

News from FormCalc and LoopTools

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The System

FeynArts

Amplitudes

FormCalc

Fortran Code

LoopTools

$$|\mathcal{M}|^2$$

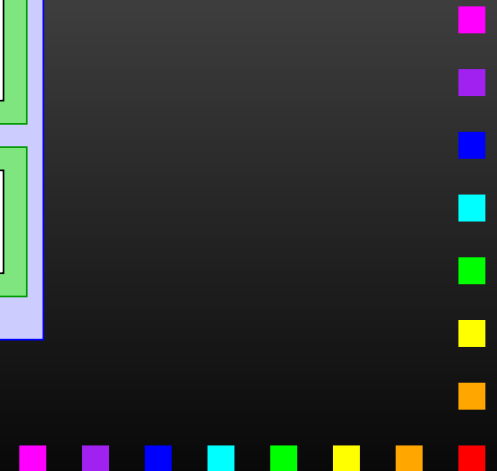
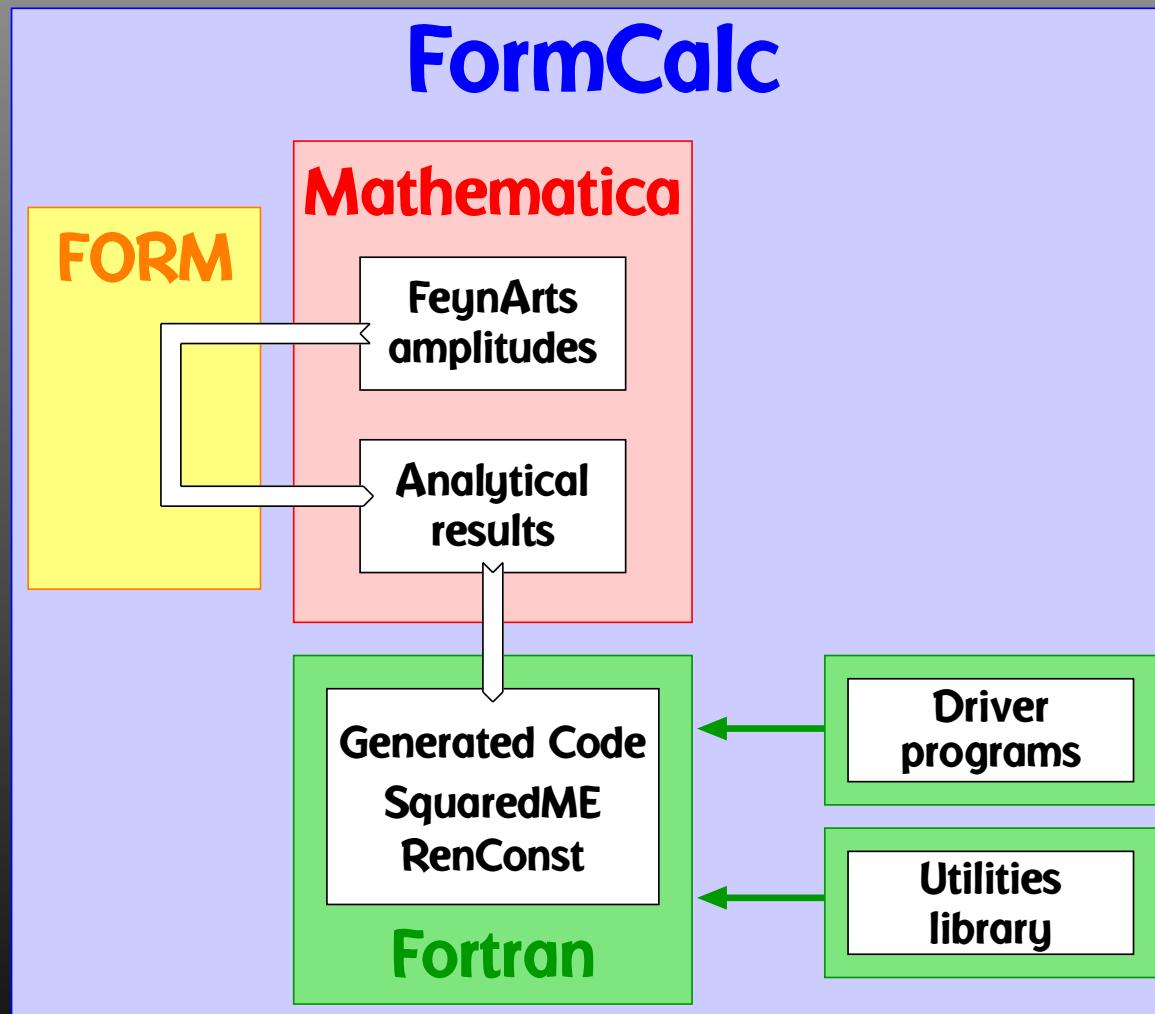
Cross-sections, Decay rates, ...

FormCalc is a matrix-element generator that turns FeynArts amplitudes up to 1-loop into a **Fortran code for computing the partonic squared matrix element.**

The generated code can be run with FormCalc's own driver programs, or used with other 'Frontends', e.g. Monte Carlos.

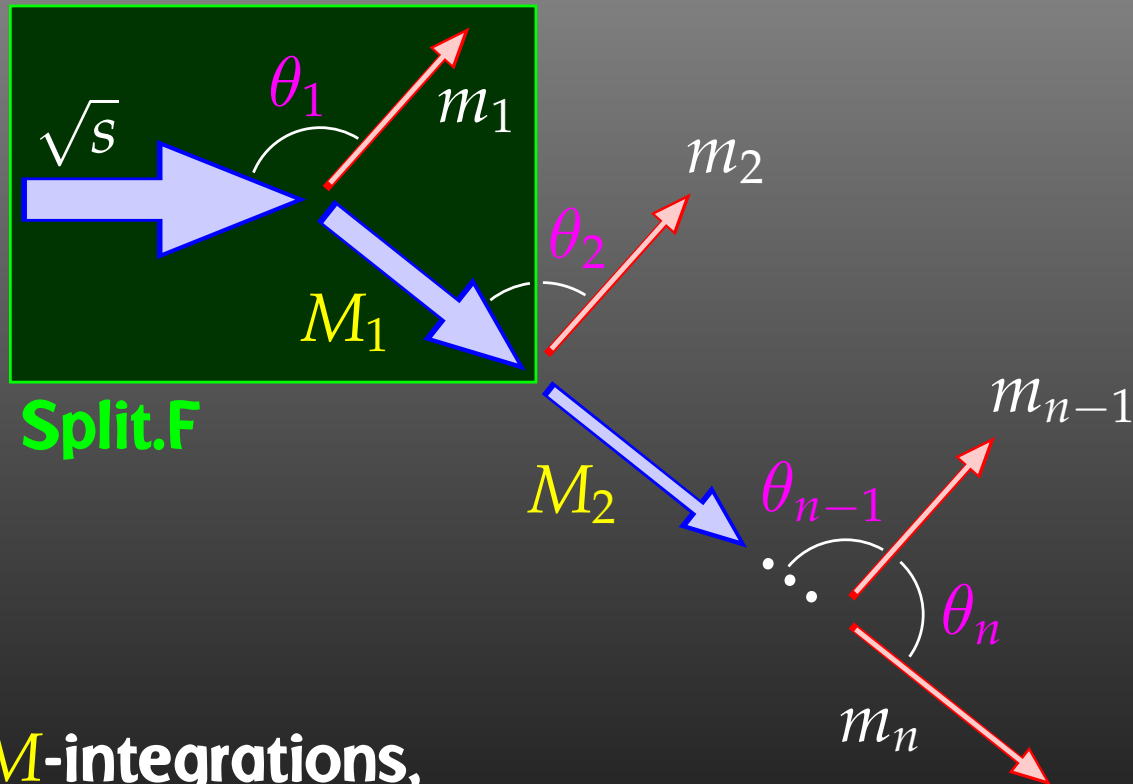


FormCalc Internals

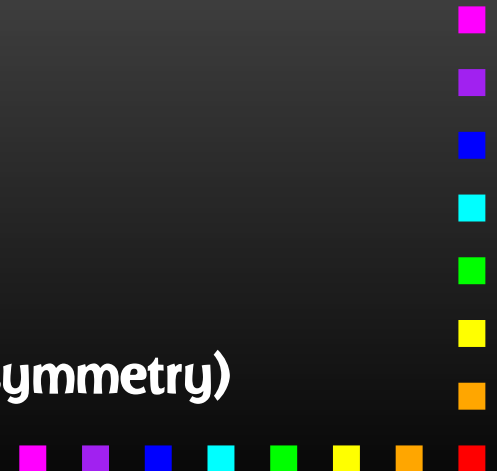


New Kinematics

n -particle phase-space is built up iteratively:



- $(n - 1)$ M -integrations,
- n $\cos \theta$ -integrations,
- n φ -integrations (φ_1 trivial because of axial symmetry)



Phase-space

Explicit phase-space parameterization:

$$\begin{aligned} & \frac{1}{2\sqrt{s}} \int_{m_2+\dots+m_n}^{\sqrt{s}-m_1} dM_1 d\cos\theta_1 d\varphi_1 \frac{k_1}{2} \\ & \times \int_{m_3+\dots+m_n}^{M_1-m_2} dM_2 d\cos\theta_2 d\varphi_2 \frac{k_2}{2} \\ & \vdots \\ & \times \int_{m_n}^{M_{n-2}-m_{n-1}} dM_{n-1} d\cos\theta_{n-1} d\varphi_{n-1} \frac{k_{n-1}}{2} \\ & \times \int d\cos\theta_n d\varphi_n \frac{k_n}{2} \end{aligned}$$

k_i and $\cos\theta_i$ are given in the decay's rest frame.



Verbatim example from 2to3.F

```
p = 0
ex = 0
ey = 0
ez = 1
minv = sqrtS
msum = MASS3 + MASS4 + MASS5
```

```
call Split(5, dble(MASS5), p, ex, ey, ez, minv, msum,
& fac, key, Var(XMREM5), Var(XCOSTH5), Var(TRIVIAL))
```

```
call Split(4, dble(MASS4), p, ex, ey, ez, minv, msum,
& fac, 0, Var(FIXED), Var(XCOSTH4), Var(XPHI4))
```

```
call VecSet(3, dble(MASS3), p, ex, ey, ez)
```

**The X in XMREM5 refers to the ratio, i.e. XMREM5 runs from 0 to 1.
The integration borders are determined internally by Split.**



Variables

FormCalc 5 contains a new homogeneous system for all (potential) integration variables. Each variable is referred to by a preprocessor constant, e.g. SQRTS or XCOSTH.

- $\text{Var}(v)$ = the actual value of v .
- $\text{Show}(v)$ = the value printed in the output – to print e.g. t instead of $\cos \theta$.
- $\text{Lower}(v)$, $\text{Upper}(v)$, $\text{Step}(v)$ = the lower limit, upper limit, and step width of v . If the step is zero, the cross-section is integrated over v .
- $\text{CutMin}(v)$, $\text{CutMax}(v)$ = the lower and upper cuts on v .

Two special variables: **FIXED** for fixed values and **TRIVIAL** for trivial integrations.



Cuts

Split allows to place cuts on each M and $\cos \theta$ integration. The φ integration is not modified in the present setup.

Cuts restricting M_i

Cut on	Key
M_i	CUT_MREM
E_i	CUT_MREM_E
k_i	CUT_MREM_K
$E_{T,i}$	CUT_MREM_ET
$k_{T,i}$	CUT_MREM_KT
y_i	CUT_MREM_RAP
η_i	CUT_MREM_PRAP

Cuts restricting $\cos \theta_i$

Cut on	Key
$\cos \theta_i$	CUT_COSTH
$\cos \hat{\theta}_i$	CUT_COSTHCMS
E_i	CUT_COSTH_E
k_i	CUT_COSTH_K



Application of Cuts

```
key = 0
```

```
#ifdef E5MIN
```

```
    CutMin(XMREM5) = E5MIN
```

```
    key = key + Cut(CUT_MREM_E, CUT_MIN)
```

```
#endif
```

```
#ifdef COSTH5CUT
```

```
    CutMin(XCOSTH5) = -(1 - COSTH5CUT)
```

```
    CutMax(XCOSTH5) = +(1 - COSTH5CUT)
```

```
    key = key + Cut(CUT_COSTH, CUT_MIN + CUT_MAX)
```

```
#endif
```

```
    call Split(5, dble(MASS5), p, ex, ey, ez, minv, msum,  
&    fac, key, Var(XMREM5), Var(XCOSTH5), Var(TRIVIAL))
```

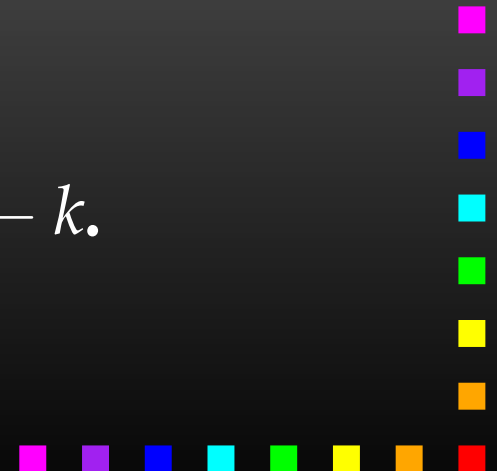
```
    ...
```



Kinematical Information

Kinematical information is available for each external particle:

- `momspec(SPEC_M, i)` - **mass** m ,
- `momspec(SPEC_E, i)` - **energy** E ,
- `momspec(SPEC_K, i)` - **momentum** k ,
- `momspec(SPEC_ET, i)` - **transverse energy** E_T ,
- `momspec(SPEC_KT, i)` - **transverse momentum** k_T ,
- `momspec(SPEC_RAP, i)` - **rapidity** y ,
- `momspec(SPEC_PRAP, i)` - **pseudo-rapidity** η ,
- `momspec(SPEC_DELTAK, i)` - **the difference** $E - k$.

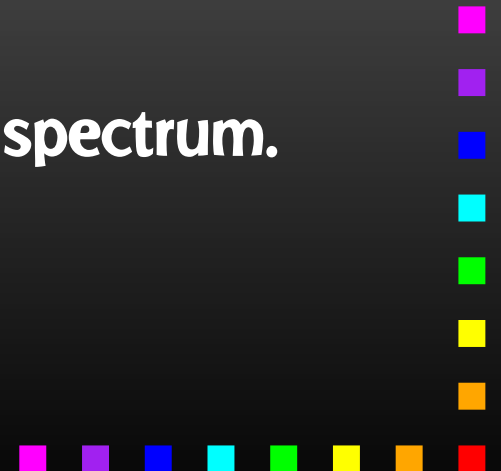


Convolution

With the new variable system, the **Convolution with arbitrary PDFs** can easily be achieved.

Three modules are already included in FormCalc 5:

- `lumi_parton.F` = initial-state partons
= no convolution.
- `lumi_hadron.F` = initial-state hadrons
= convolution with hadronic PDFs
from the LHAPDF library.
- `lumi_photon.F` = initial-state photons
= convolution with CompAZ spectrum.



Modularity

As before, the two files `process.h` and `run.F` direct the choice of parameters and include one each of

`1to2.F`

`2to2.F`

`2to3.F`

`lumi_parton.F`

`lumi_hadron.F`

`lumi_photon.F`

`model_sm.F`

`model_mssm.F`

`model_thdm.F`

There is virtually **no cross-talk** between different modules which are in that sense ‘universal.’

```
-rw-r--r-- 1 hahn users 1501 2005-09-13 08:55 1to2.F
-rw-r--r-- 1 hahn users 1652 2005-09-13 08:56 2to2.F
-rw-r--r-- 1 hahn users 2153 2005-09-13 08:55 2to3.F
-rw-r--r-- 1 hahn users 2003 2005-06-06 15:17 lumi_hadron.F
-rw-r--r-- 1 hahn users 829 2005-06-06 15:17 lumi_parton.F
-rw-r--r-- 1 hahn users 1353 2005-06-06 15:18 lumi_photon.F
-rw-r--r-- 1 hahn users 5944 2005-05-31 09:31 model_sm.F
-rw-r--r-- 1 hahn users 21460 2005-10-01 09:43 model_mssm.F
-rw-r--r-- 1 hahn users 3647 2005-05-13 13:52 model_thdm.F
```



Code Reusability

The main program in FormCalc 5 only scans the command line and invokes

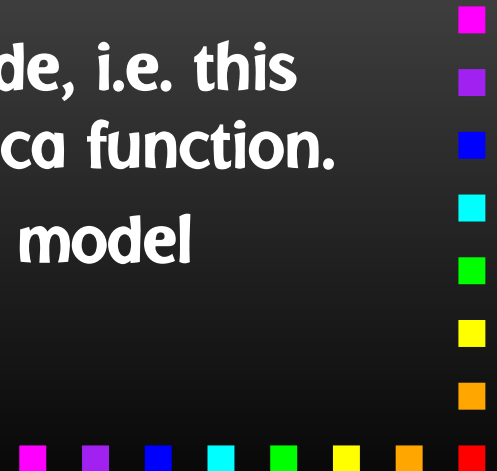
```
call ProcessIni(...)  
call ParameterScan(...)
```

All further action is decoupled from the main program and can **easily be called from any program**. It is thus straightforward to use FormCalc-generated code in own programs.

Planned application:

Mathematica Interface for FormCalc-generated code, i.e. this makes the cross-section available as a Mathematica function.

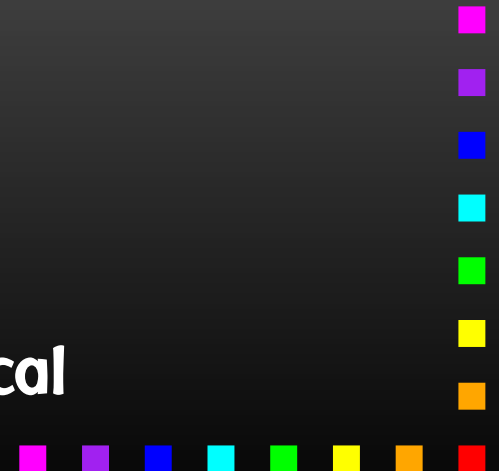
Example use: Find minimum of cross-section w.r.t. model parameters using Mathematica's `FindMinimum`.



FormCalc Summary

New FormCalc Features:

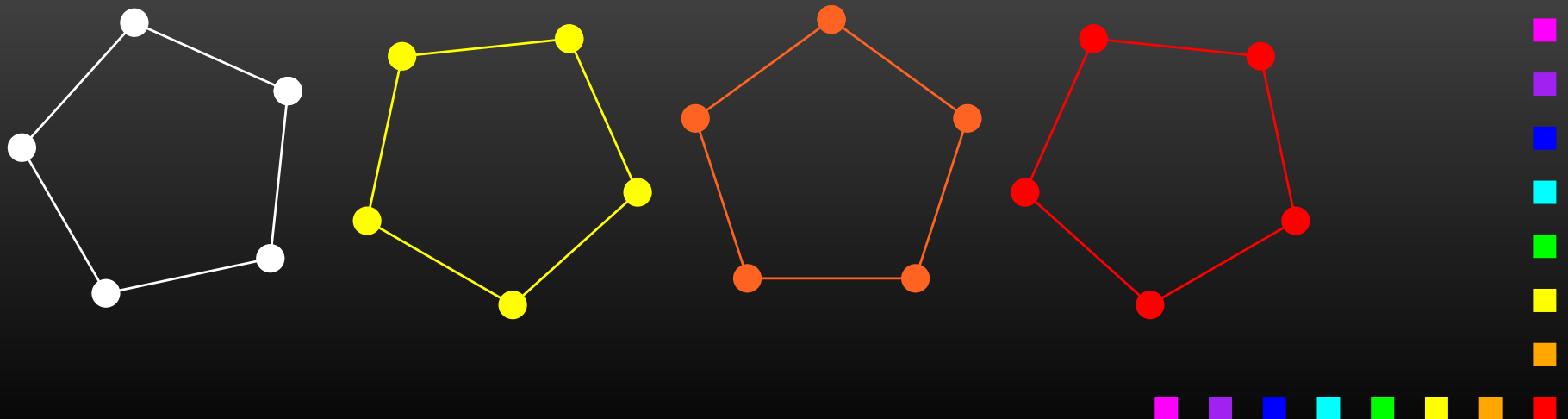
- **New kinematics routines** can build up arbitrary phase-spaces with a wide range of cuts possible.
- **Better modularity:** almost no cross-talk between modules. Calling FormCalc code from other programs is straightforward.
- **Convolution** with arbitrary distribution functions included:
 - ▷ partons (no convolution),
 - ▷ hadrons (links with LHAPDF library),
 - ▷ photons (uses CompAZ).
- **Uniform variable system** + detailed kinematical information for all external legs.



LoopTools 2.2

LoopTools is a library for the one-loop integrals. It is based on FF and has a Fortran, C/C++, and Mathematica interface. It is referenced by the FormCalc-generated code.

- The **five-point family of functions** (scalar + tensor coefficients) have been implemented by M. Rauch, in both the Denner/Dittmaier and the Passarino/Veltman decomposition for comparison.



Bget

The **two-point functions have been united** into the Bget function which works similar to its Cget, Dget, and Eget counterparts, in particular it caches its results.

The reason is mainly **Cache Efficiency** in view of the five-point decomposition:

Eget $\xrightarrow{\text{calls}}$ 5 Dget $\xrightarrow{\text{call}}$ (5 · 4) Cget $\xrightarrow{\text{call}}$ (5 · 4 · 3) Bget

Also new: **Cache lookups use a binary search method.**

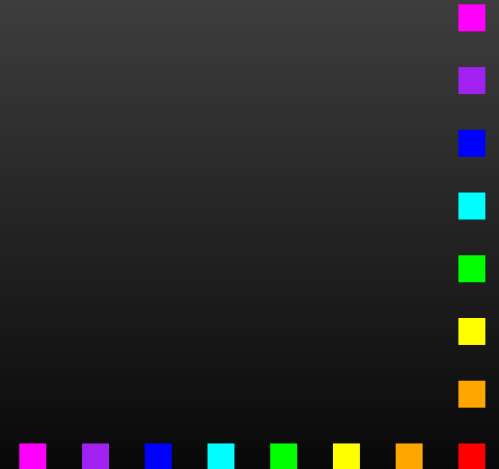
Compatibility routines for the old B0, B1, etc. are of course available.



Complex Versions

Versions of the LoopTools functions for **Complex Parameters** have been added as far as they are contained in FF, i.e. currently only some special cases for the complex D_0 are implemented.

B0i, Bget	CB0i, CBget
C0i, Cget	CC0i, CCget
D0i, Dget	CD0i, CDget
E0i, Eget	CE0i, CEget



Alternate Versions

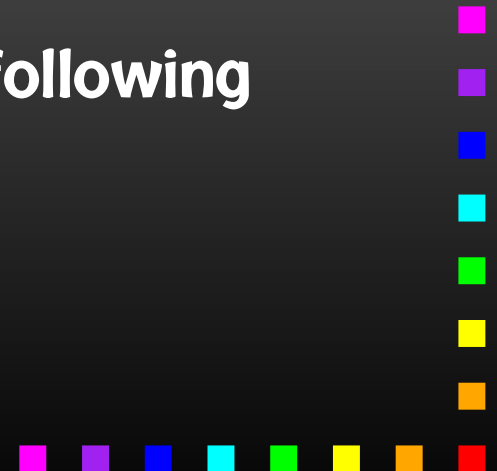
For some functions **alternate versions** exist, most of which are based on an implementation by Denner. The user can choose **at run-time** which version to use, and whether checking is performed. This is determined by the **Version Key**:

- 0*key compute version 'a' (mostly FF),
- 1*key compute version 'b' (mostly Denner),
- 2*key compute both, compare, return 'a',
- 3*key compute both, compare, return 'b'.

Alternate versions are currently available for the following functions: A0, Bget, C0, D0, Eget, CEget.

Example:

```
call setversionkey(2*KeyD0 + 3*KeyBget)
```



Command-line Interface

The new **Command-line Interface** is useful in particular for testing and debugging.

It lists the N -point scalar and tensor coefficients corresponding to the number of arguments, i.e. 3 arguments = B, 6 arguments = C, etc.

```
> lt 500 80.4 91.1887
p      = 500.00000000000000
m1     = 80.400000000000001
m2     = 91.188700000000000
=====
      FF 2.0, a package to evaluate one-loop integrals
      written by G. J. van Oldenborgh, NIKHEF-H, Amsterdam
      =====
      for the algorithms used see preprint NIKHEF-H 89/17,
      'New Algorithms for One-loop Integrals', by G.J. van
      Oldenborgh and J.A.M. Vermaseren, published in
      Zeitschrift fuer Physik C46(1990)425.
      =====
bb0     = (-3.162048481416085,1.760724049383876)
bb1     = (1.594933518284790,-0.8613661011403501)
bb11    = (-7.269245396361010,-23.04426716231248)
bb00    = (-1.086060618894423,0.4674785644394271)
bb001   = (5.154082369023078,11.27351589602220)
bb111   = (0.8310364075655215,-0.2737898598156348)
dbb0    = (-3.5481451611823340E-003,3.8420899025032380E-003)
dbb1    = (1.7079741517372242E-003,-1.9175856430236573E-003)
dbb00   = (0.2544364496951837,-0.1969437683504615)
dbb11   = (-7.6724543502407716E-004,1.2584010742473584E-003)

total number of errors and warnings
=====
fferr: no errors
```



LoopTools Caches

With the addition of new functions, the internal caching mechanism is now used on:

`Bcache` `Ccache` `Dcache` `Ecache`
`CBcache` `CCcache` `CDcache` `CEcache`

Obviously the former system with `getcachelast` and `setcachelast` is no longer practicable for all those caches.

The new cache-management functions operate on all caches simultaneously:

- call `clearcache` - clears all caches.
- call `markcache` - marks the current position.
- call `restorecache` - reverts to the last marked position.



LoopTools Summary

New LoopTools features:

- **Scalar 5-point function plus tensor coefficients available** (thanks to M. Rauch).
- **Complex versions** available as far as implemented in FF.
- **Checking can be enabled at run time**, individually for all integrals which have alternate versions.
- **Extended and improved cache system.**
- **Command-line interface.** Useful for testing and debugging.
- **Better internal accuracy** in the tensor reduction. Uses LU-decomposition + quadruple precision at strategic points, available with (free) Intel ifort.

