

Complementarity of T2K/HK with Other Longer Baseline Experiments

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The purpose of this talk is to motivate to enforce the synergetic activities among the future long baseline (LBL) experiments.

The speaker is not a member of LBL experiments. Therefore, an objective view may be provided as a bystander.

The discussion is conceptual one and the used parameter values are rough. There might be errors or misunderstandings.

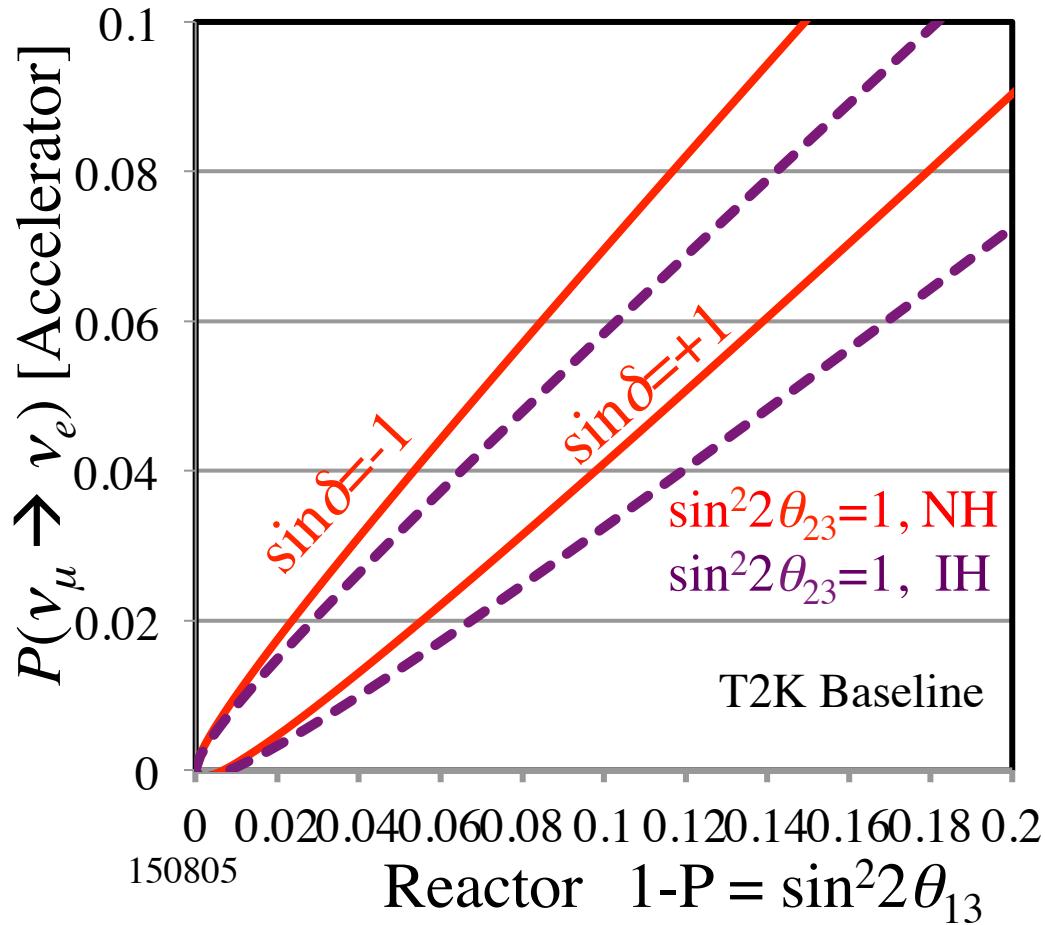
Flow of this talk

- * ~~Purpose of this talk~~
- * Example of a successful synergy
- * $P(\nu_\mu \rightarrow \nu_e)$ and A_{CP} with matter effect
- * Possible synergies
- * Conclusion

An example of successful synergy:

The complementarity between Accelerator and Reactor

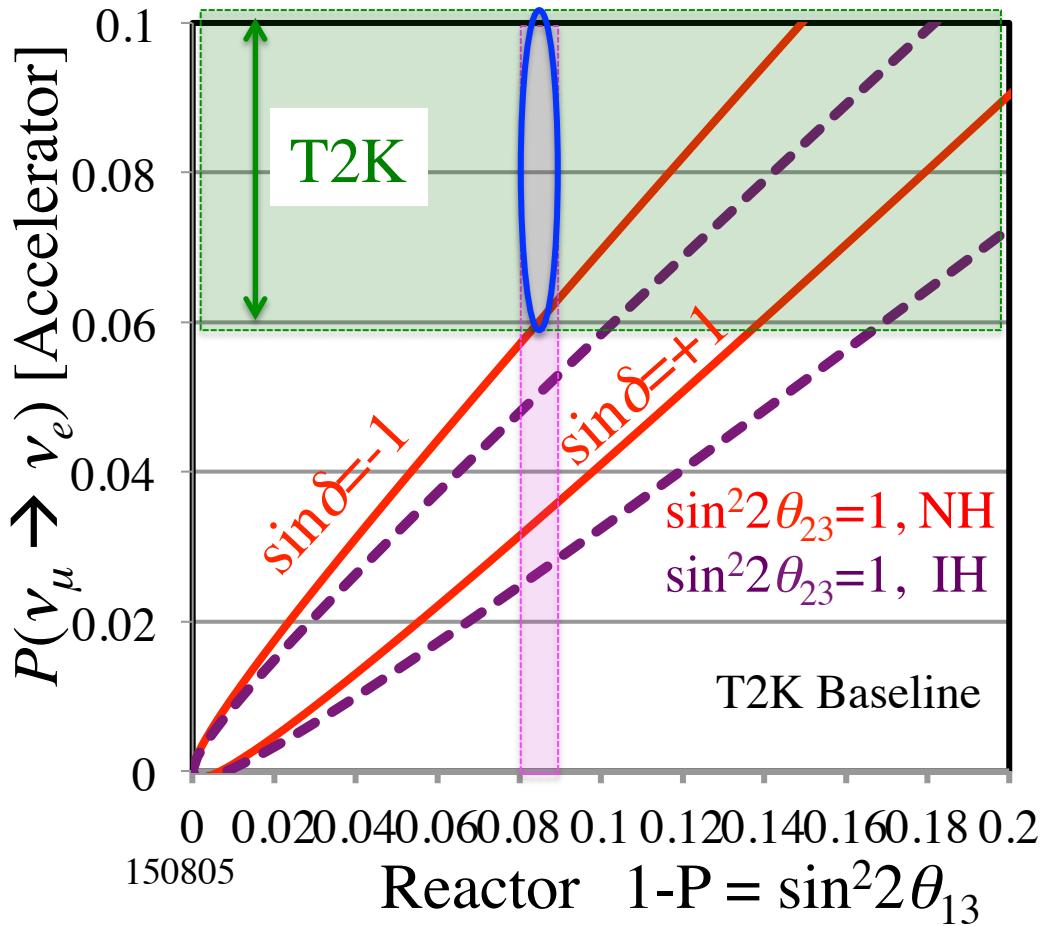
$$P(\nu_\mu \rightarrow \nu_e; \Phi_{31} = \pi/2) \sim \frac{\sin^2 2\theta_{13}}{2(1 - (L/L_0))^2} - 0.043 \frac{\sin 2\theta_{13}}{1 - (L/L_0)} \sin \delta$$



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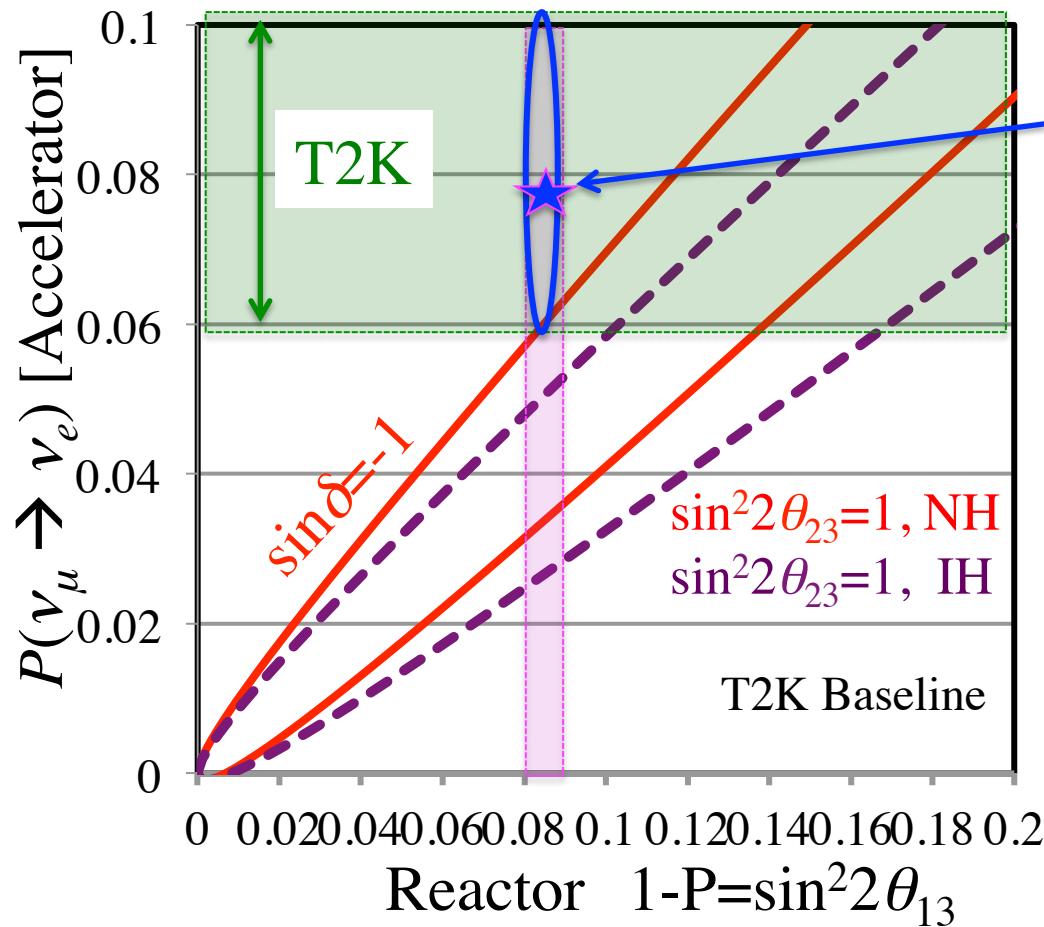


The synergy of Reactor and Accelerator has given us hints of large $\sin \delta$ & Normal hierarchy,

An example of successful synergy:

The complementarity between Accelerator and Reactor

$$P_{31}(\nu_\mu \rightarrow \nu_e; \Phi_{31} = \pi/2) \sim \frac{\sin^2 2\theta_{13}}{2(1 - (L/L_0))^2} - 0.043 \frac{\sin 2\theta_{13}}{1 - (L/L_0)} \sin \delta$$



By the way ...
The center value is in
the unphysical region now.
T2K: Please shrink the
error.
Nova: What is your result?
Double Chooz will check
the **DB & RENO** results
soon with the near detector.

→ Redundancy is
important

CP Asymmetry

* Difference between $P(\nu_\alpha \rightarrow \nu_\beta)$ and $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$

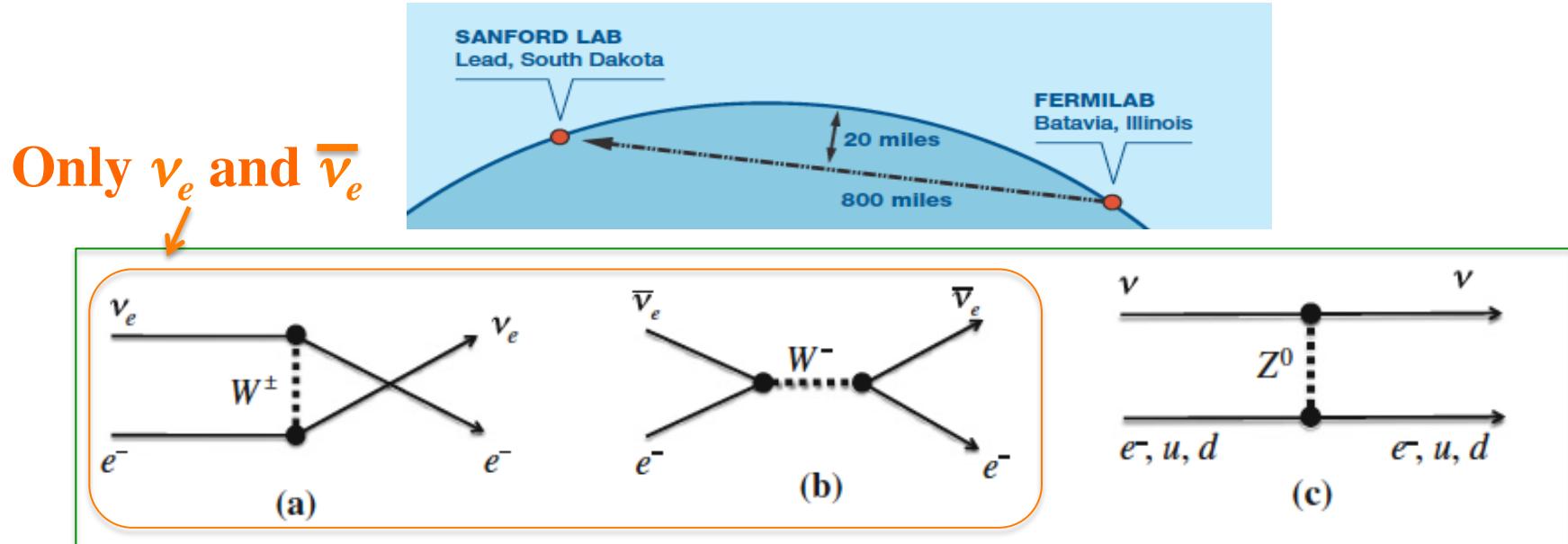
* Experimentally:

$$A_{CP}(@\Phi_{31} = \pi/2) = \frac{P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}{P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}$$
$$\sim -\left| \frac{\Delta m_{12}^2}{\Delta m_{31}^2} \right| \frac{\pi \sin 2\theta_{12}}{\tan \theta_{23} \sin 2\theta_{13}} \sin \delta \sim \underline{-0.29} \sin \delta$$

Thanks to the all experiments, this coefficients can be calculated now.
(synergies!)

* However, the matter effect introduces a fake A_{CP}

Matter (MSW) Effect



Effective Weak Potential

$$V_W = 2\sqrt{2}E_\nu \frac{n_e G_F}{m_3^2 - m_1^2}$$

Energy dependent

changes the coupling sign
depending on ν or $\bar{\nu}$

changes sign depending on
the mass hierarchy

Baseline Dependence of the Matter Effect

At the oscillation maximum;

$$\Phi_{31} = \frac{|\Delta m_{31}^2| L}{4E_\nu} = \frac{\pi}{2}$$

the weak potential can be expressed by using the baseline L ,

$$V_W = \frac{2\sqrt{2}E_\nu G_F \bar{n}_e}{m_3^2 - m_1^2} = \pm \frac{L}{\pi/\sqrt{2} G_F \bar{n}_e} = \pm \frac{L}{L_0} \sqrt{\frac{\rho}{n_e}}$$

M.H.

Reference Baseline: $L_0 = \frac{\pi G_F}{\sqrt{2}} \frac{1}{L} \int_0^L n_e dl \sim \pm 5,500 \text{ km}$

$(\rho=3[\text{g/cm}^3])$

	$L[\text{km}]$	$V_W (=L/L_0)$
T2K/HK	295	± 0.055
NOVA	810	± 0.15
LBNF	1,300	± 0.24

Weak Potential & Oscillation Probability

Main effect of the weak potential on the oscillation:

$$\sin \Phi_{31} \rightarrow \frac{\sin(1 - V_W) \Phi_{31}}{1 - V_W}$$

At oscillation maximum $\sin(1 - V_W) \frac{\pi}{2} \sim 1 - \frac{\pi^2}{8} V_W^2 \sim 1$

Then, the appearance probability with the matter effect is,

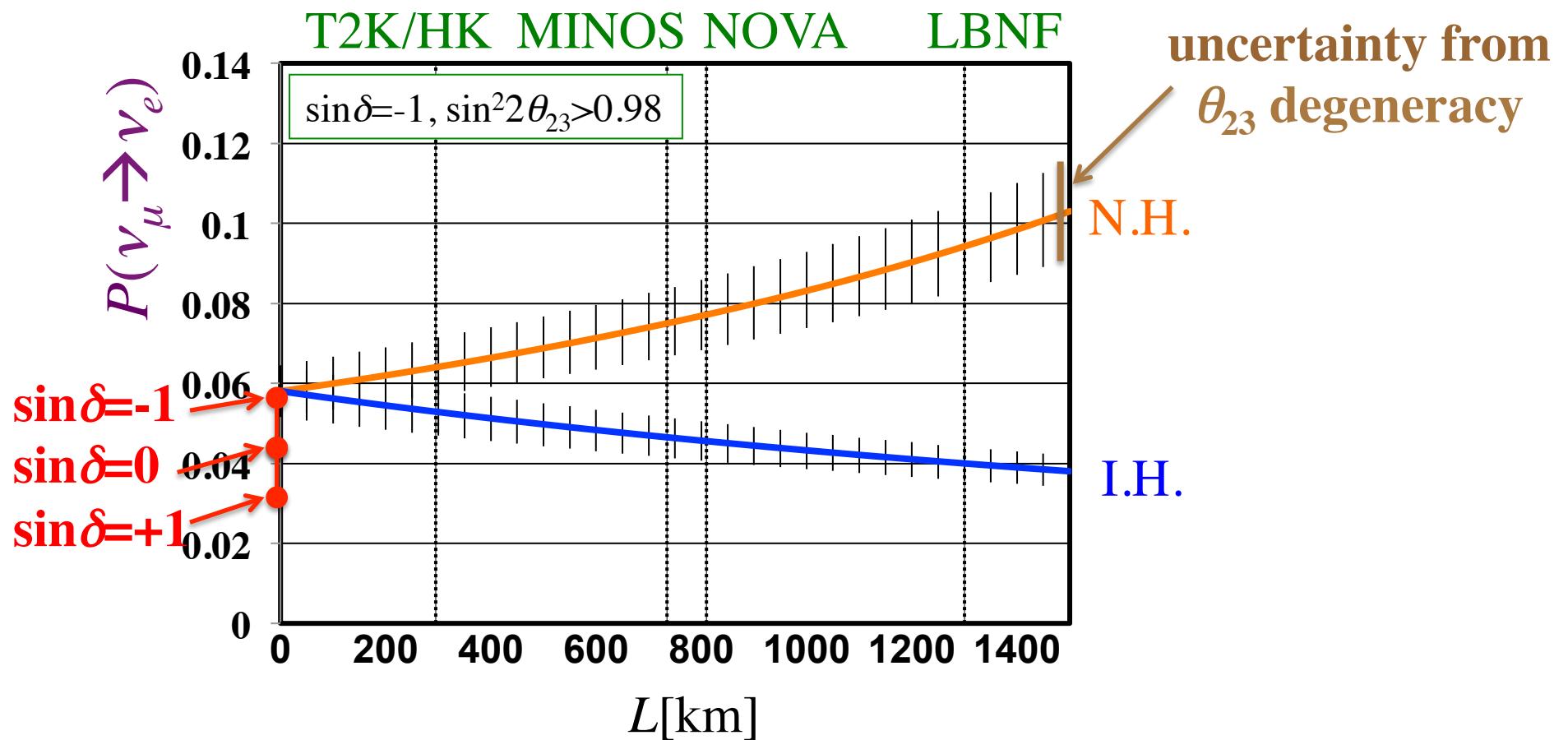
$$P(\nu_\mu \rightarrow \nu_e; @\Phi_{31}) \sim \frac{s_{23}^2 \sin^2 2\theta_{13}}{(1 - V_W)^2} \pm \frac{\pi}{2} \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \frac{\sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}}{(1 - V_W)} \sin \delta$$

Oscillation probabilities for various cases

$$\left\{ \begin{array}{l} P_{NH} (\nu_\mu \rightarrow \nu_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1-L/|L_0|)^2} - \frac{0.013}{(1-L/|L_0|)} \sin \delta \\ \\ P_{IH} (\nu_\mu \rightarrow \nu_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1+L/|L_0|)^2} - \frac{0.013}{(1+L/|L_0|)} \sin \delta \\ \\ P_{NH} (\bar{\nu}_\mu \rightarrow \bar{\nu}_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1+L/|L_0|)^2} + \frac{0.013}{(1+L/|L_0|)} \sin \delta \\ \\ P_{IH} (\bar{\nu}_\mu \rightarrow \bar{\nu}_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1-L/|L_0|)^2} + \frac{0.013}{(1-L/|L_0|)} \sin \delta \end{array} \right.$$

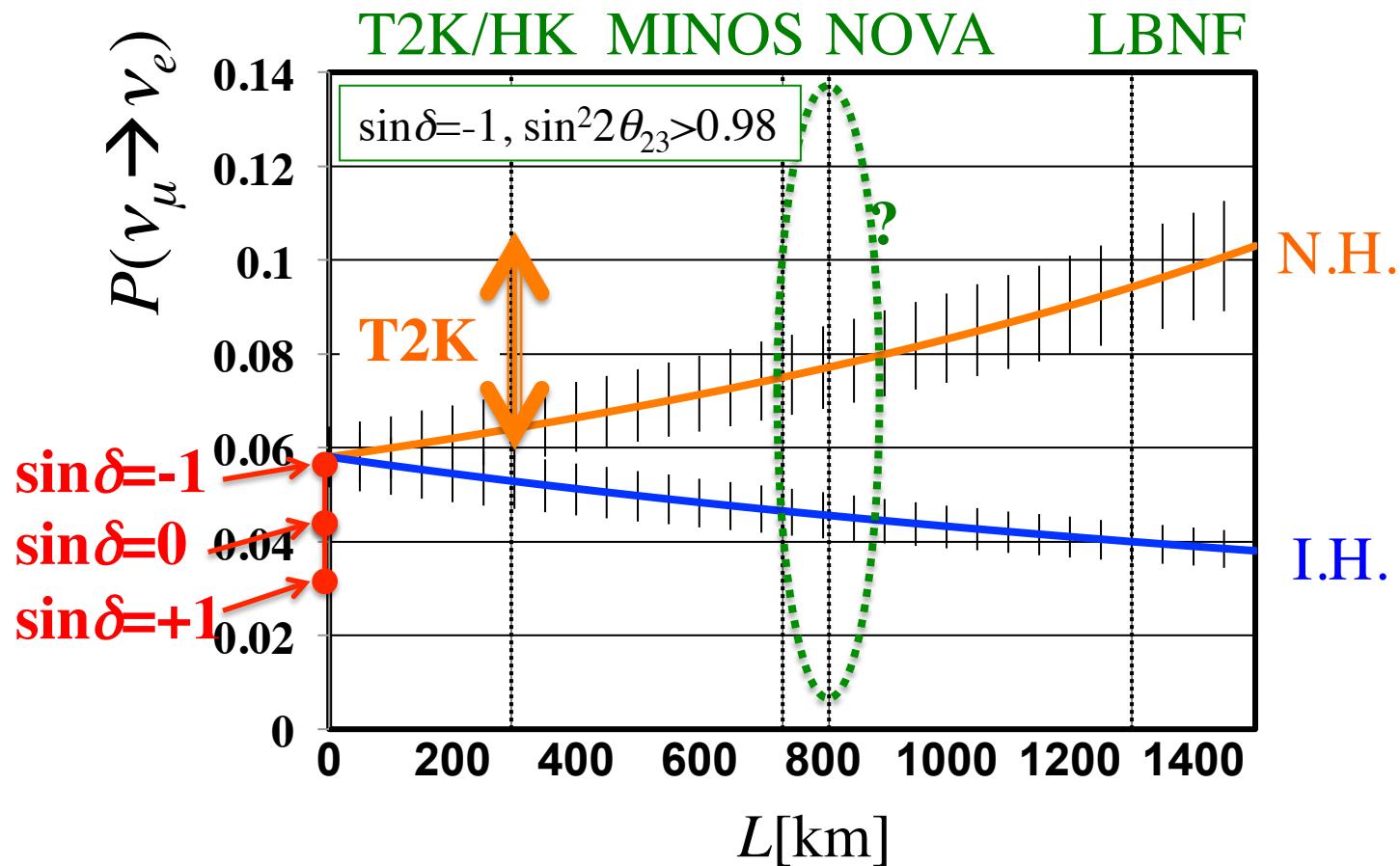
Baseline Dependence of ν_e Appearance Prob.

$$P(\nu_\mu \rightarrow \nu_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1 \pm L/|L_0|)^2} - \frac{0.013}{(1 \pm L/|L_0|)} \sin \delta$$



Baseline Dependence of ν_e Appearance Prob.

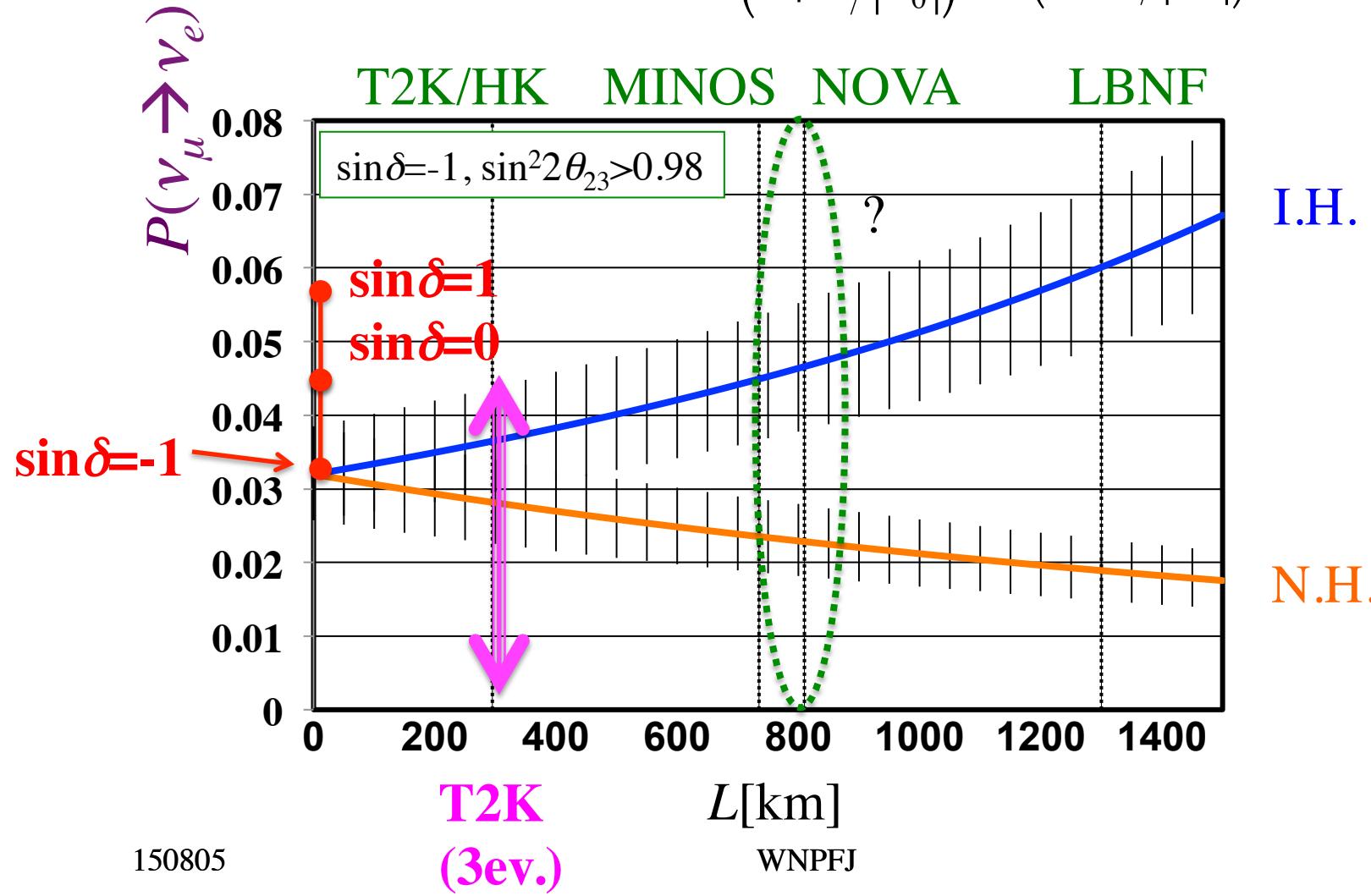
$$P(\nu_\mu \rightarrow \nu_e; @\Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1 \pm L/|L_0|)^2} - \frac{0.013}{(1 \pm L/|L_0|)} \sin \delta$$



T2K+NOVA
may enforce
the hint on
M.H. and $\sin \delta$
or may give us
tension.

Baseline Dependence of $\bar{\nu}_e$ Appearance Prob.

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e; @ \Phi_{31}) \sim s_{23}^2 \frac{0.09}{(1 \mp L/|L_0|)^2} + \frac{0.013}{(1 \mp L/|L_0|)} \sin \delta$$



CP asymmetry with the matter effect

$$A_{CP}(@\Phi_{13}) = \frac{P - \bar{P}}{P + \bar{P}} \sim -\pi \left| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \right| \frac{\sin 2\theta_{12}}{t_{23} \sin 2\theta_{13}} \sin \delta_{CP} \pm 2 \left(\frac{L}{L_0} \right)$$

$\sim -0.29 \sin \delta_{CP} \pm A_{FK}$

fake CP asymmetry

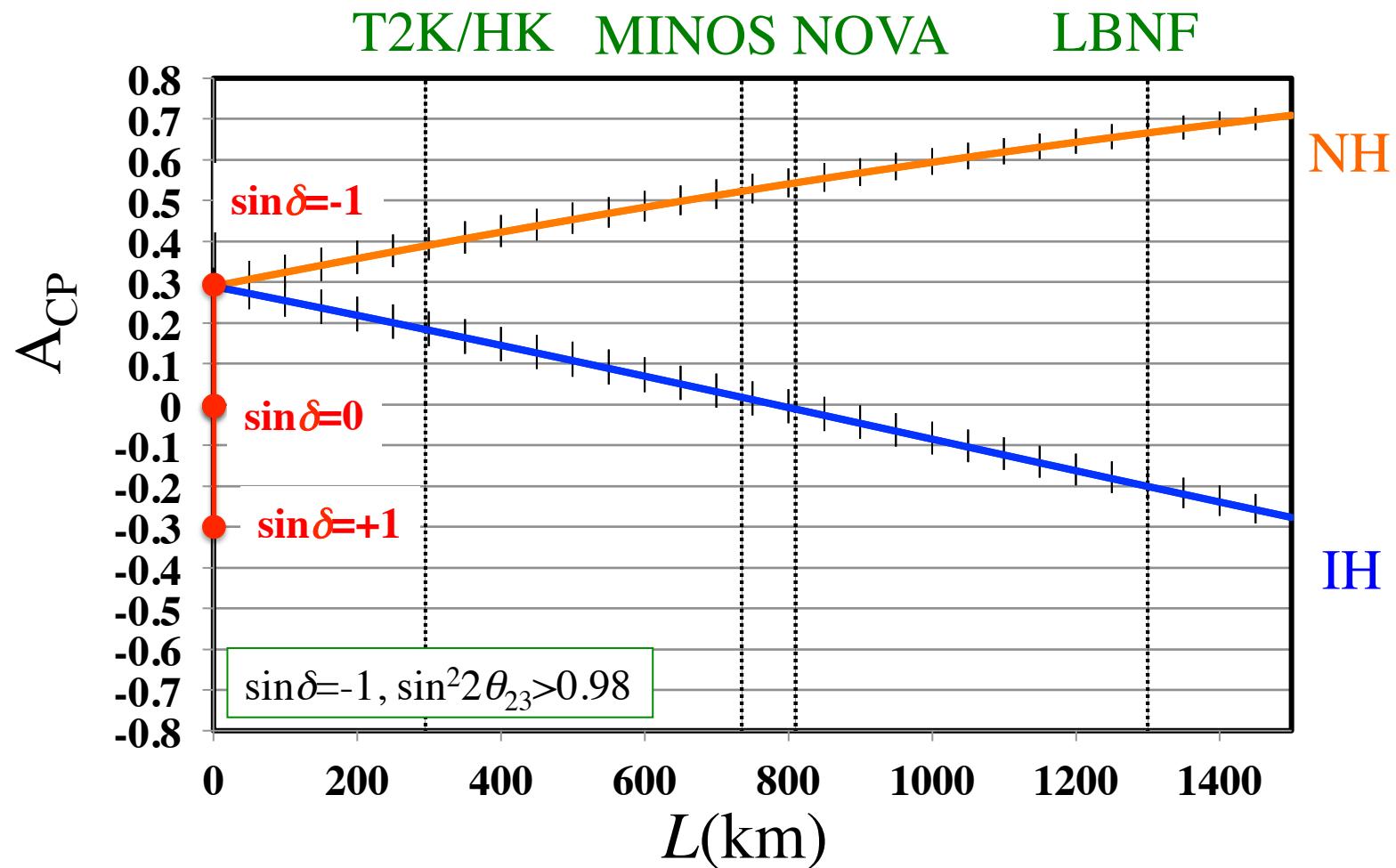
	$L[\text{km}]$	V_W	$A_{FK}=2(L/L_0)$
T2K/HK	295	± 0.055	± 0.11
Nova	810	± 0.15	± 0.30
LBNF	1,300	± 0.24	± 0.48

Error of the $\sin \delta$ measurement

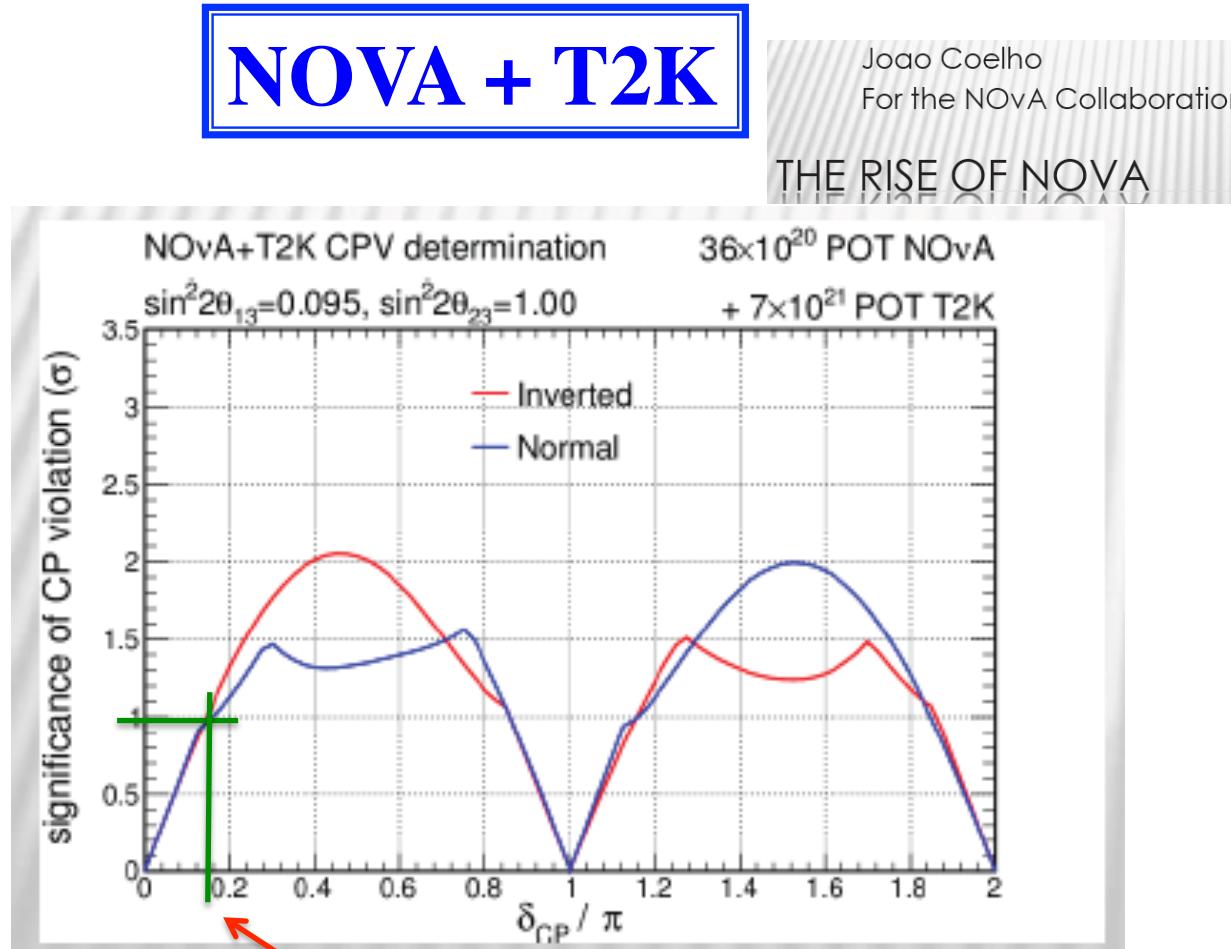
$$\delta(\sin \delta_{CP}) = 3.4 \sqrt{(\delta A_{CP})^2 + (A_{FK} (\delta \bar{n}_e / \bar{n}_e))^2}$$

Baseline Dependence of CP asymmetry

$$A_{CP} \sim -0.29 \sin \delta \pm 2 \left(\frac{L}{L_0} \right)$$



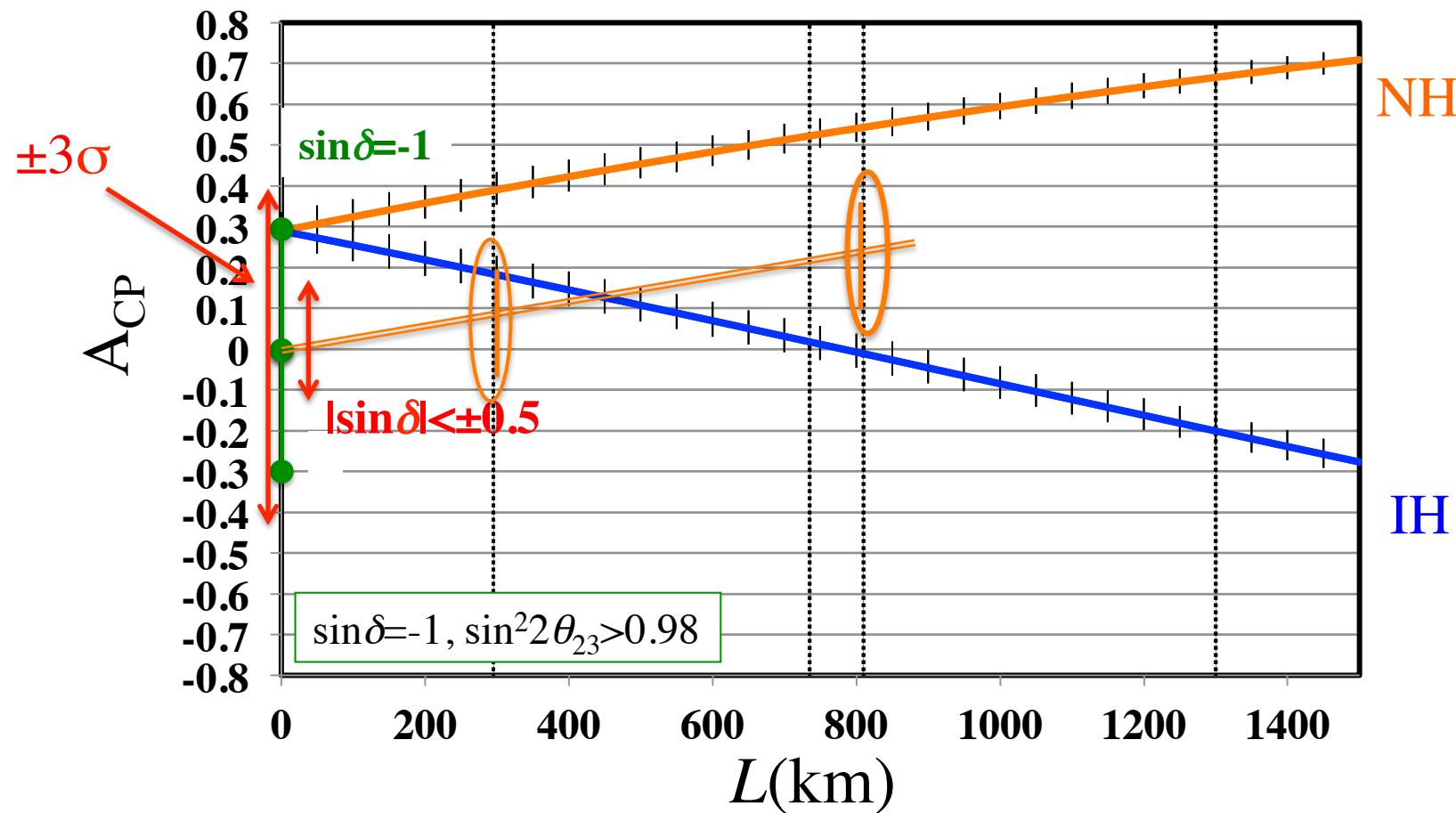
Will evaluate the sensitivity by
3 σ error of $\sin\delta_{CP}$ assuming $\delta_{CP}=0$.



NOVA + T2K

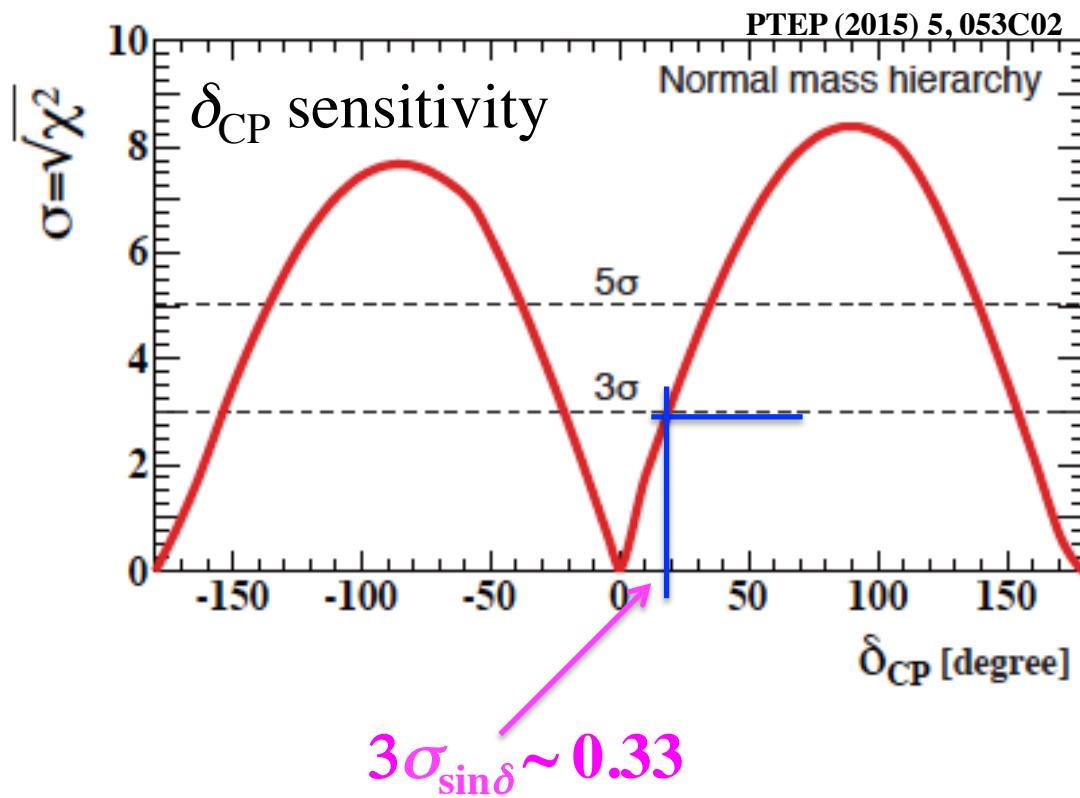
$$A_{CP} \sim -0.29 \sin \delta \pm 2(L/L_0)$$

T2K/HK MINOS NOVA LBNF



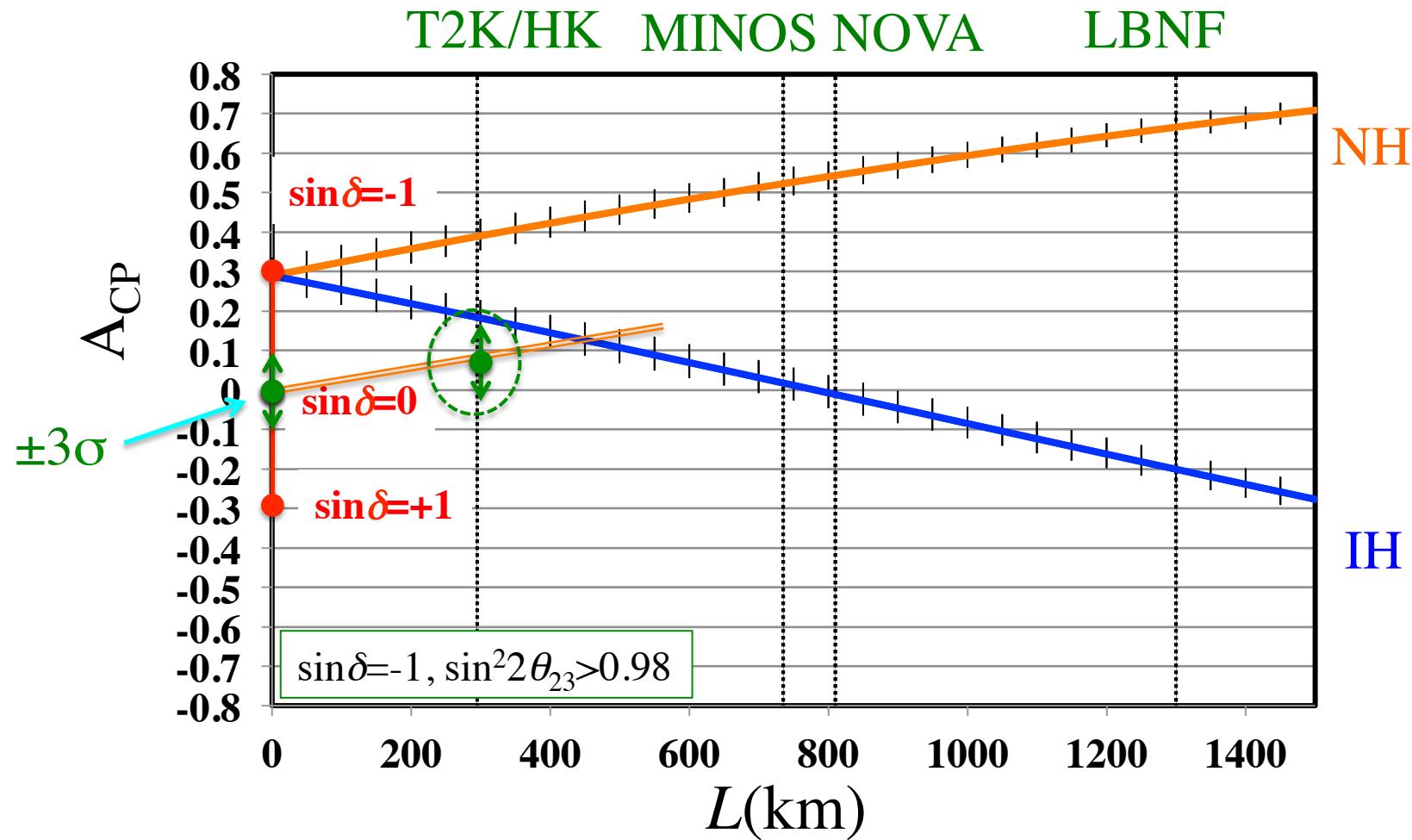
May be possible to limit δ_{CP} by 2σ but not 3σ .

HK case



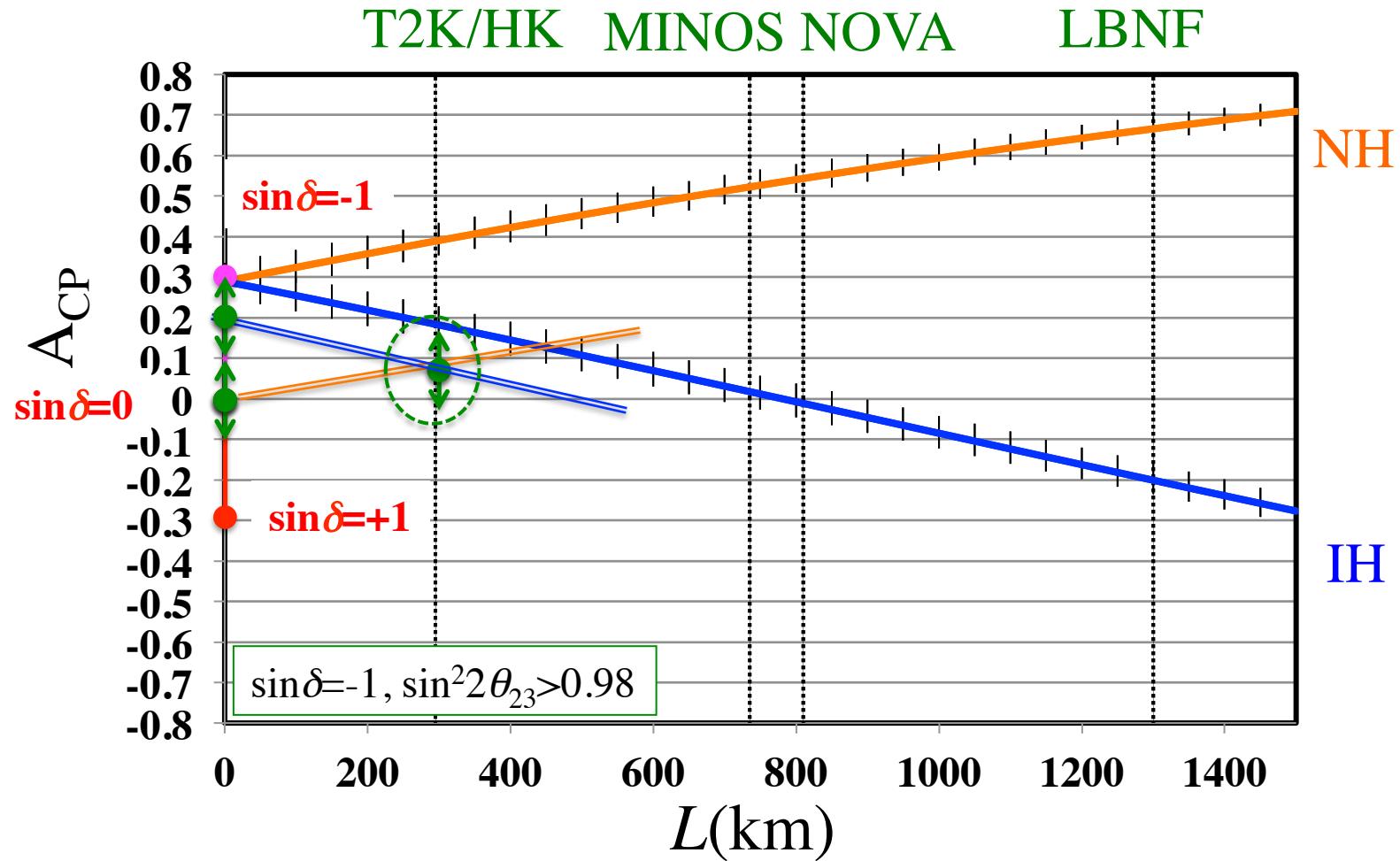
HK case

If $\sin\delta=0$ & N.H. and HK measured the expected value.



If M.H. is known, $|\sin\delta|<0.33(3\sigma)$ can be obtained.

HK case

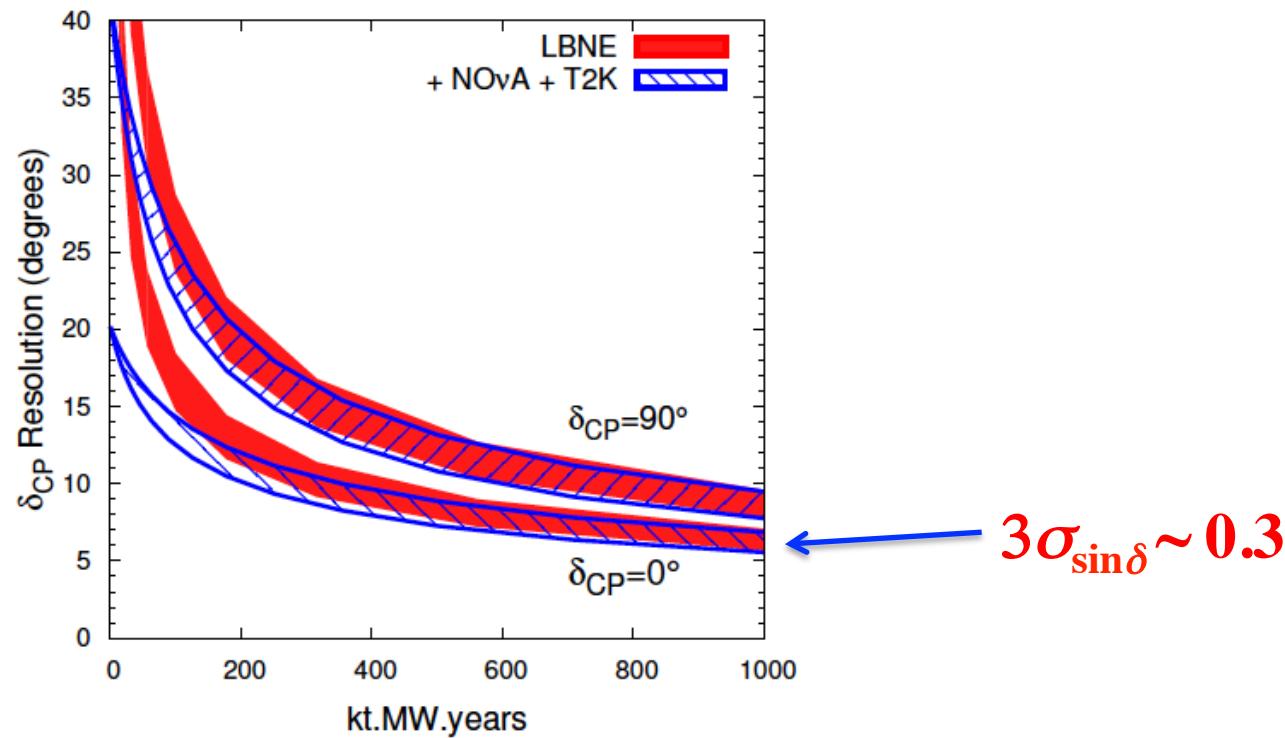


If M.H. is not known, there are two solutions.
 $\sin \delta = 0$ can not be confirmed. \rightarrow M.H. is necessary.

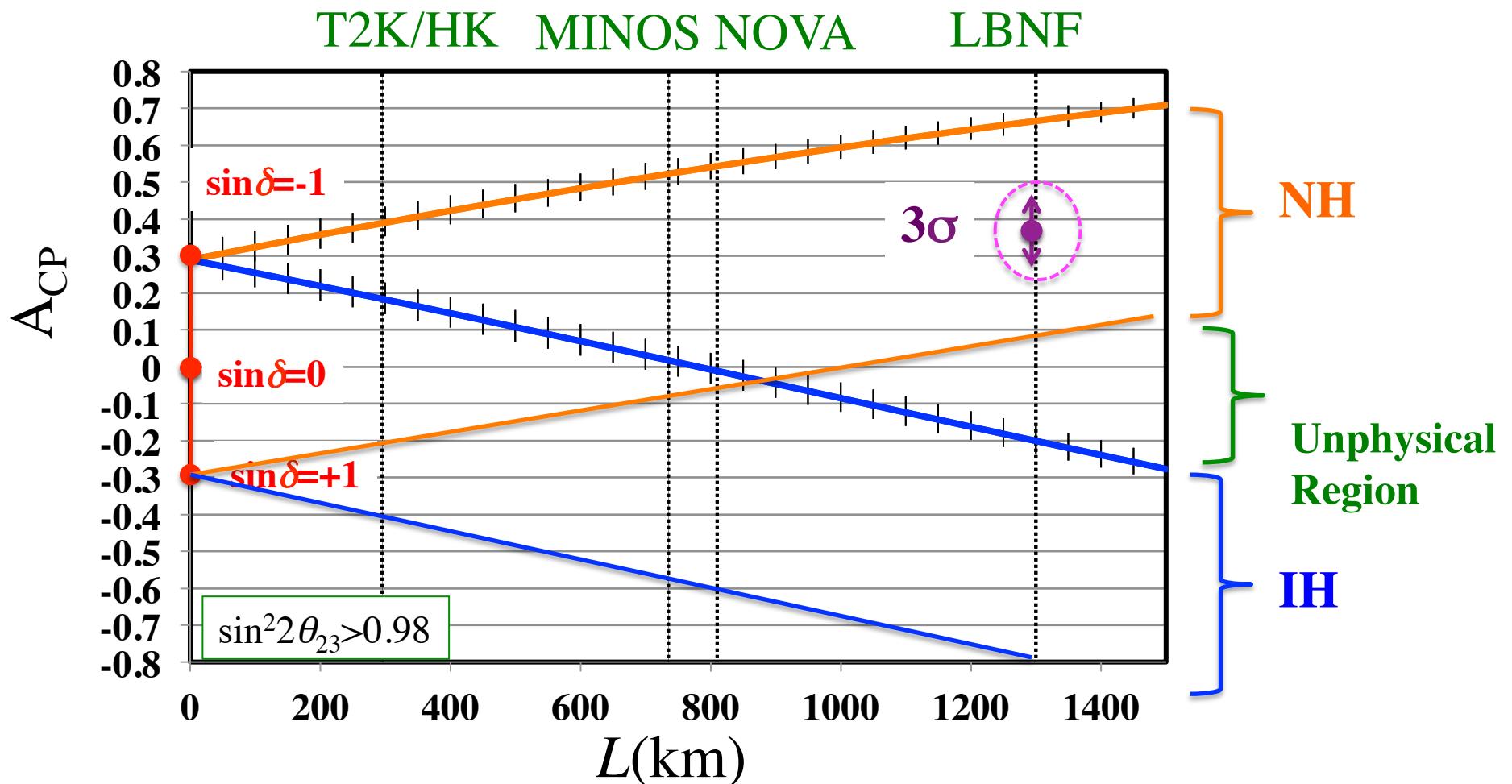
LBNF case

arXive: 1307.7335

δ_{CP} Resolution

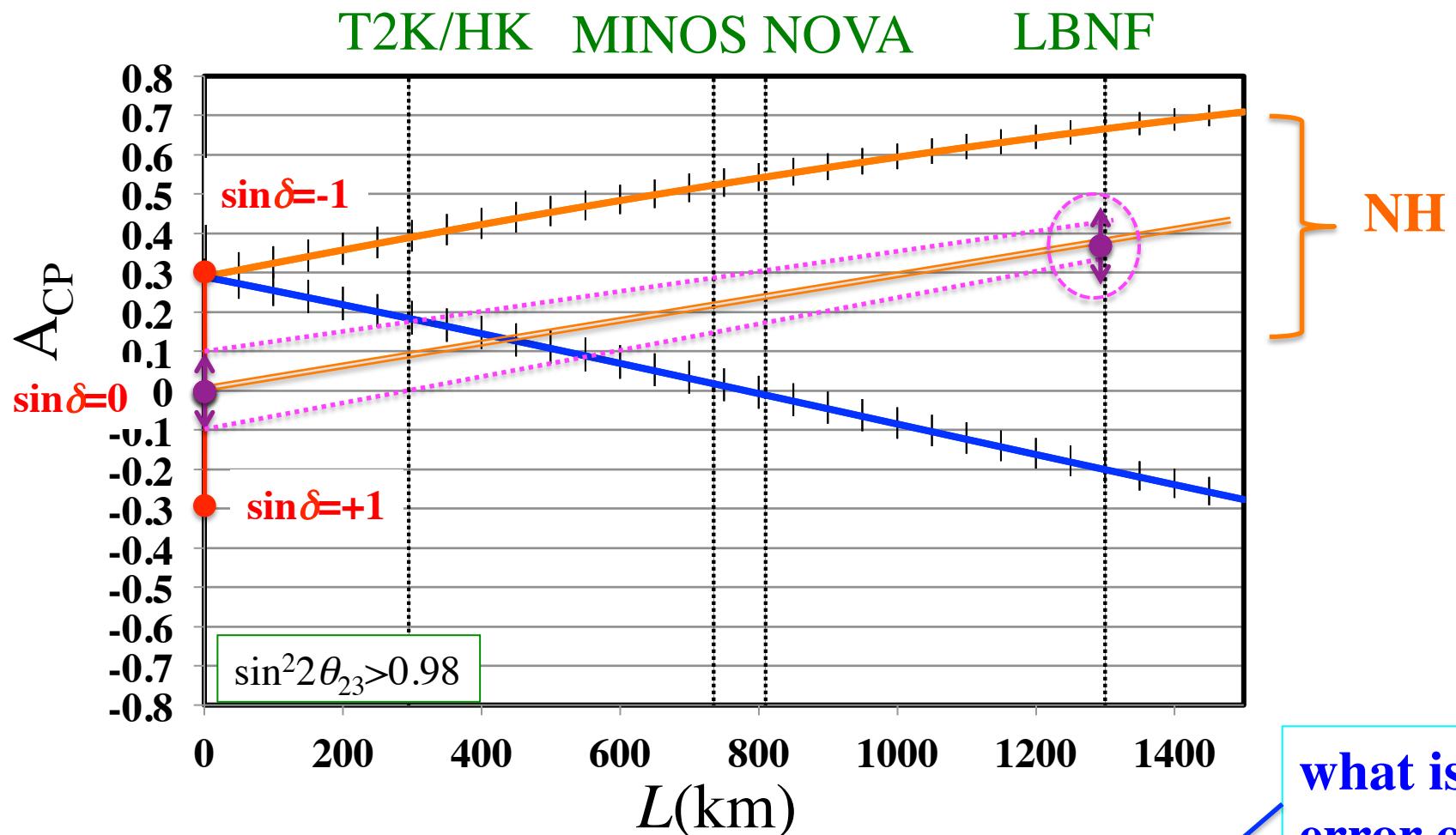


LBNF case



This case, M.H. is determined to be N.H.

LBNF case



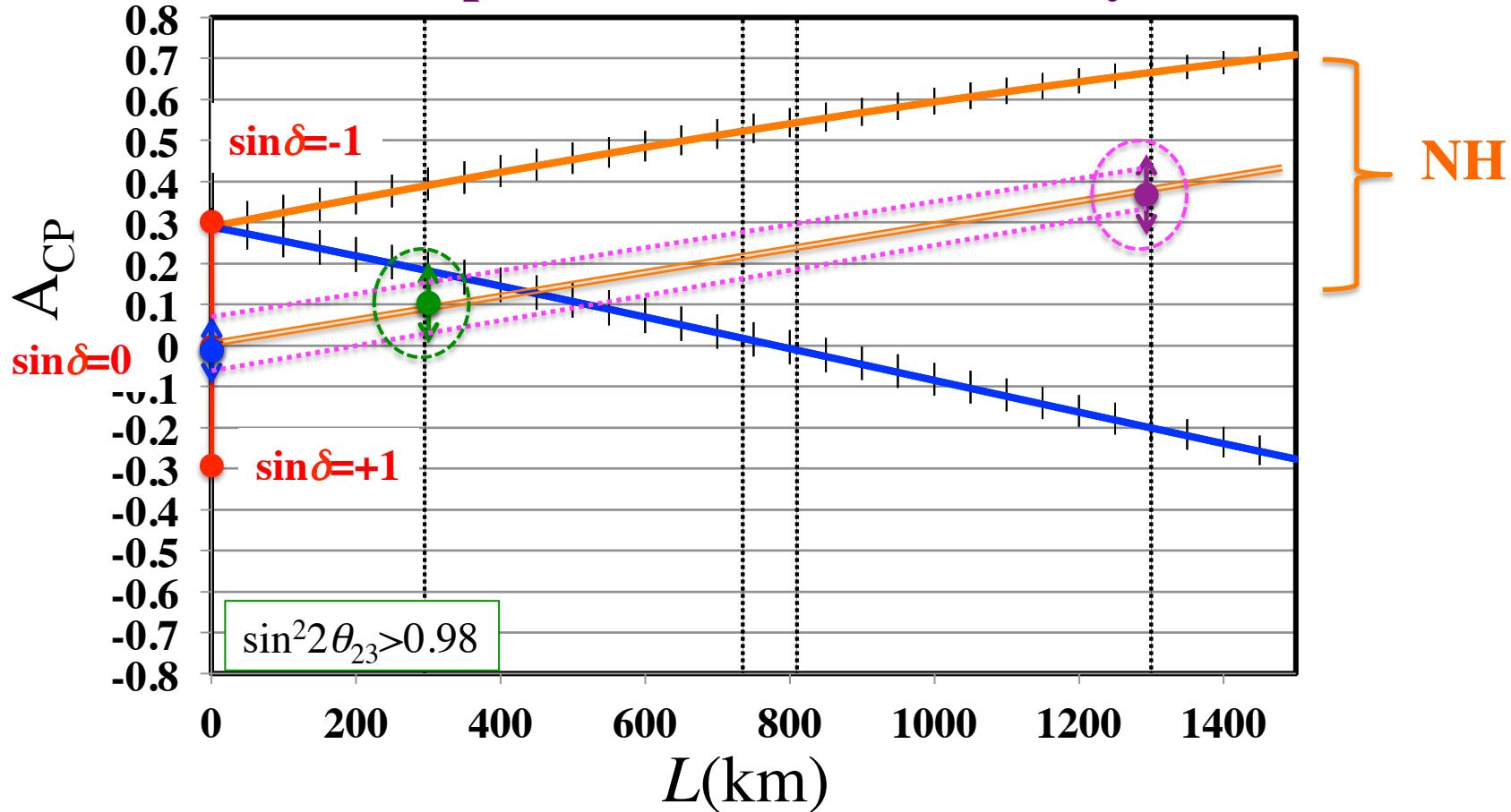
Then extrapolate to $L=0$ to obtain $\sin \delta_{CP}$.

$$\delta(\sin \delta_{CP}) = 3.4 \sqrt{(\delta A_{CP})^2 + (A_{FK} (\delta \bar{n}_e / \bar{n}_e))^2}$$

what is the error of the average density?

HK+LBNF case

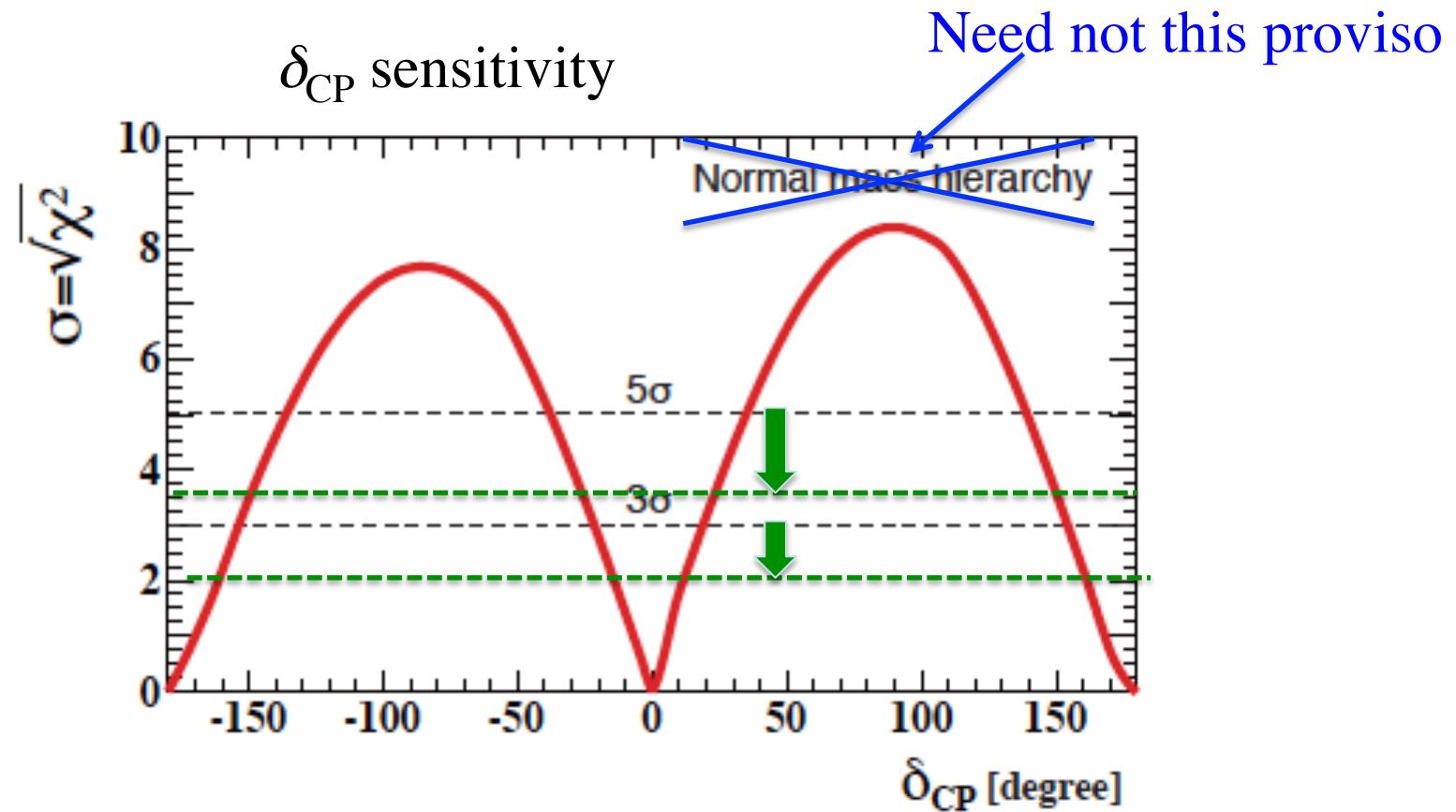
Improvement of $\sin\delta$ accuracy



* $\delta\sin\delta_{HK}=0.1$ & $\delta\sin\delta_{LB}=0.1$
 $\rightarrow \delta\sin\delta_{HK+LB}=0.071??$ (common error?)

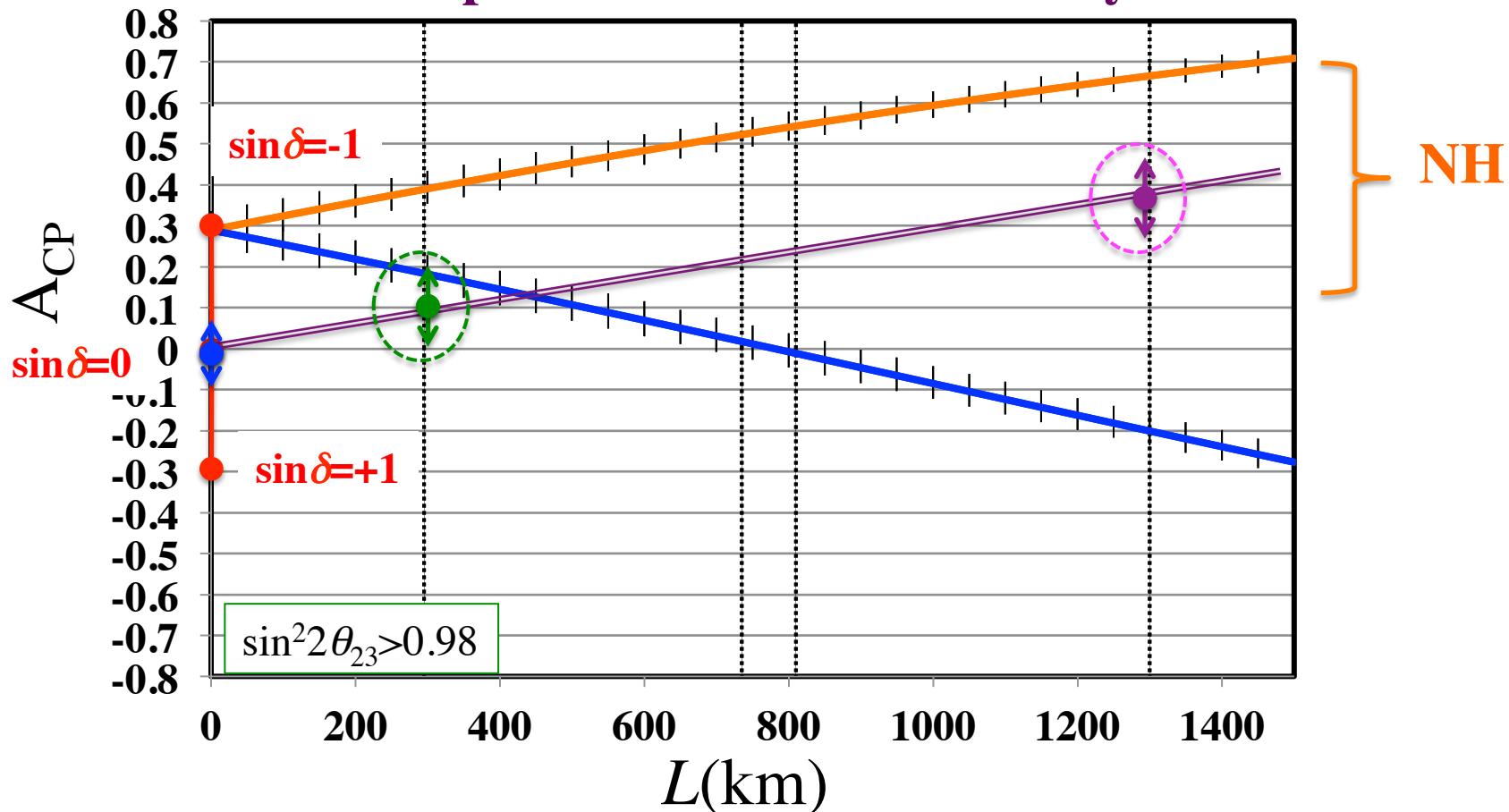
HK+LBNF case

If $\delta \sin \delta_{\text{CP}} \sim 0.1 \rightarrow \delta \sin \delta_{\text{CP}} \sim 0.1/\sqrt{2}$ by combining with LBNF



HK+LBNF case

Improvement of $\sin\delta$ accuracy

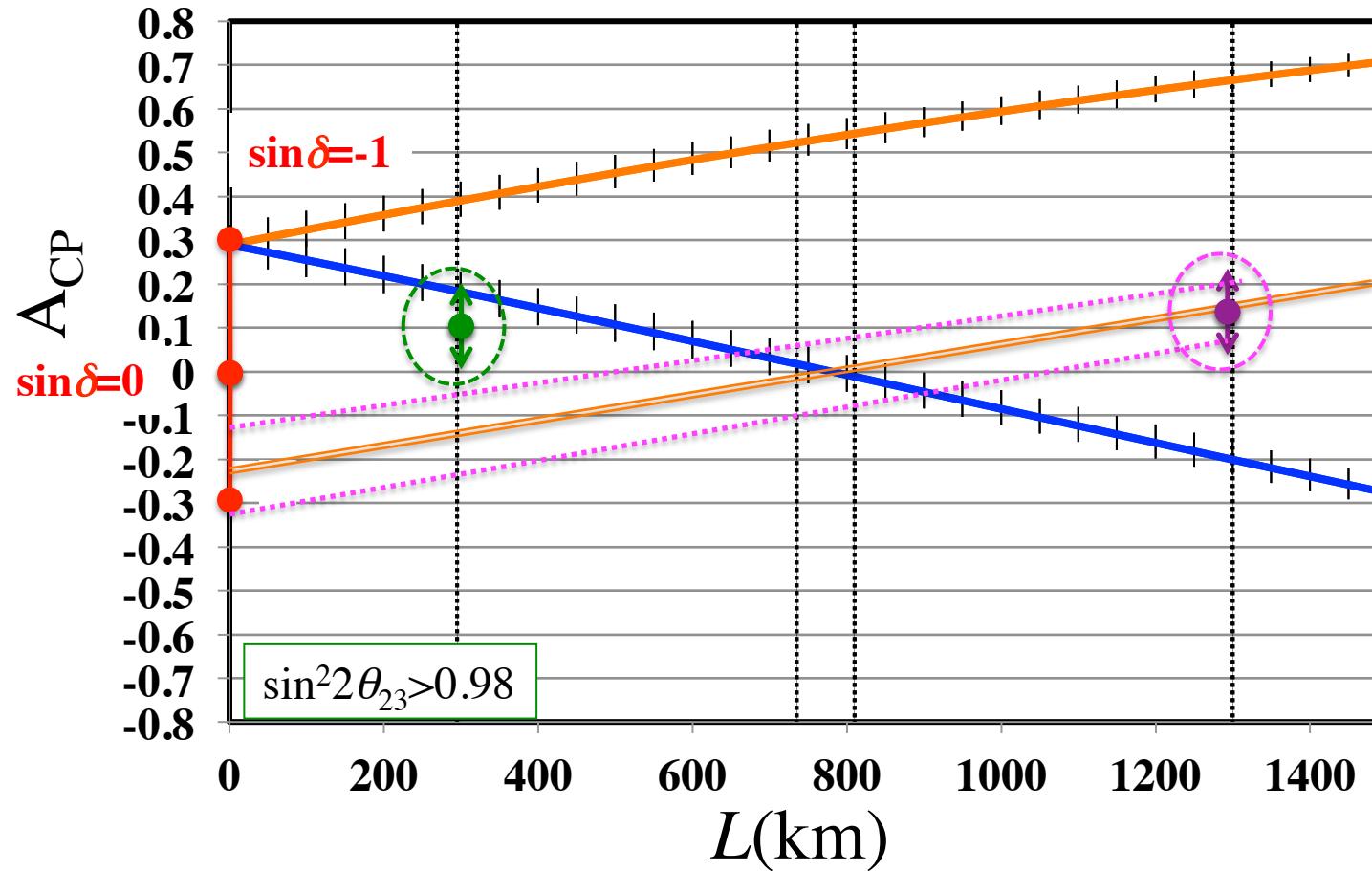


* MSW error independent analysis is possible.

$$\sin\delta = 3.4 \frac{L_{HK} A_{LB} - L_{LB} A_{HK}}{L_{LB} - L_{HK}}$$

HK+LBNF case

Strict test of the standard neutrino scheme and MSW effect.



This indicates a new physics or failure of the standard MSW

Energy dependence of the oscillation

$$\sin(1 - V_W) \Phi_{31} = \sin\left(\Phi_{31} - \frac{n_e G_F}{\sqrt{2}} L\right)$$

Constant phase shift ($\Delta\Phi$) at given L

	$L[\text{km}]$	V_W	$2(L/L_0)$	$\Delta\Phi[\text{rad}]$
T2K/HK	295	± 0.055	± 0.11	± 0.086
NOVA	810	± 0.15	± 0.30	± 0.24
LBNF	1300	± 0.24	± 0.48	± 0.38

$$\Delta\Phi_{LB} - \Delta\Phi_{HK} = \frac{G_F}{\sqrt{2}} (\bar{n}_e^{LB} L_{LB} - \bar{n}_e^{HK} L_{HK}) \sim 0.29?$$

Strong test of MSW with the same osc. mode.

Any merit compared with using Φ_{31} from the ν_μ disappearance?

On the complementarity of Hyper-K and LBNF

- * Enhance the sensitivity of CPV
- * Solving θ_{23} degeneracy
- * Improve precision of oscillation parameters. (not only δ_{CP} ..)
- * Search for non standard phenomena: different L and E
- * Nucleon decay: different channel
- * Supernova: flavor separated measurements

:

The last sentence of this report.

The benefit that will accrue from the parallel implementation of these complementary experiments should be quantified at an early stage.

→ A concrete benefit: Proposals will become stronger

Conclusion

Be Bosons;

$$|1+1|^2=4,$$

Rather Incoherence;

$$|1|^2+|1|^2=2,$$

No Fermions;

$$|1-1|^2=0.$$