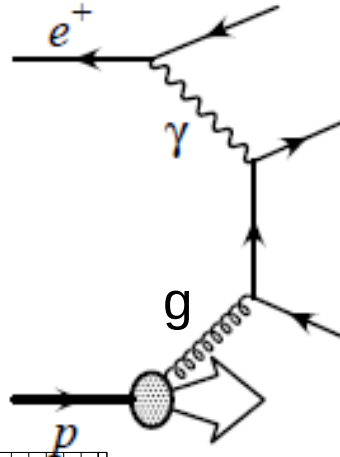
Using HERA I+II combined data.  
Same setting as HERA PDF 1.0.



Uncertainties at the high  $x$  region reduced.

# Inclusive Jet measurements in HERA II

Directly sensitive  
to **gluon density**  
at medium  $x$ .



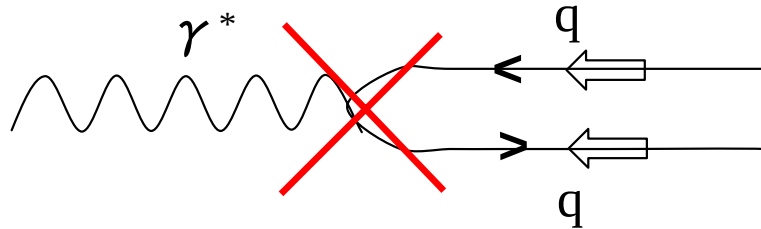
Also allows simultaneous  
constraints of PDFs and  $\alpha_s$ .

# Longitudinal structure function: $F_L$

- $F_L$  is proportional to the cross section of longitudinal photon interacting with proton.

$$F_L \propto \sigma_L$$

- In naïve QPM, proton has co-linear spin  $\frac{1}{2}$  quarks only.



Longitudinal photon cannot interact with a quark  $\rightarrow F_L = 0$

- gluon emission in the proton  $\rightarrow F_L \neq 0$   
i.e.  $F_L$  directly reflects gluon dynamics in the proton.

$$\text{In pQCD: } F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[ \frac{16}{3} F_2 + 8 \sum_q e_q^2 \left( 1 - \frac{x}{z} \right) z g(z) \right]$$

gluon PDF

Measurement of  $F_L$  is good test for the current understanding of proton structure and QCD.

# Measurement of $F_L$

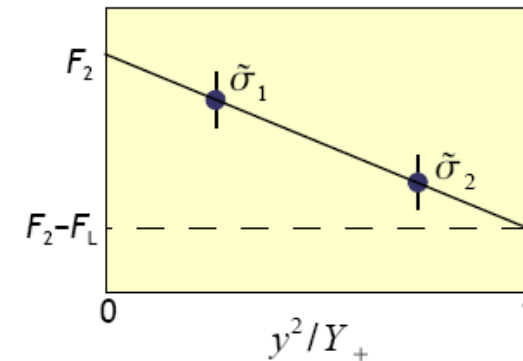
- Measured cross section is a combination of  $F_2$  and  $F_L$ .

At low  $Q^2$   $\tilde{\sigma}(e^\pm p) = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$   $Y_+ = 1 + (1 - y^2)$   
 $\rightarrow 1 < Y_+ < 2$

- Separation of  $F_L$  from  $F_2$ .

Cross sections at the same  $(x, Q^2)$  but the different  $y$

$y = \frac{Q^2}{sx}$   $\rightarrow$  multiple beam energies



HERA was successfully operated with low  $E_p$  for its last months.

Data sets with three different energy are available.

$\sqrt{s} = 318, 252, 225 \text{ GeV}$  ( $E_p = 920, 575, 460 \text{ GeV}$ )

$\rightarrow$  Direct  $F_L$  measurements at low  $x$  ( $x: 10^{-4} \sim 10^{-3}$ ) = gluon dominance.

- Extraction of structure functions without QCD assumption
- Consistency check of pQCD framework for the proton structure.

# Reduced cross sec. at $E_p = 460, 575, 920 \text{ GeV}$

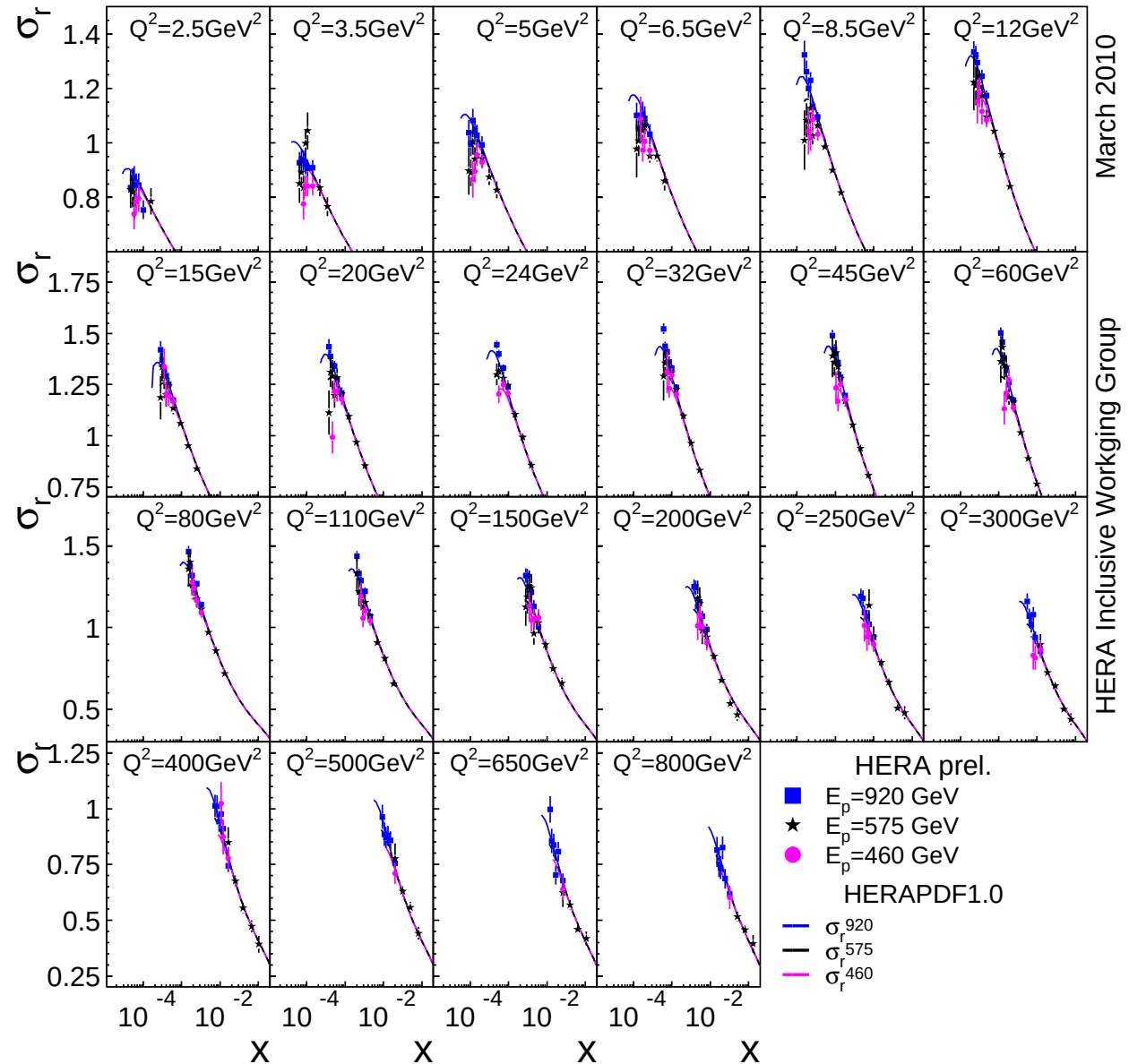
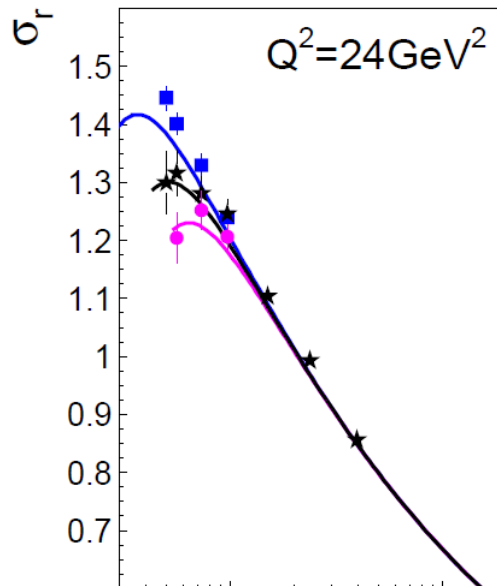
H1 and ZEUS

The data covers

$$0.85 > y > 0.1$$

Difference at low- $x$   
(i.e. high- $y$ )

$\rightarrow F_L$

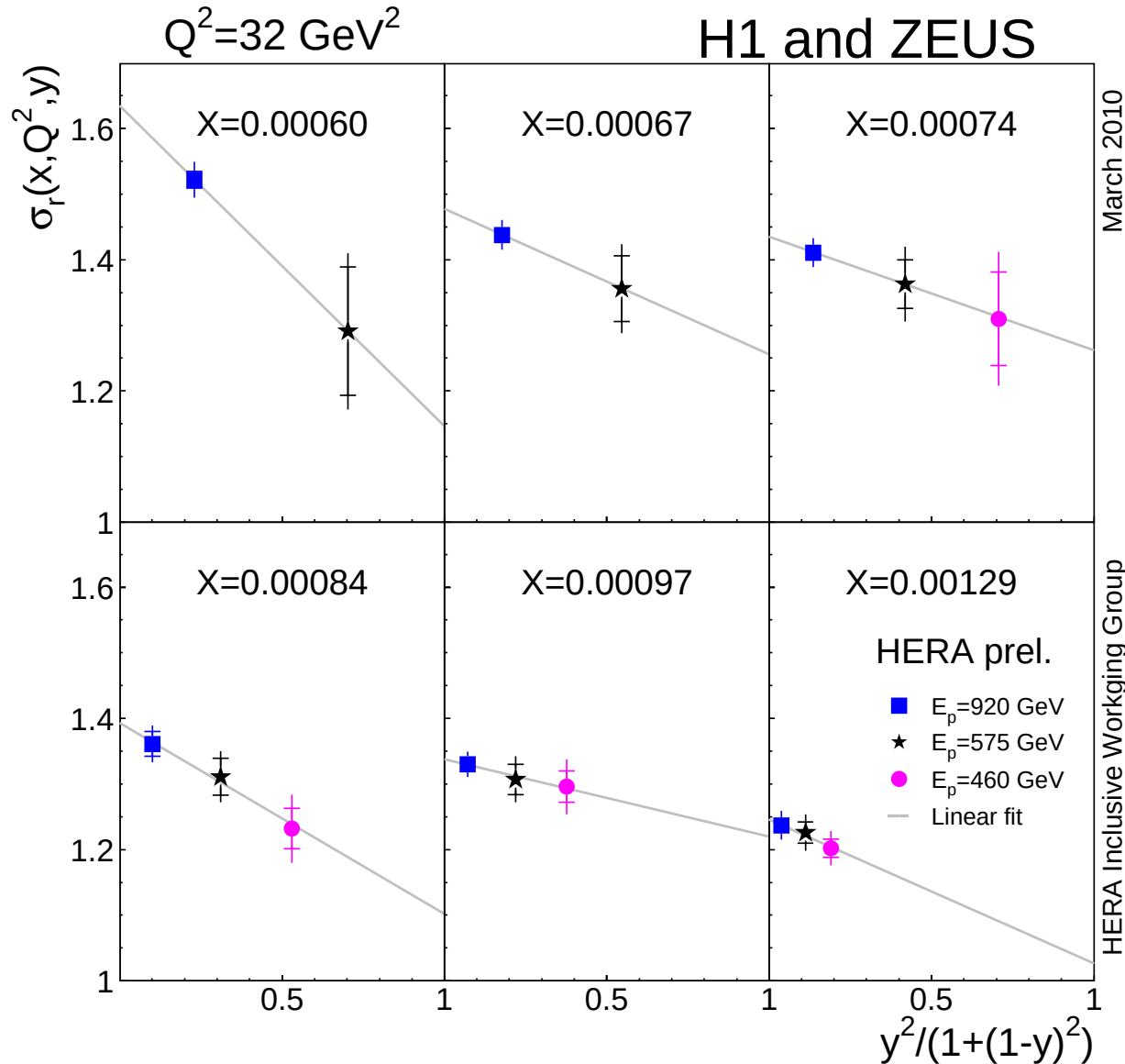


March 2010

HERA Inclusive Working Group

Note: ZEUS covers  $24 < Q^2 < 110 \text{ GeV}^2$ . Still trying to go lower  $Q^2$

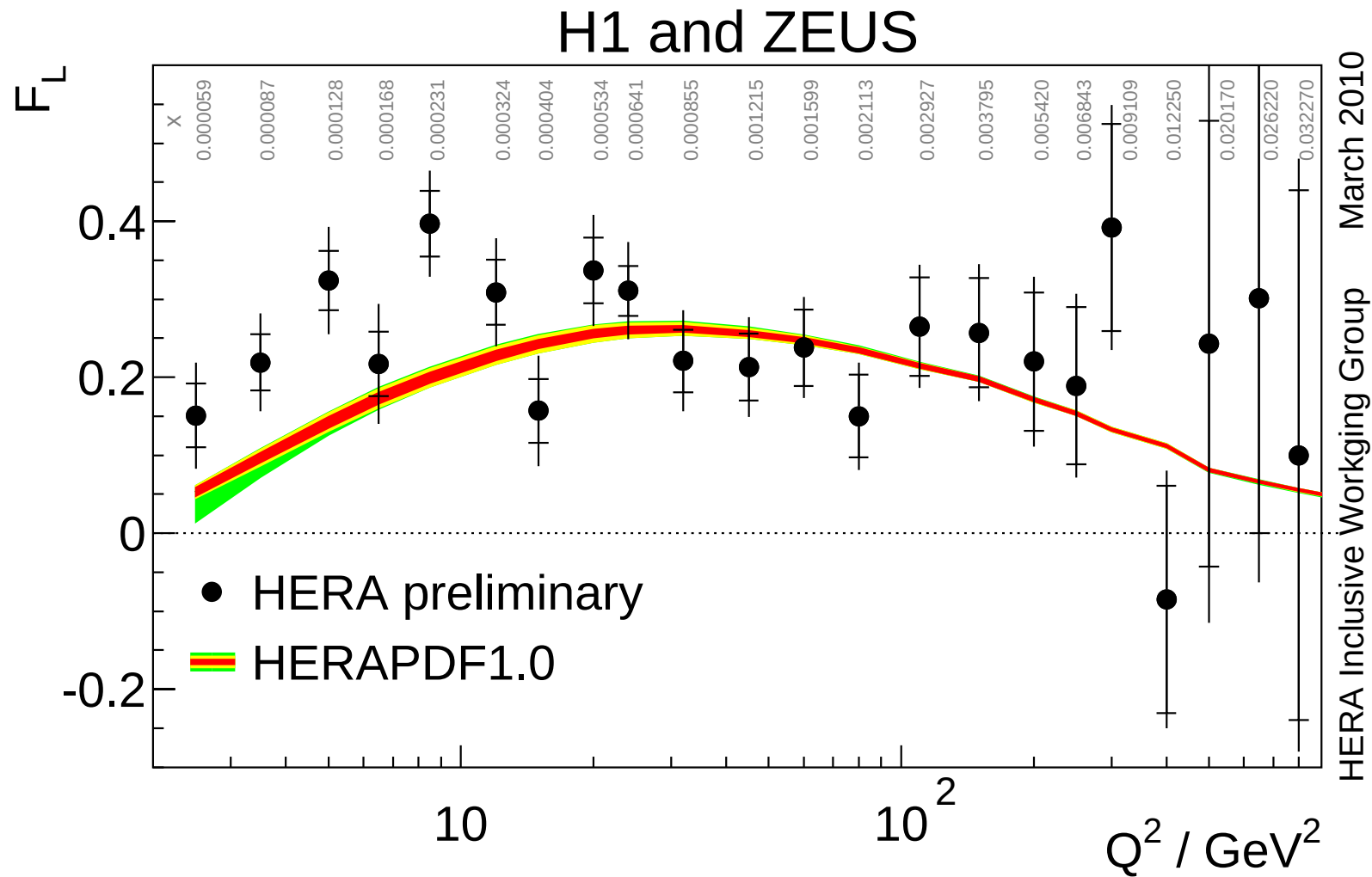
# $F_L$ extraction



$$\tilde{\sigma}(e^\pm p) = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

→ At given  $(x, Q^2)$  bin,  
 $F_L$  should be seen as  
 a negative slope.

# HERA $F_L$



$F_L$ , averaged over  $x$ , for each  $Q^2$  bin

Good agreement between data and prediction for  $Q^2 > 10 \text{ GeV}^2$ .

# Heavy Flavour production

- Dominant process of heavy quark production: **Boson-Gluon-Fusion (BGF)**

- Two schemes to treat heavy quarks in pQCD;

- massive scheme (FFN)

appropriate for  $Q^2 \sim M_q^2$

Heavy quarks are produced via BGF.

→ Sensitive to gluon PDFs

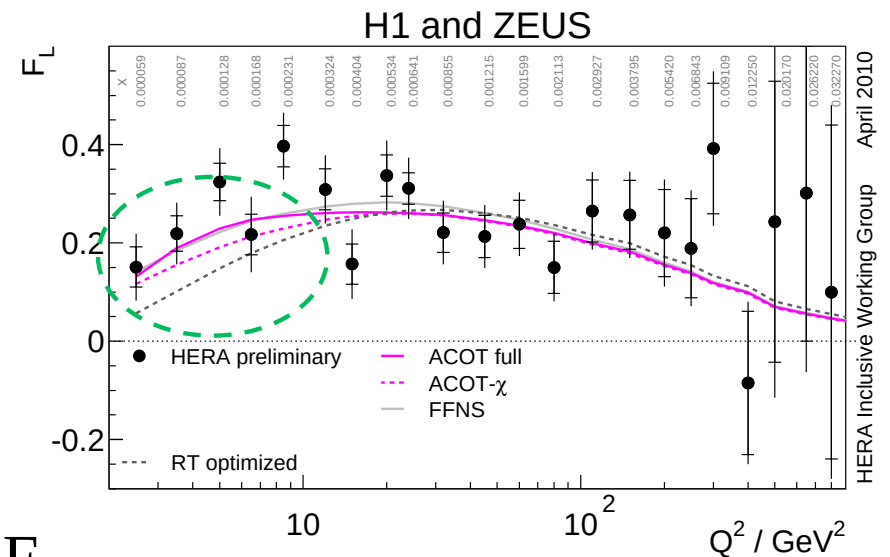
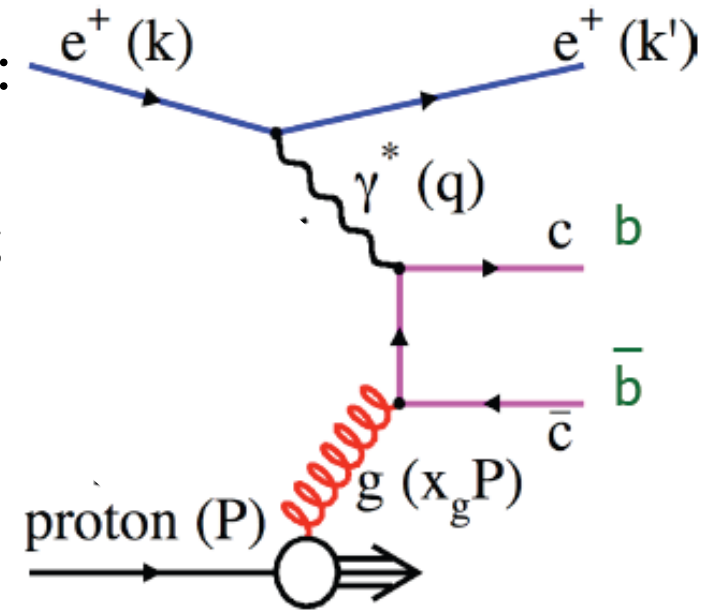
- massless scheme (ZMVFN)

appropriate for  $Q^2 \gg M_q^2$

Heavy quarks are massless and exist in the proton if  $Q^2$  is above the mass threshold.

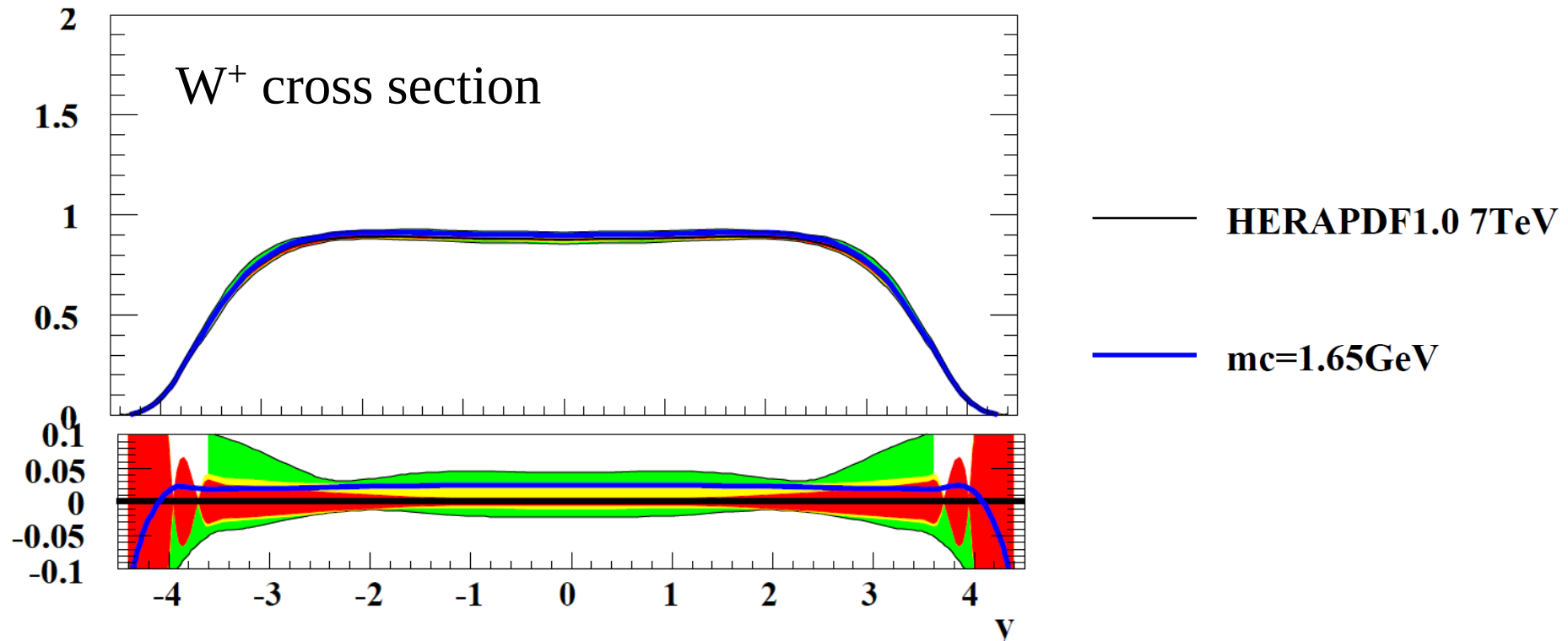
→ Intrinsic heavy quarks' PDFs

May affect on description of low  $Q^2$   $F_L$ .





# Charm mass impact on LHC W cross sec.

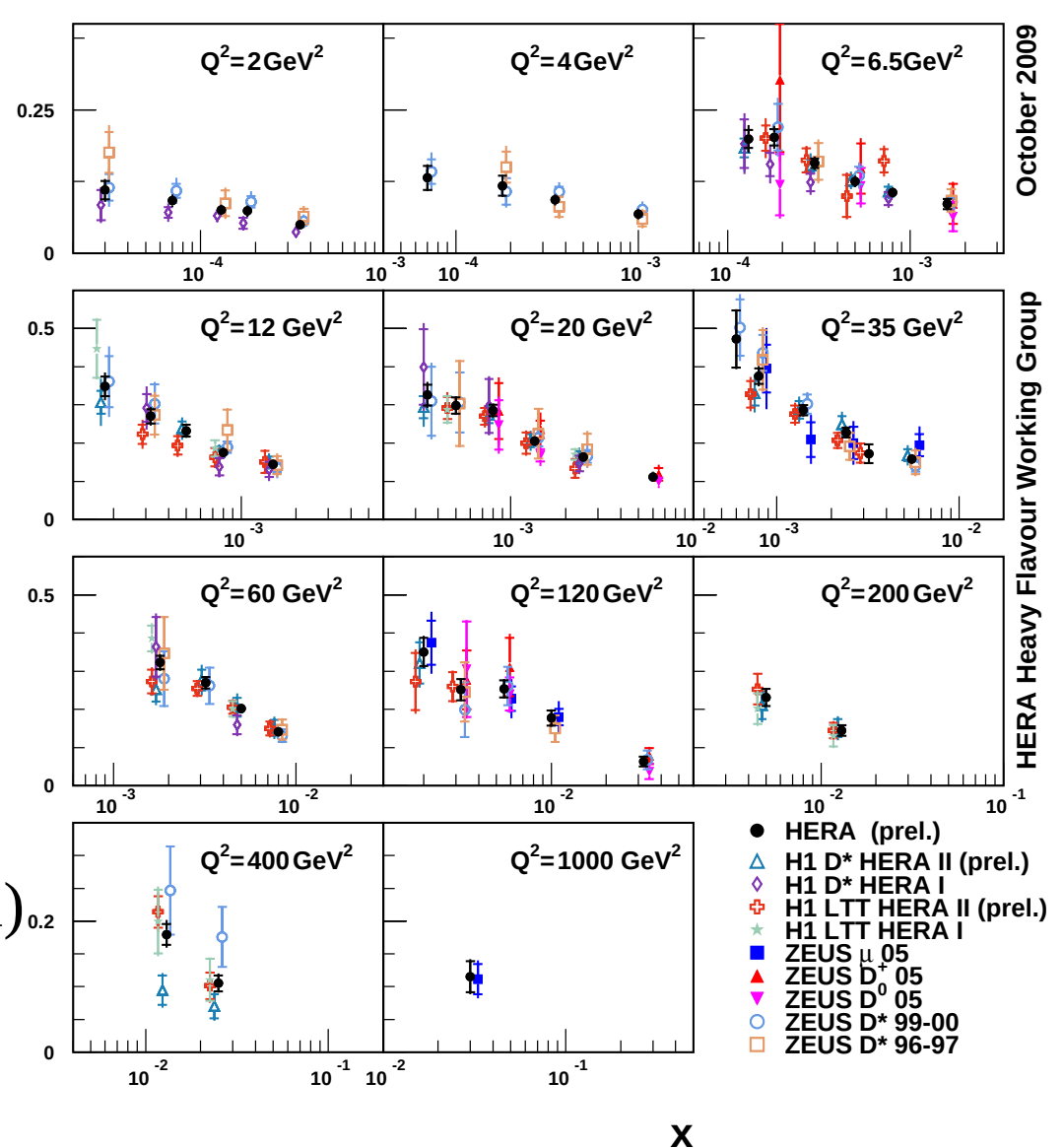


$m_c$ : 1.4 GeV  $\rightarrow$  1.65 GeV.

$m_c$  value in HERA PDF 1.0 does affect on LHC W cross section by  $\sim 3\%$ .

# HERA combined $F_2^{cc}$

- ◆  $F_2^{cc}$  is extracted for large kinematic region.
    - different methods
      - D mesons by slow pions
      - Impact parameter tagging
      - Muons from semi-leptonic decay
    - different data sets
      - HERA I and II (partial)
- Combination gives very precise data.

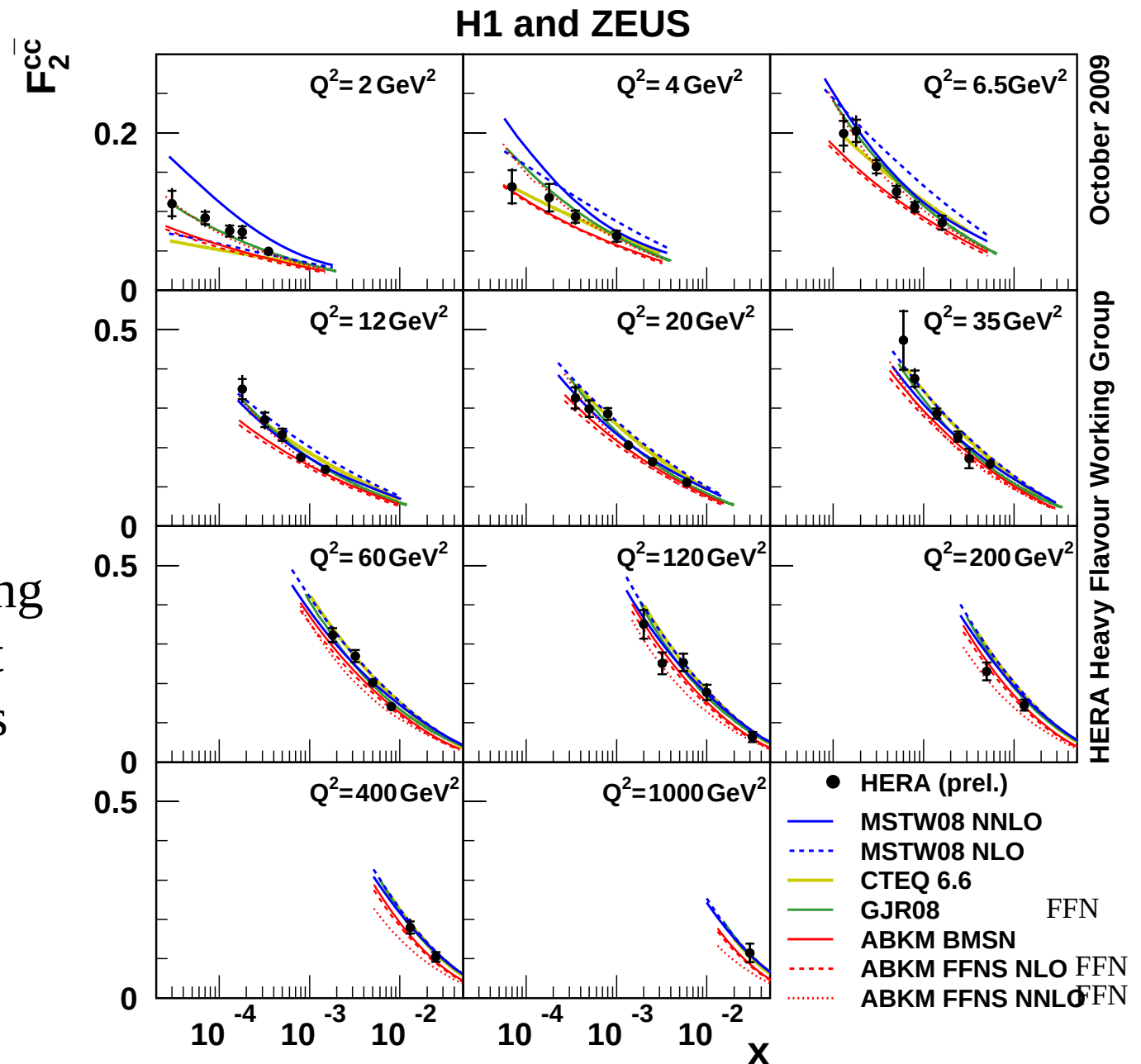


# HERA $F_2^{cc}$

Precision is 5-10%.

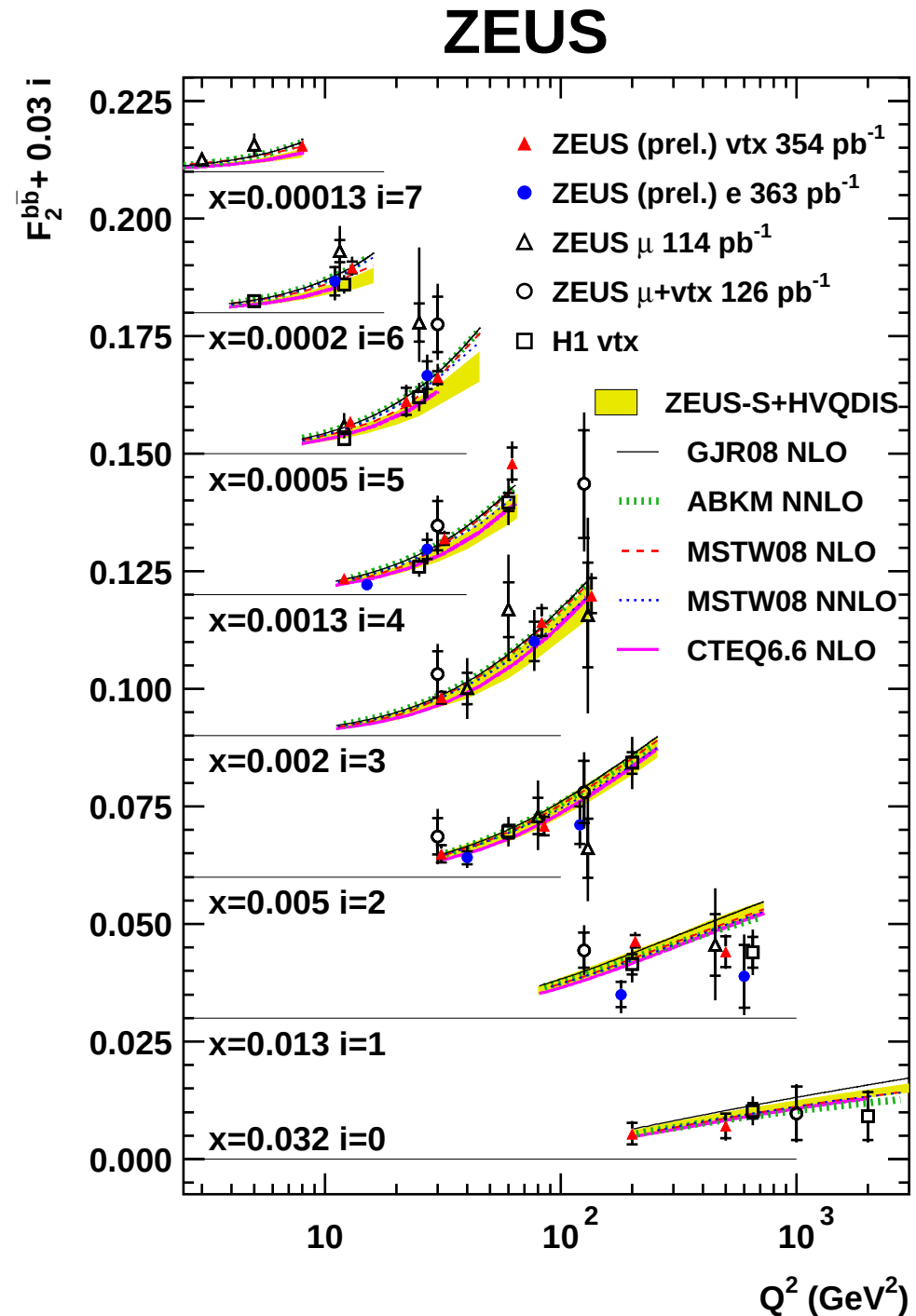
Possible to constrain theory calculation.

→ Better understanding of charm treatment and  $m_c$  in QCD fits can be expected.



# $F_2^{bb}$

- Methods:
  - Impact parameter
  - tagging,  $\mu$  +jet
- Measurements are consistent with each other.
- Combination of H1+ZEUS will provides improved precision



# Summary

HERA results are valuable input for to understand the proton structure.

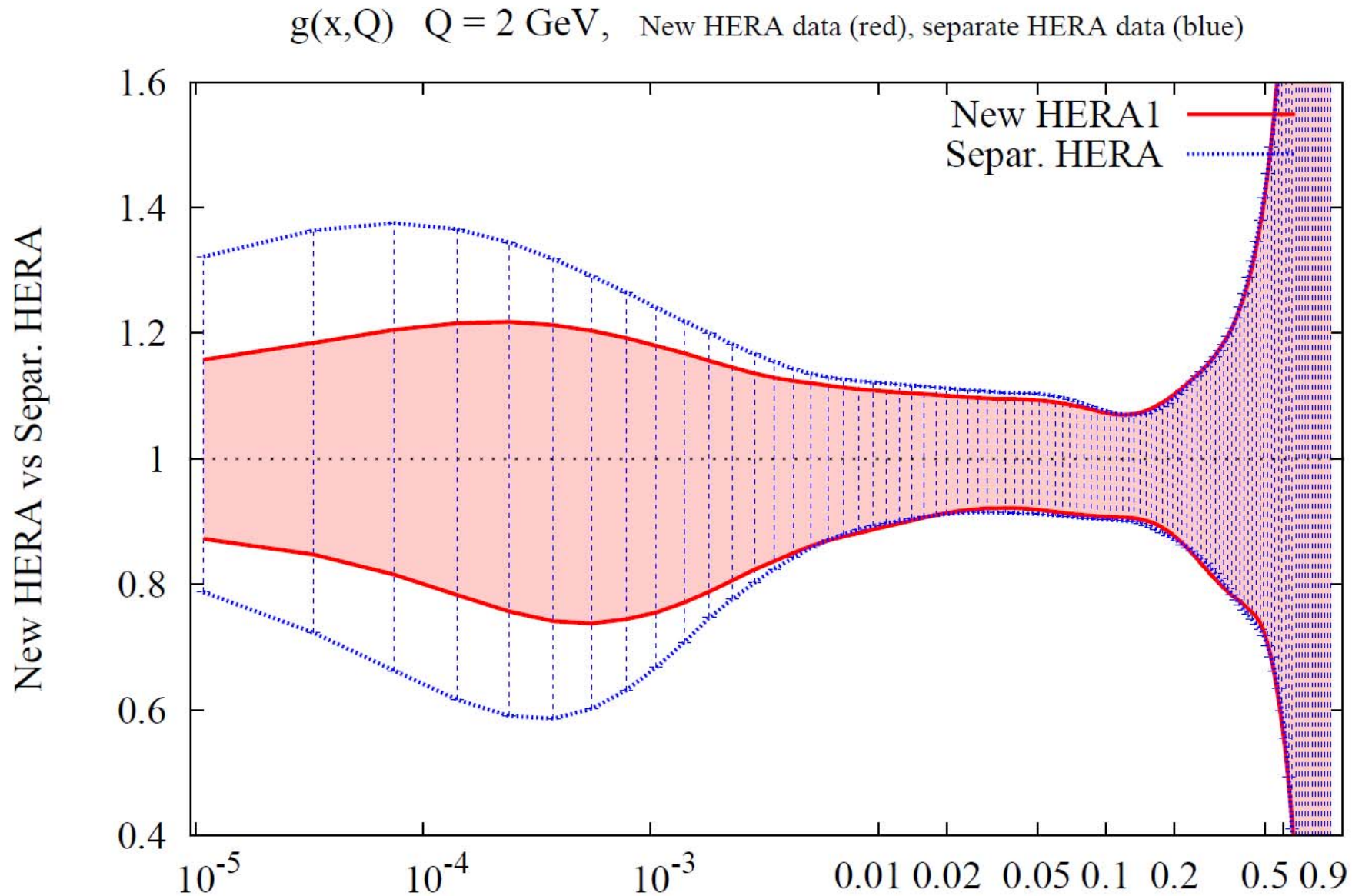
- ◆ Combination of H1 and ZEUS measurements provides very precise data.
  - A very good PDF determination in HERA PDF1.0.
- ◆ Using the full HERA II statistics, the analyses of high- $Q^2$  NC/CC, jets and heavy flavour processes will improve the precision of the results.
  - Further understanding of the proton structure may come.

**Backup**

# Input for HERA I combined data

| Data Set     |       | $x$ Range            |                    | $Q^2$ Range<br>GeV <sup>2</sup> |       | $\mathcal{L}$<br>pb <sup>-1</sup> | $e^+/e^-$ | $\sqrt{s}$<br>GeV |
|--------------|-------|----------------------|--------------------|---------------------------------|-------|-----------------------------------|-----------|-------------------|
| H1 svx-mb    | 95-00 | $5 \times 10^{-6}$   | 0.02               | 0.2                             | 12    | 2.1                               | $e^+p$    | 301-319           |
| H1 low $Q^2$ | 96-00 | $2 \times 10^{-4}$   | 0.1                | 12                              | 150   | 22                                | $e^+p$    | 301-319           |
| H1 NC        | 94-97 | 0.0032               | 0.65               | 150                             | 30000 | 35.6                              | $e^+p$    | 301               |
| H1 CC        | 94-97 | 0.013                | 0.40               | 300                             | 15000 | 35.6                              | $e^+p$    | 301               |
| H1 NC        | 98-99 | 0.0032               | 0.65               | 150                             | 30000 | 16.4                              | $e^-p$    | 319               |
| H1 CC        | 98-99 | 0.013                | 0.40               | 300                             | 15000 | 16.4                              | $e^-p$    | 319               |
| H1 NC HY     | 98-99 | 0.0013               | 0.01               | 100                             | 800   | 16.4                              | $e^-p$    | 319               |
| H1 NC        | 99-00 | 0.0013               | 0.65               | 100                             | 30000 | 65.2                              | $e^+p$    | 319               |
| H1 CC        | 99-00 | 0.013                | 0.40               | 300                             | 15000 | 65.2                              | $e^+p$    | 319               |
| ZEUS BPC     | 95    | $2 \times 10^{-6}$   | $6 \times 10^{-5}$ | 0.11                            | 0.65  | 1.65                              | $e^+p$    | 301               |
| ZEUS BPT     | 97    | $6 \times 10^{-7}$   | 0.001              | 0.045                           | 0.65  | 3.9                               | $e^+p$    | 301               |
| ZEUS SVX     | 95    | $1.2 \times 10^{-5}$ | 0.0019             | 0.6                             | 17    | 0.2                               | $e^+p$    | 301               |
| ZEUS NC      | 96-97 | $6 \times 10^{-5}$   | 0.65               | 2.7                             | 30000 | 30.0                              | $e^+p$    | 301               |
| ZEUS CC      | 94-97 | 0.015                | 0.42               | 280                             | 17000 | 47.7                              | $e^+p$    | 301               |
| ZEUS NC      | 98-99 | 0.005                | 0.65               | 200                             | 30000 | 15.9                              | $e^-p$    | 319               |
| ZEUS CC      | 98-99 | 0.015                | 0.42               | 280                             | 30000 | 16.4                              | $e^-p$    | 319               |
| ZEUS NC      | 99-00 | 0.005                | 0.65               | 200                             | 30000 | 63.2                              | $e^+p$    | 319               |
| ZEUS CC      | 99-00 | 0.008                | 0.42               | 280                             | 17000 | 60.9                              | $e^+p$    | 319               |

# Impact of combined data on CTEQ PDFs



from M. Guzzi, DIS2010, Florence